



Tallinn University of Technology, May 2025

**TAL  
TECH**

Estonian Doctoral School



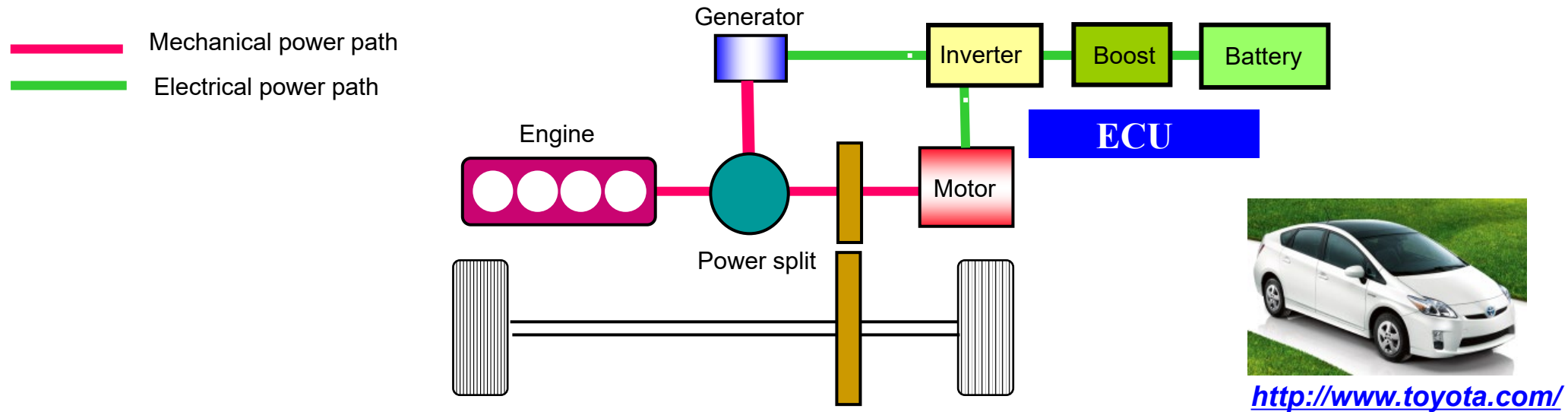
# “Energy & Systems”



**Prof. Alain BOUSCAYROL, Prof. Betty LEMAIRE-SEMAIL**



- More complex systems
  - Hybrid systems ... several technologies and operations to combine
  - Example: THS from Toyota (hybrid electric vehicle)



How to manage the various power flows?  
How to optimise energy consumption?

multi-layer control ?

- More efficient systems with same performances
  - New systems for reduction of energy consumption...  
...for higher performances
  - Example: VAL subway (Siemens)



1984 – VAL 206  
First automatic subway



position accuracy



2000 – VAL 208  
new PM machines



loss reduction



201x – NeoVAL  
new supply system

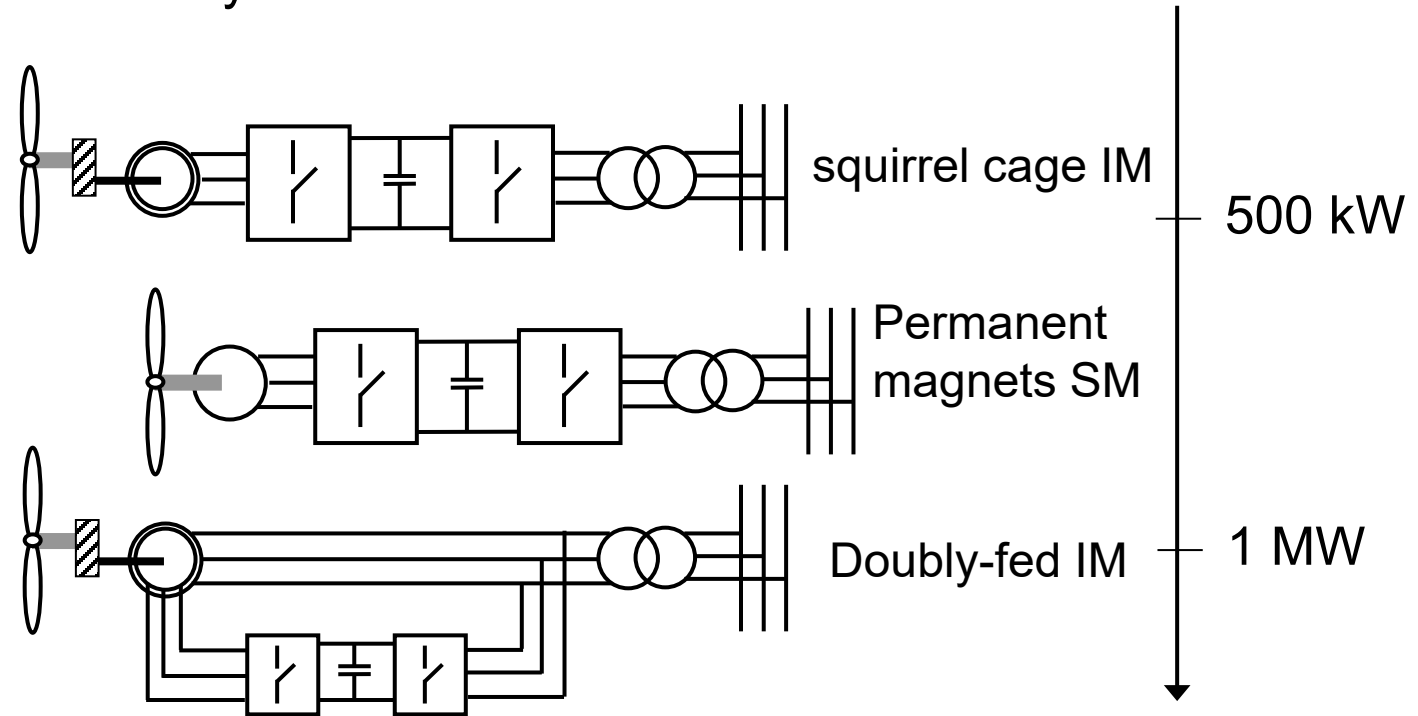


more energy recovery

How to ensure high dynamical and efficiency?  
(double objective : dynamics and energy)

multi-objective control ?

- More renewable energy conversion systems
  - Different systems for different applications and ranges
  - Example: wind energy conversion systems



How to design systems?

How to compare systems?

How to control the different systems?

flexible control?

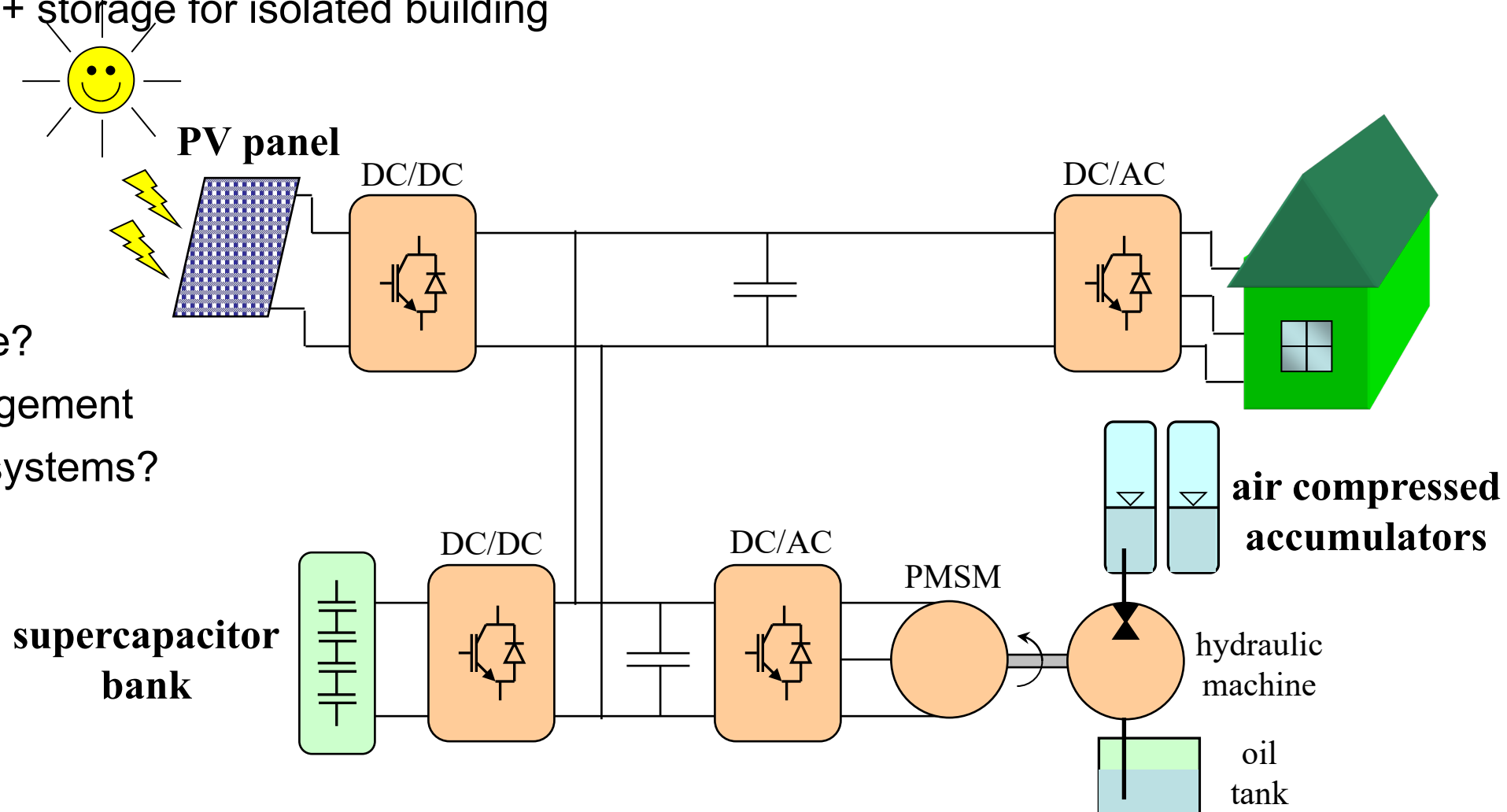
- More flexible supply systems
  - Balanced between generation and load
  - Example of PV + storage for isolated building



[Bossmann & al. 2007]

(Switzerland)

How to design storage?  
Optimal energy management  
between subsystems?

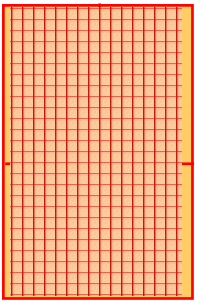


# Simulation for ever!

Launching Simulation Software is more and more a “Pavlov reflex”



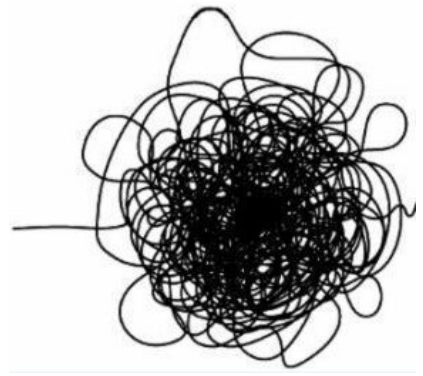
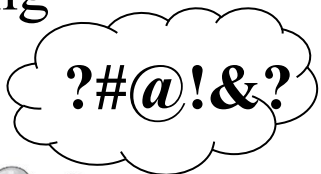
Fast development with “copy & paste”



**system simulation**



Nightmare for finding errors



**results** confidence? accuracy?



- 1 Model, Representation, Simulation**
- 2 Systems and Interaction**
- 3 Energy and Causality**
- 4 Graphical descriptions**

1

**Model, Representation, Simulation**

2

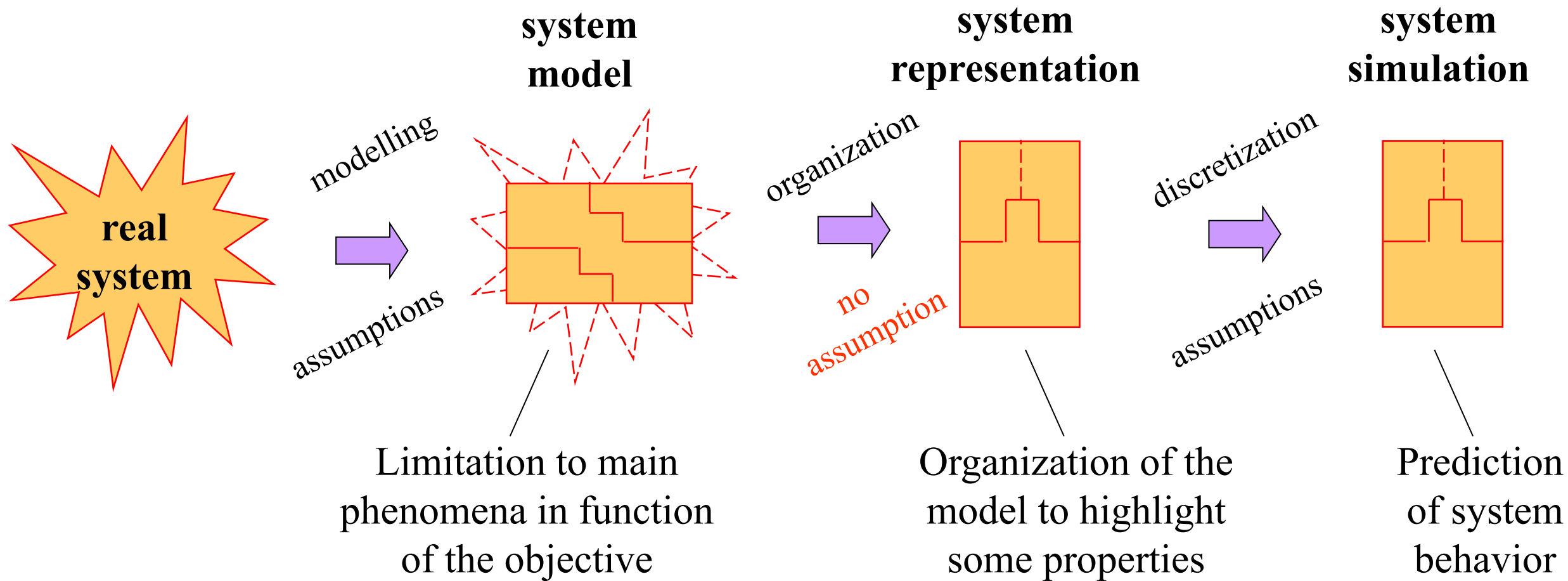
**Systems and Interaction**

3

**Energy and Causality**

4

**Graphical descriptions**



Intermediary steps are required for complex systems

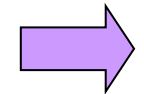


modelling  
assumptions

system model

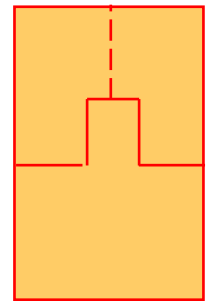


organization

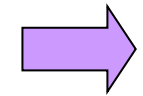


no assumption

system representation

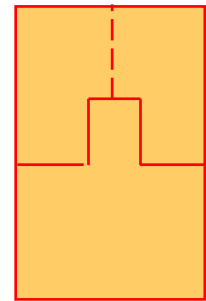


discretization

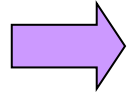


assumptions

system simulation

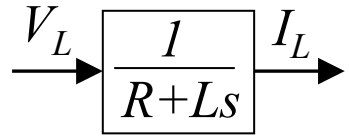
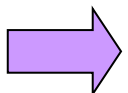


smoothing inductor

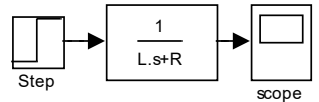
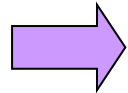


$$v_l = L \frac{d}{dt} i_L + R i_L$$

(low frequency dynamical model)



(bloc diagram +Laplace)

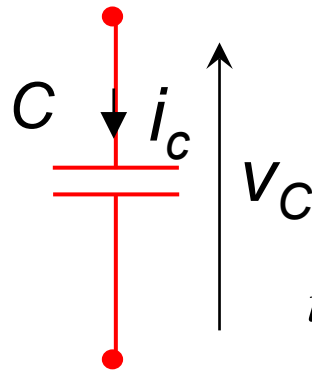


(Simulink © +Range Kutta)

**Model** = description based on physical laws  
(validity range function of assumptions)

**Representation** = organisation of a model  
in order to highlight some properties

Example: capacitor



$$i_c = C \frac{d}{dt} v_c$$

mathematical model

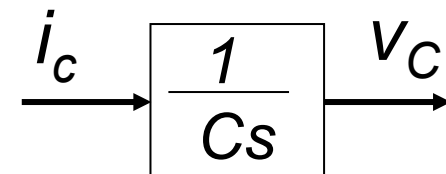
state space representation

$$\frac{d}{dt} v_c = \frac{1}{C} i_c$$

transfer function

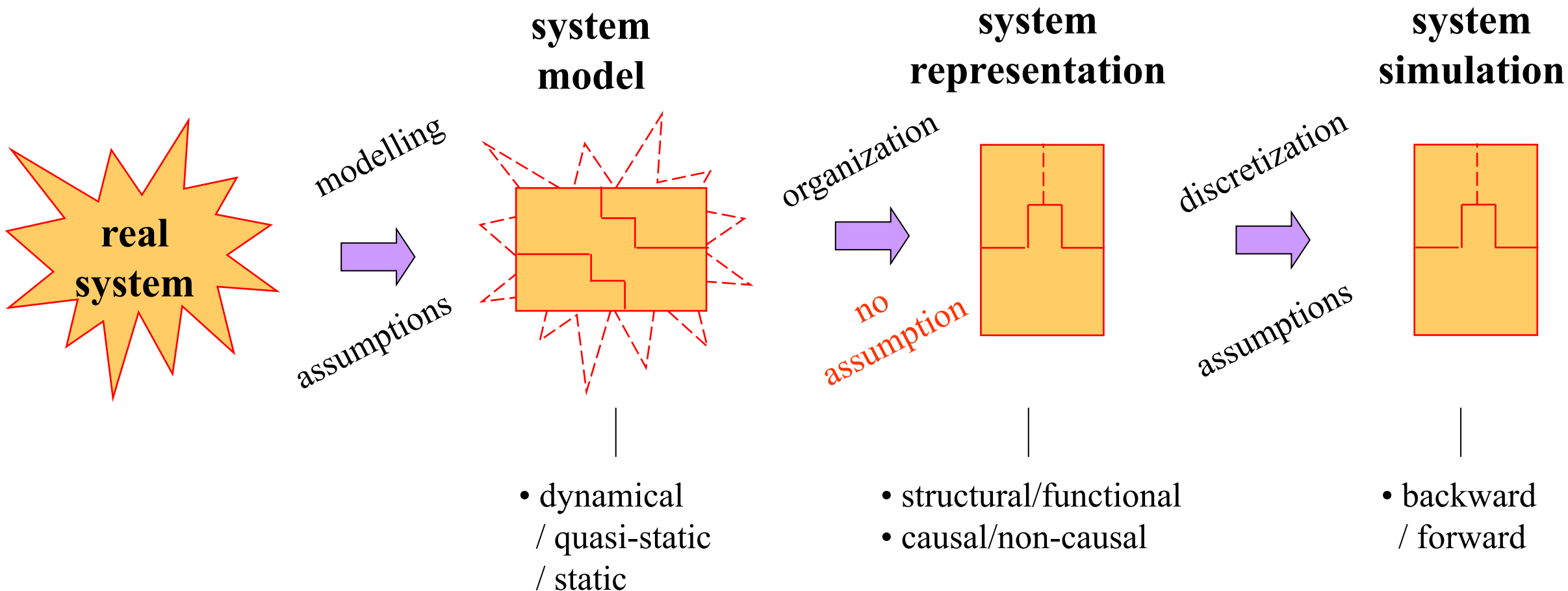
$$\frac{V_c(s)}{I_c(s)} = \frac{1}{Cs}$$

bloc diagram



COG





Different possibilities at each step in function of the objective

Which subsystem model?

## Static model

- steady state operations
- no transient states
- fast computation time
- global behavior

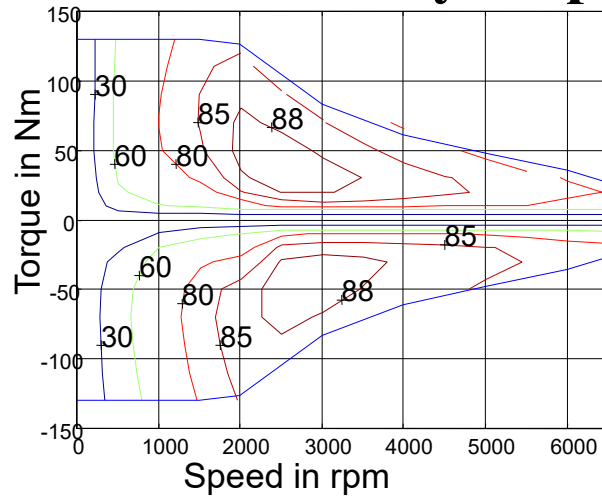
## Dynamic model

- transient state operations
- but also steady state operations
- long computation time
- detailed behavior

## Quasi-static model

- static model + main time constant
- intermediary computation time
- intermediary behavior

### static efficiency map



$$i_{DC} = \frac{T_{em} \Omega + P_t(T_{em}, \Omega)}{U_{DC}}$$

### quasi-static model

$$+ J \frac{d}{dt} \Omega = T_{em} - T_{load} - f \Omega$$

### dynamic model

$$\begin{cases} V_{Sd} = R_S i_{Sd} + \cancel{\frac{d\phi_{Sd}}{dt}} - \omega_S \phi_{Sq} \\ V_{Sq} = R_S i_{Sq} + \cancel{\frac{d\phi_{Sq}}{dt}} + \omega_S \phi_{Sd} \\ 0 = R_R i_{Rd} + \cancel{\frac{d\phi_{Rd}}{dt}} - \omega_R \phi_{Rq} \\ 0 = R_R i_{Rq} + \cancel{\frac{d\phi_{Rq}}{dt}} + \omega_R \phi_{Rd} \end{cases}$$

$$T_{em} = p \frac{L_m}{L_R} \cdot (\phi_{Rd} \cdot i_{Sq} - \phi_{Rq} \cdot i_{Sd})$$

$$J \frac{d}{dt} \Omega = T_{em} - T_{load} - f \Omega$$

## How to describe a system?

### Structural description

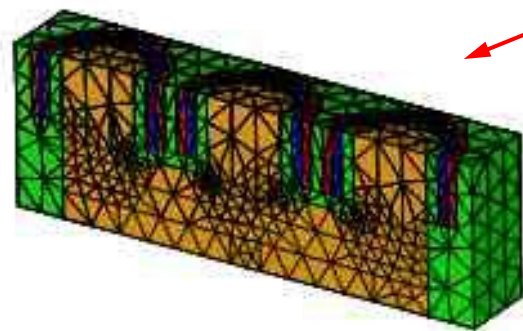
- Physical structure in priority
- Physical links between subsystems
- Design application

### Functional description

- function priority
- Virtual links between subsystems
- Analysis and control application



Example: 3-phase transformer



3D Finite Element Model

$$\begin{cases} \underline{v}_2 = m \underline{v}_1 \\ \underline{i}_1 = m \underline{i}_2 \end{cases}$$

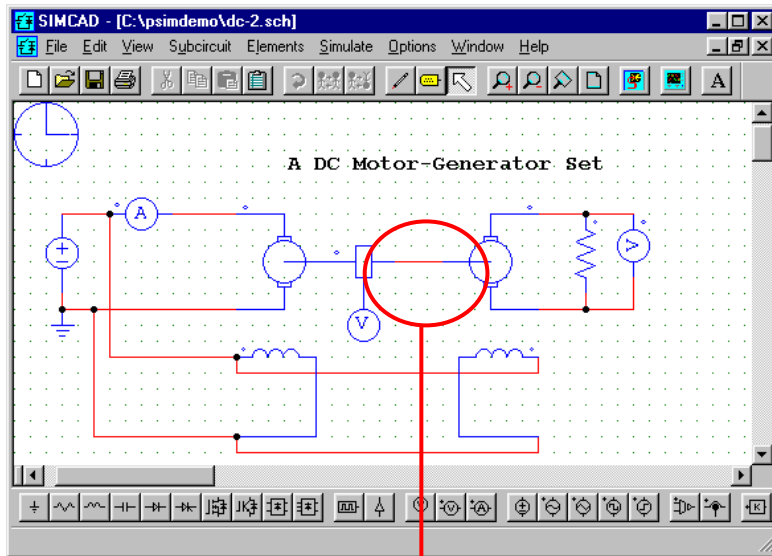
Mathematic model

Assumption: ideal transformer

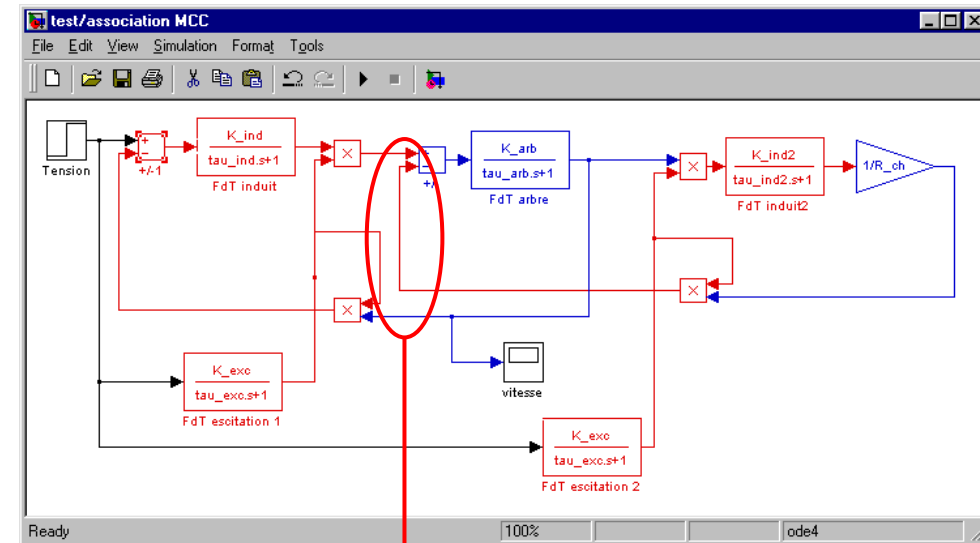
# System with two DC machines

## PSIM (structural)

## Matlab-Simulink (functionnal)



machines connected by a unique physical link (shaft)



machines connected by two virtual links (torque/speed)

### How to connect subsystem?

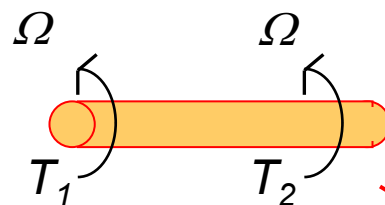
#### Causal description

- fixed input and output
- output = integral function of inputs
- difficult interconnection subsystems
- basic solver

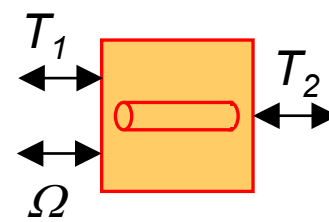
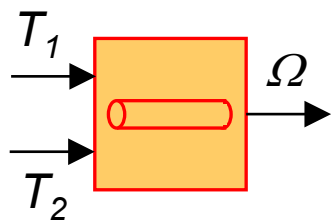
#### Acausal description

- floating inputs and outputs
- different relationships
- easy subsystem interconnection
- specific solver required
- simulation library

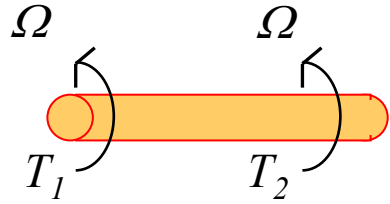
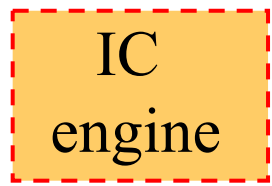
Example: rotating shaft



$$J \frac{d}{dt} \Omega = T_1 - T_2$$

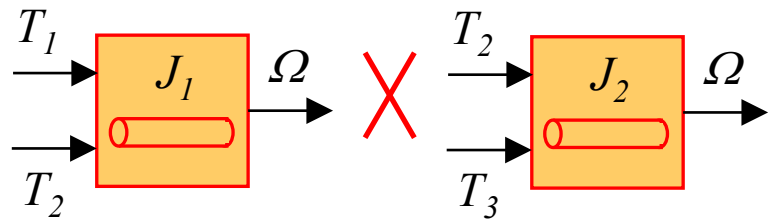


## Example

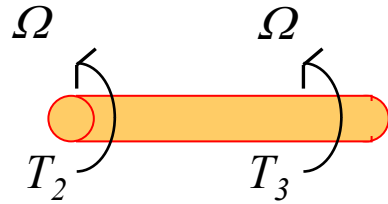
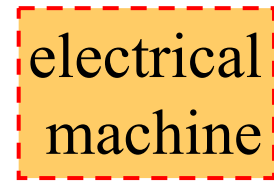
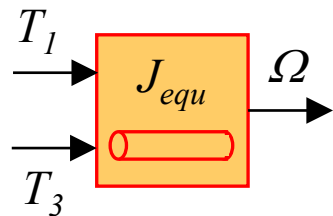


$$J_1 \frac{d}{dt} \Omega = T_1 - T_2$$

### causal description

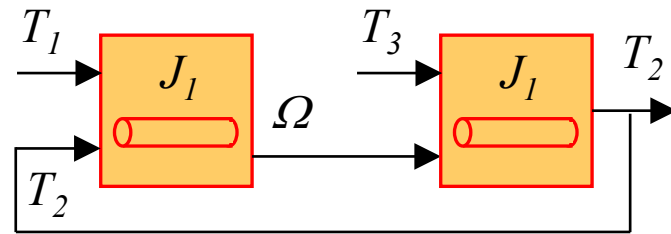


$$(J_1 + J_2) \frac{d}{dt} \Omega = T_1 - T_3$$



$$J_2 \frac{d}{dt} \Omega = T_2 - T_3$$

### acausal description



derivative relationship

specific solver

Which method to compute the model?

**Forward approach**

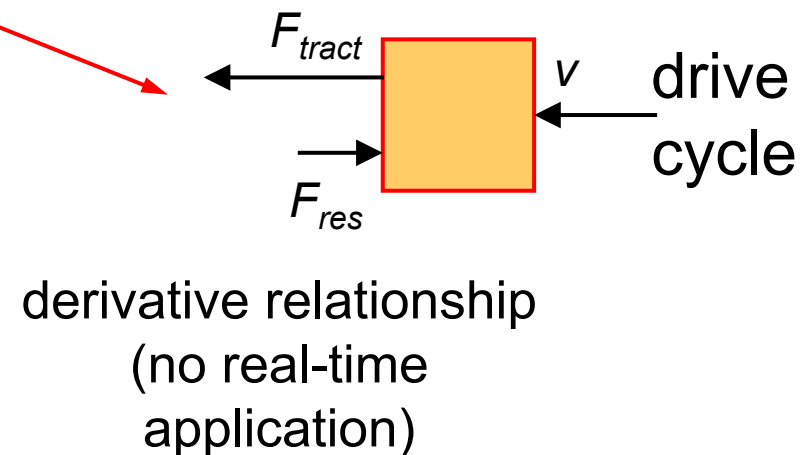
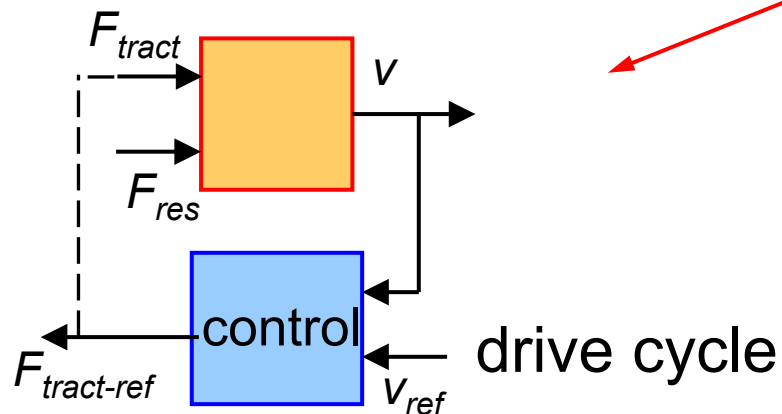
- from the cause to the effect
- respect of the energy flow
- controller required

**Backward approach**

- from the desired effect to the required cause
- anticipate energy flow
- no controller required
- needs to know the result in advance

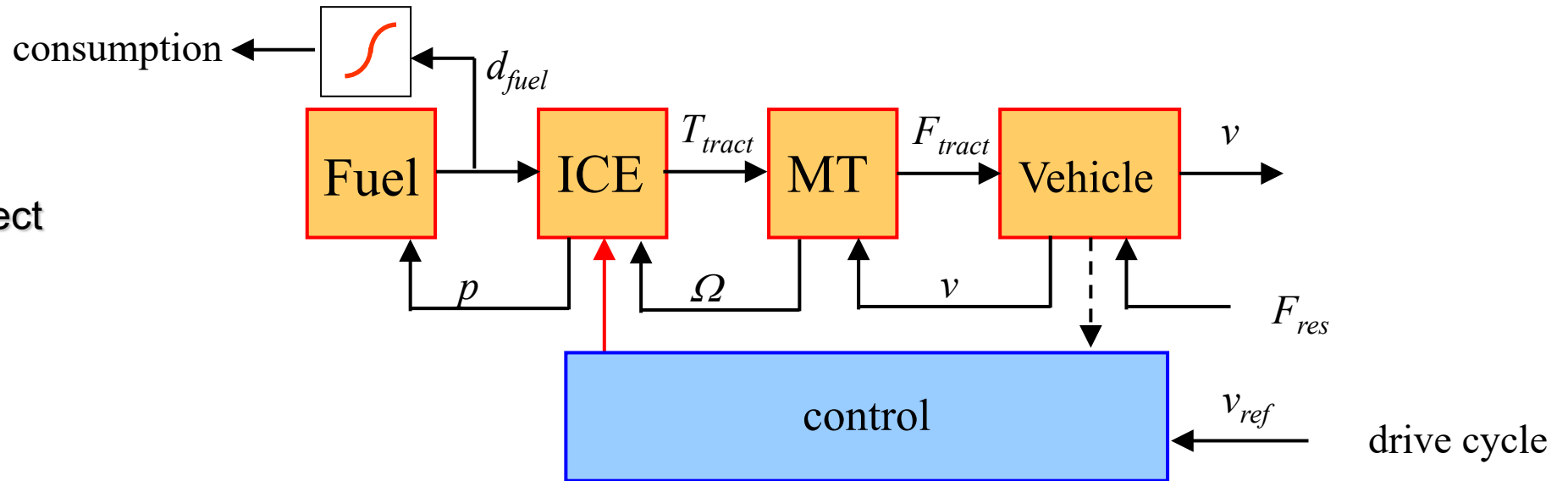
$$M \frac{d}{dt} v = F_{tract} - F_{res}$$

Example: a vehicle mass



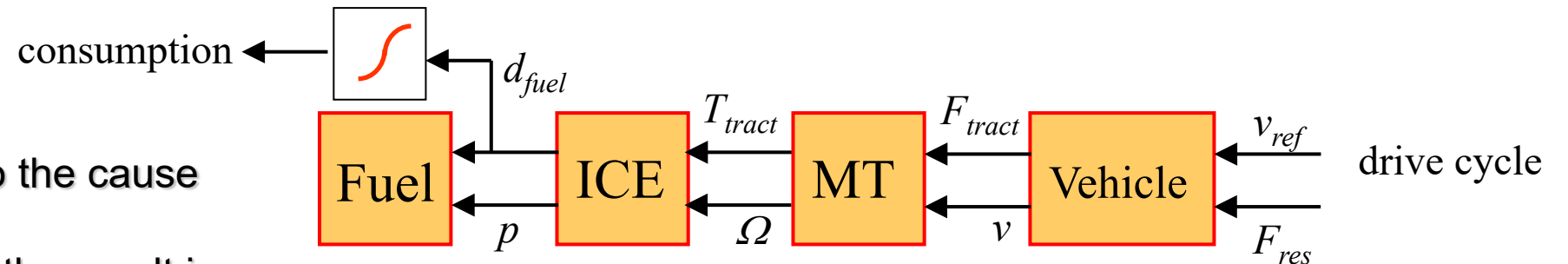
## Forward

- from the cause to the effect (direct simulation)
- needs of control

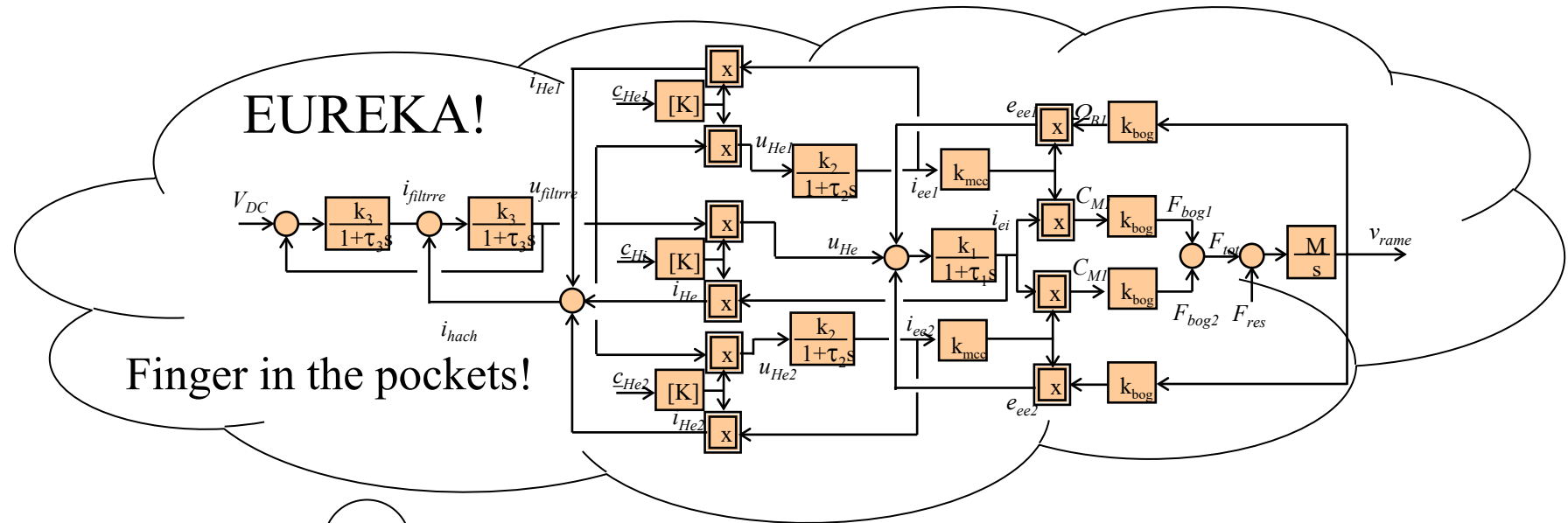


## Backward

- from the effect back to the cause (inverse simulation)
- needs of knowledge of the result in advance



could be same models, but different representations (cf. I/O)



But block diagrams:

- can be confusing for complex systems
- are limited to continuous and linear systems
- do not highlight energy properties
- do not highlight interaction between subsystems

Remember, See the wood before the trees!



Prof. C.C. Chan

1

**Model, Representation, Simulation**

2

**Systems and Interaction**

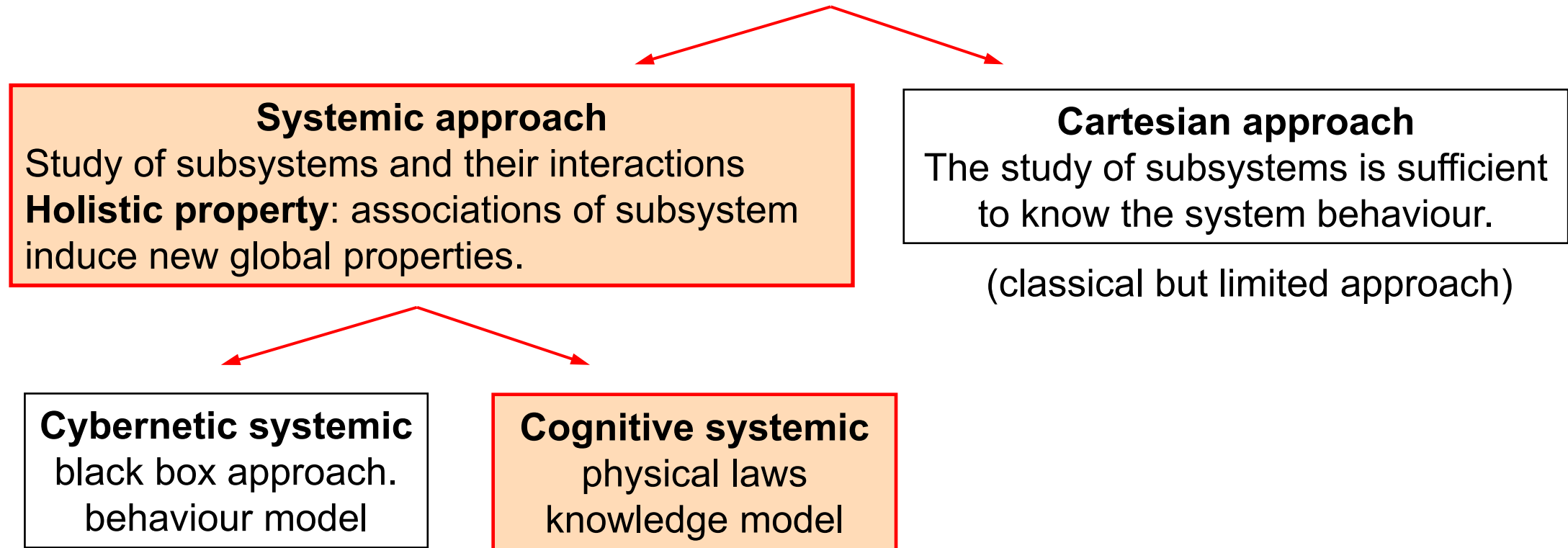
3

**Energy and Causality**

4

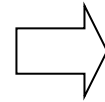
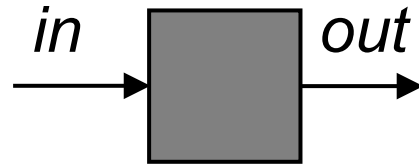
**Graphical descriptions**

**System** = interconnected subsystems

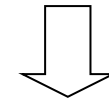


**For better performances of a system**  
**interactions** and physical laws must be considered!

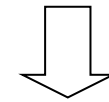
or “Black box” approach: no internal knowledge



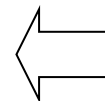
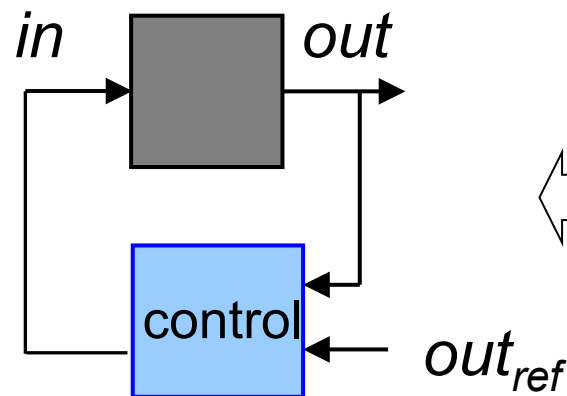
identification test:  
observation of  $out(t)$  from selected  $in(t)$



**Behavior model:**  
 $out(t) = f(t) in(t)$

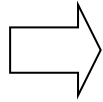


**closed-loop** control of  $out$ :  
for uncertainty compensations



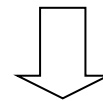
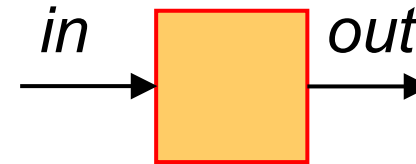
or “White box” approach: prior internal knowledge

Physical laws of  
system components

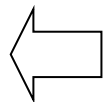
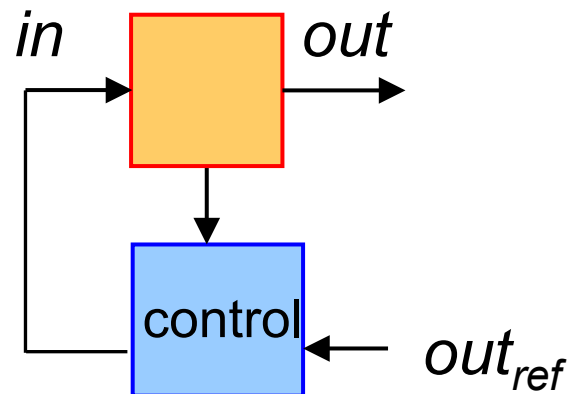


**Knowledge model:**

$$out(t) = f(t) in(t)$$

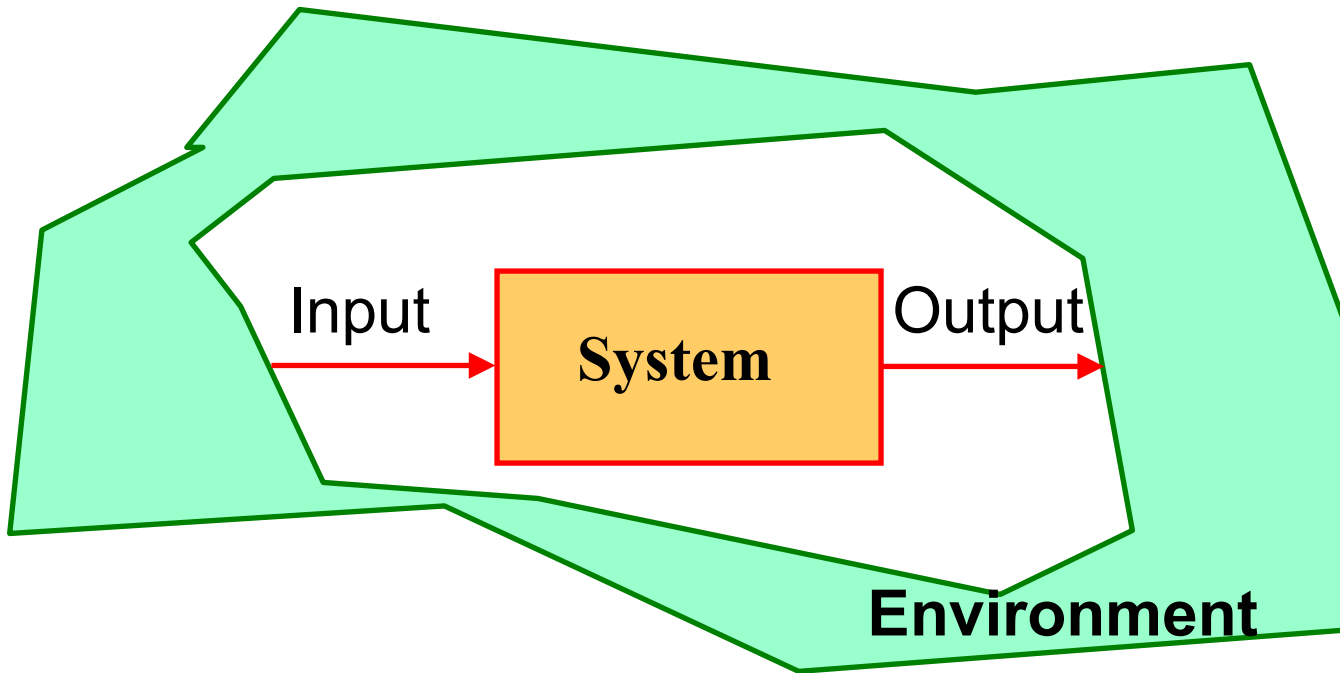


**control = inversion of model:**  
(closed loop = an inversion way)



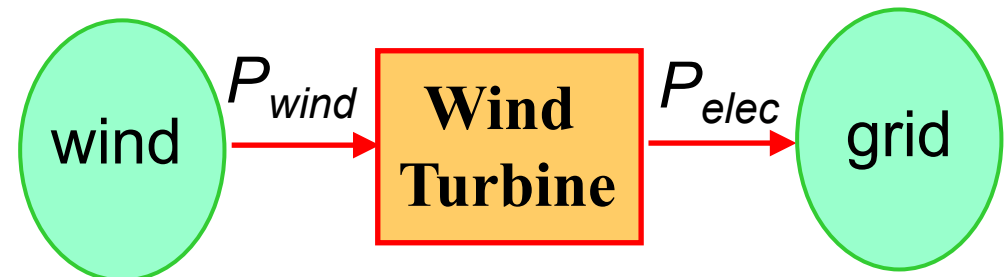
**Input:** variable produced by the environment, imposed to the system for evolution (independent of the system)

**Output:** consequence of the system evolution, imposed to its environment (not directly dependant on the environment)



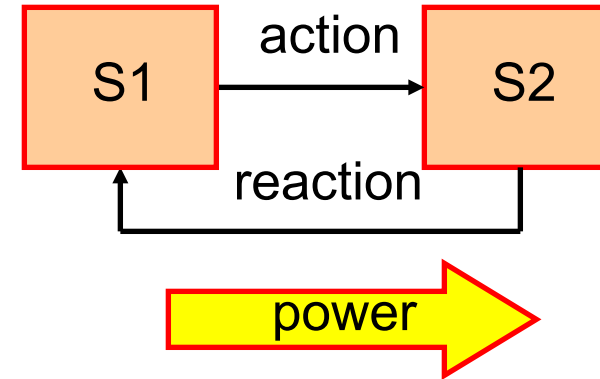
Environment & System must be defined first!

*Example: a wind turbine*



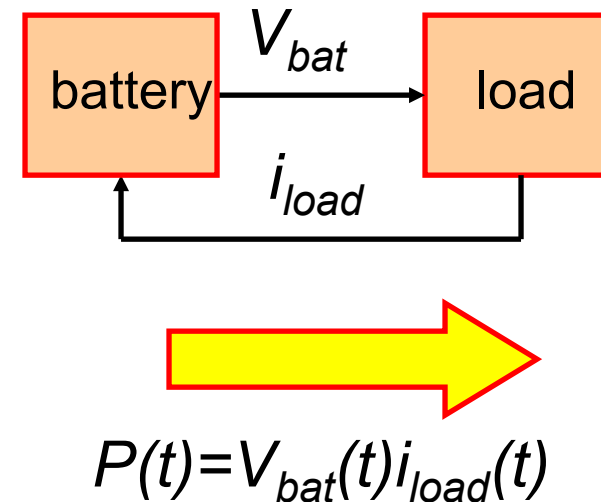
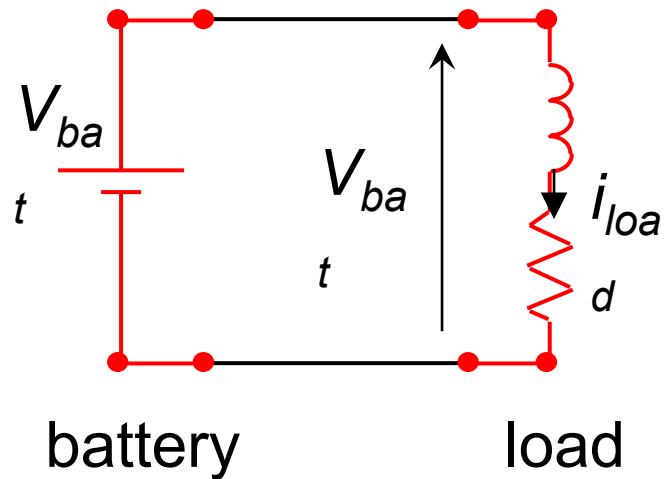
## ***Interaction principle***

Any action induces a reaction

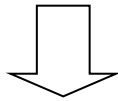


**Power** exchanged by S1 and S2 = **action x reaction**

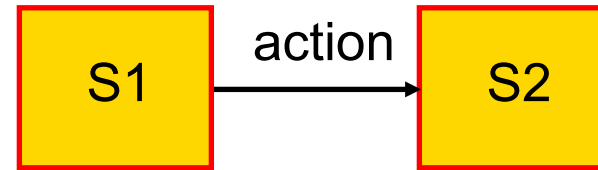
## Example: battery and load



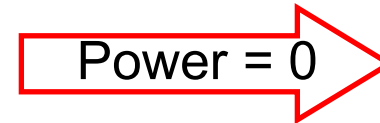
If the interaction principle is not respected for 1 subsystem



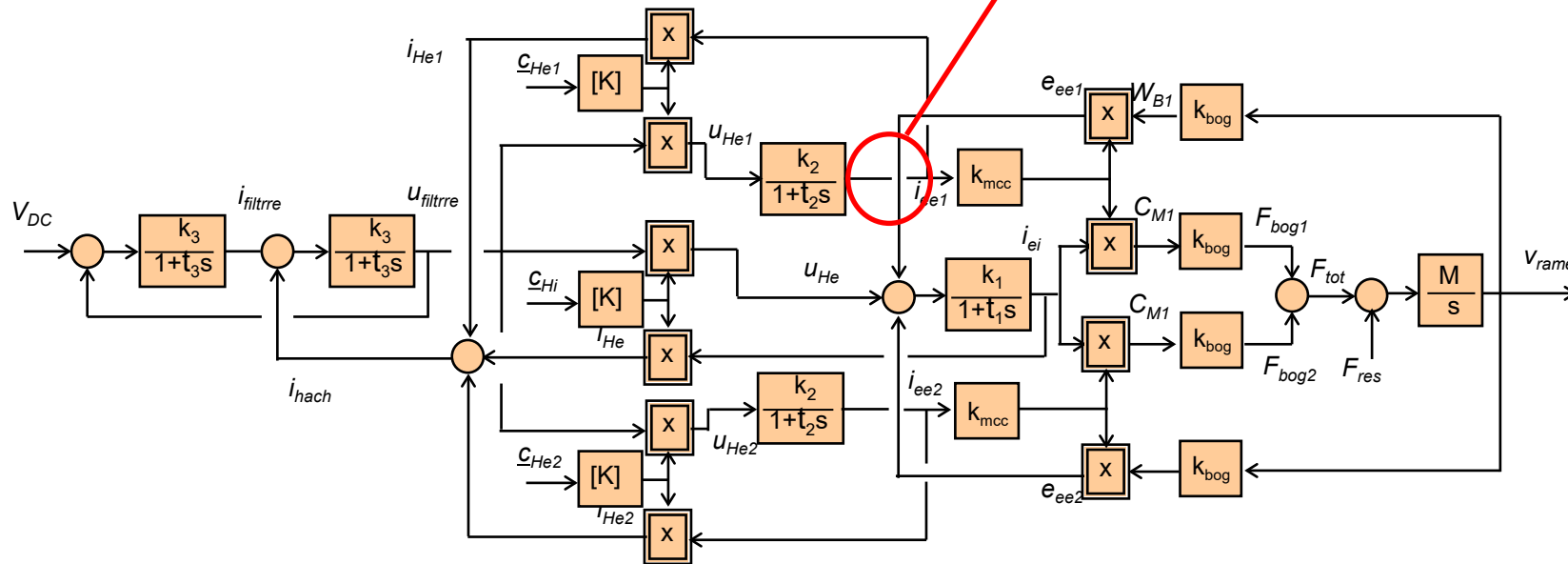
Error in the energy analysis for the whole system



(reaction = 0)



false results in terms of energy !

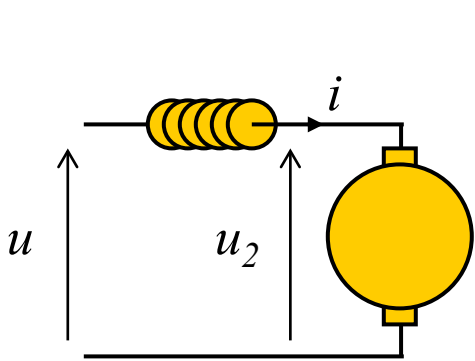


**Holistic principle**  
 Association of subsystems can lead to:

- cancelation of local properties
- emergence of new properties

$$\boxed{S1} + \boxed{S2} \neq \boxed{S1+S2}$$

Example DC machine and smoothing inductor



$$L_f \frac{di}{dt} = u - u_2 - r_f i$$

$$L_m \frac{di}{dt} = u_2 - e - r_m i$$

$$(L_f + L_m) \frac{di}{dt} = u - e - (r_f + r_m) i$$

Association of both subsystems  $\Rightarrow$  must be studied globally

$$\frac{L_f + L_m}{r_f + r_m} \neq \frac{L_f}{r_f} + \frac{L_m}{r_m}$$

Systemics vs. Cartesian approach

- A. Systemic more global
- B. Cartesian more global
- C. Equivalence

Interaction principle

- A. Action = power
- B. Reaction = power
- C. Action x Reaction = power

Structural vs. functional

- A. Structural is for design
- B. Functional is for control
- C. There is no difference

1

**Model, Representation, Simulation**

2

**Systems and Interaction**

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**Energy and Causality**

4

**Graphical descriptions**

**Energy [J]** = amount of work that can be performed by a force, an object, a system

**Power [W]** = variation of energy with time  $P(t) = \frac{dE(t)}{dt}$

**Ideal energy conversion:** energy conservation (no losses)  
and instantaneous transfer (no delay)

but

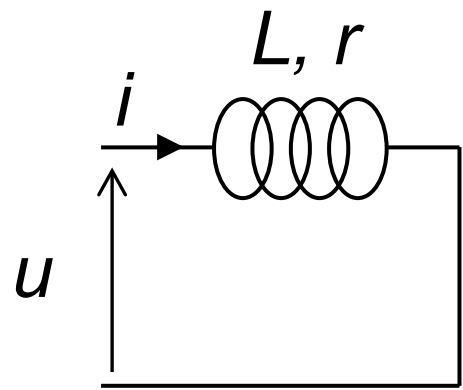
**energy dissipation:** losses, reduction of efficiency

**energy storage:** delay in energy transfer

**Energy storage in subsystems  
is key transformation for safety and efficiency**

**Energetic Variable** = state variable = variables related to energy without instantaneous changes  $\Rightarrow$  delay in energy transfer

Example inductor



$$u(t) = L \frac{di(t)}{dt} + ri(t)$$

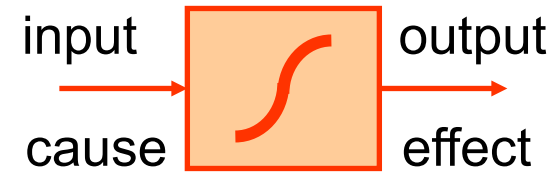
$$E(t) = \int_0^t P(t) dt = \int_0^t \left( L \frac{di(t)}{dt} i(t) + ri(t)i(t) \right) dt$$

$$E(t) = L \underbrace{\int_0^t \frac{di(t)}{dt} i(t) dt}_{\text{storage}} + r \underbrace{\int_0^t i^2(t) dt}_{\text{losses}}$$

$$E_{storage}(t) = \frac{1}{2} Li^2(t)$$

$i(t)$  energetic variable

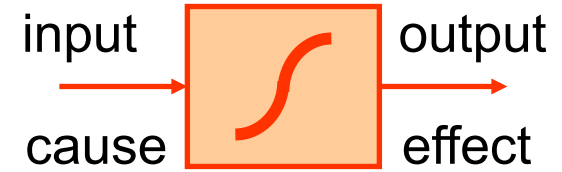
**Principle of causality**  
the effect is consequence of the cause  
i.e. output is always delayed from input  
i.e. output is an integral function of input  
i.e. output is an energy variable



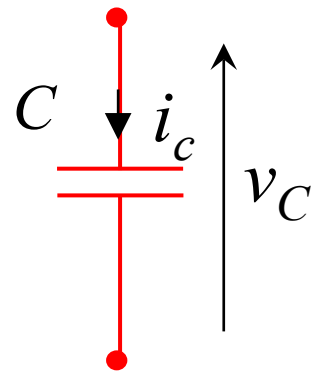
$\int x dt$   $\Rightarrow$  area  
**OK in real-time**  
knowledge of past evolution

~~slope  $\leftarrow \frac{dx}{dt}$~~   
**impossible in real-time**  
knowledge of future evolution

**Principle of causality**  
 the effect is consequence of the cause  
 i.e. output is always delayed from input  
 i.e. output is an integral function of input  
 i.e. output is a energy variable

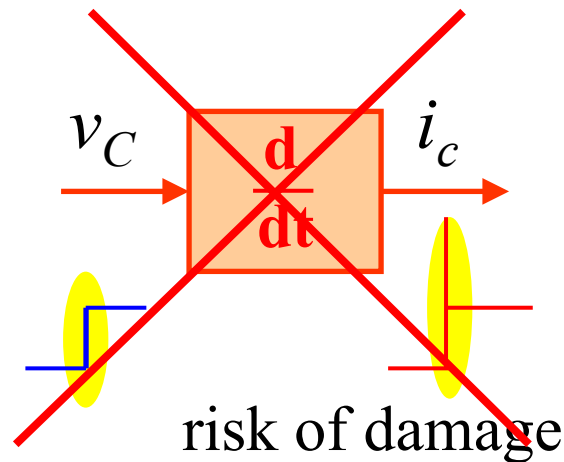
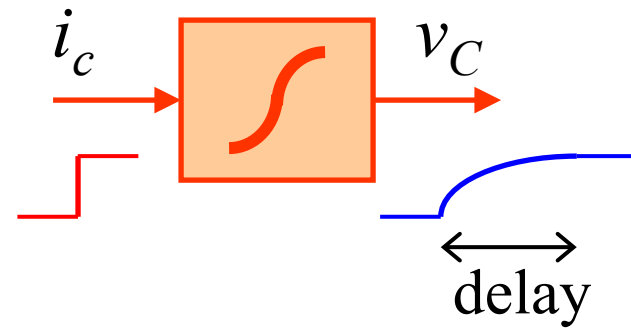


Example



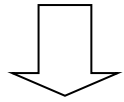
$$i_c = C \frac{d}{dt} v_c + \frac{v_c}{R}$$

$$E_c = \frac{1}{2} v_c^2$$

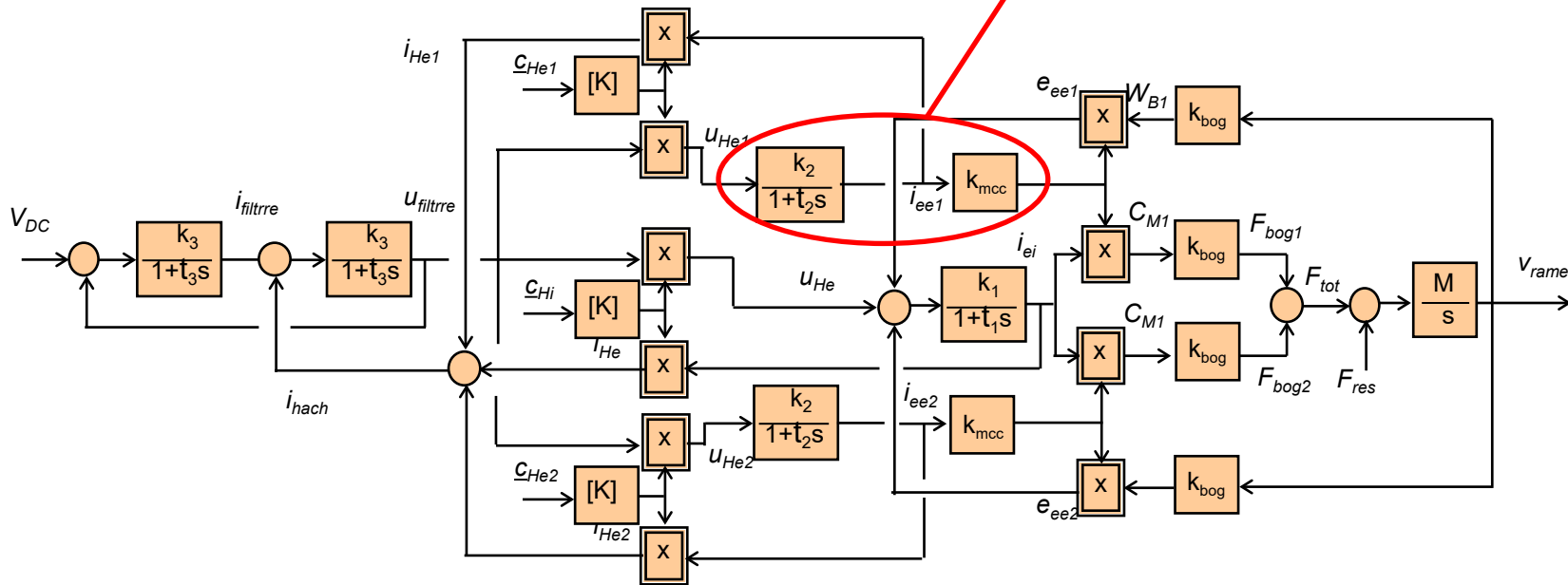
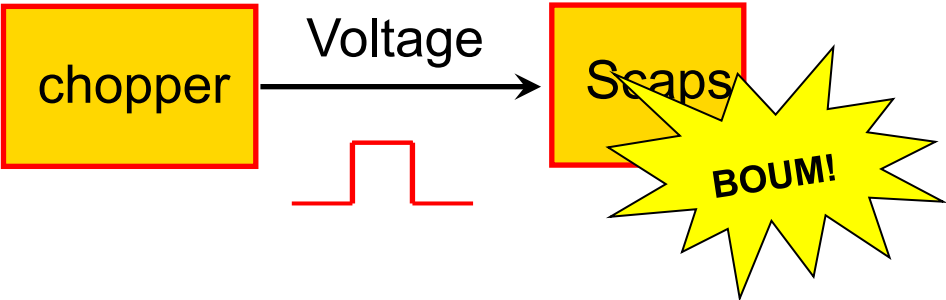


**For energy conversion systems**  
 physical causality is VITAL

If the causality principle is not respected for 1 subsystem



Risk of damage!  
No real-time management



Causality principle

- A. Output delayed from Input
- B. Input delayed from Output
- C. No delay between input/output

Causality principle

- A. Out = integral of In
- B. Out = derivative of In
- C. Out = proportional to In

Real energy conversion systems

- A. delay in energy transfer
- B. losses in energy transfer
- C. Power is energy transfer

1

**Model, Representation, Simulation**

2

**Systems and Interaction**

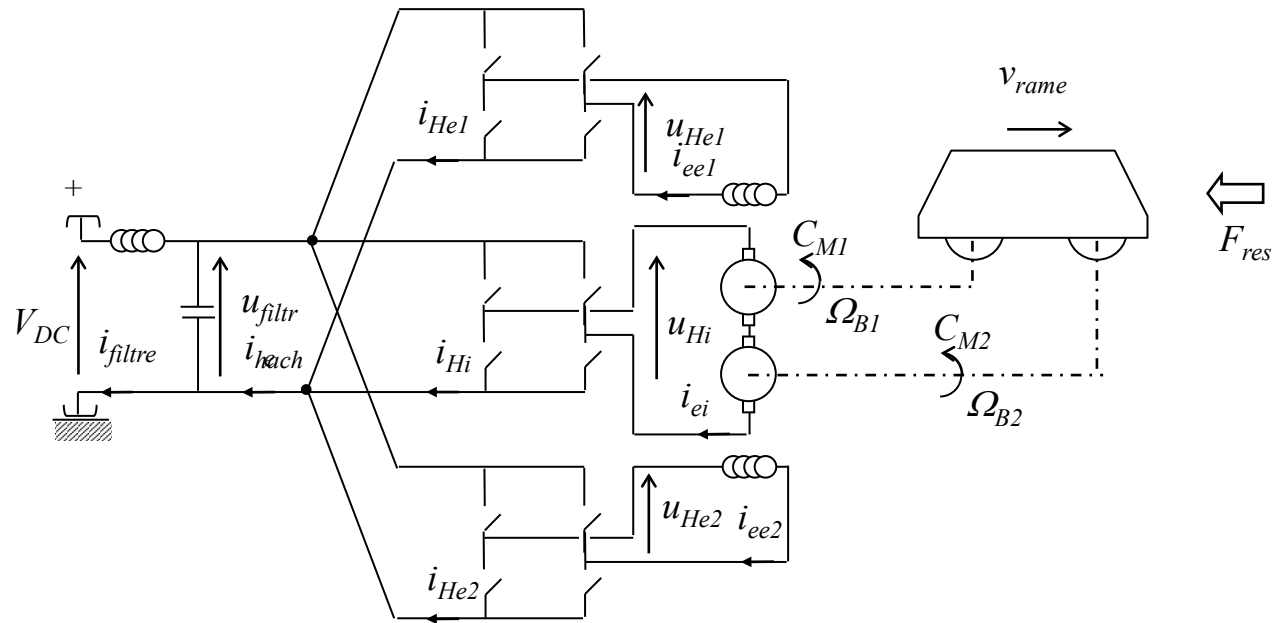
3

**Energy and Causality**

4

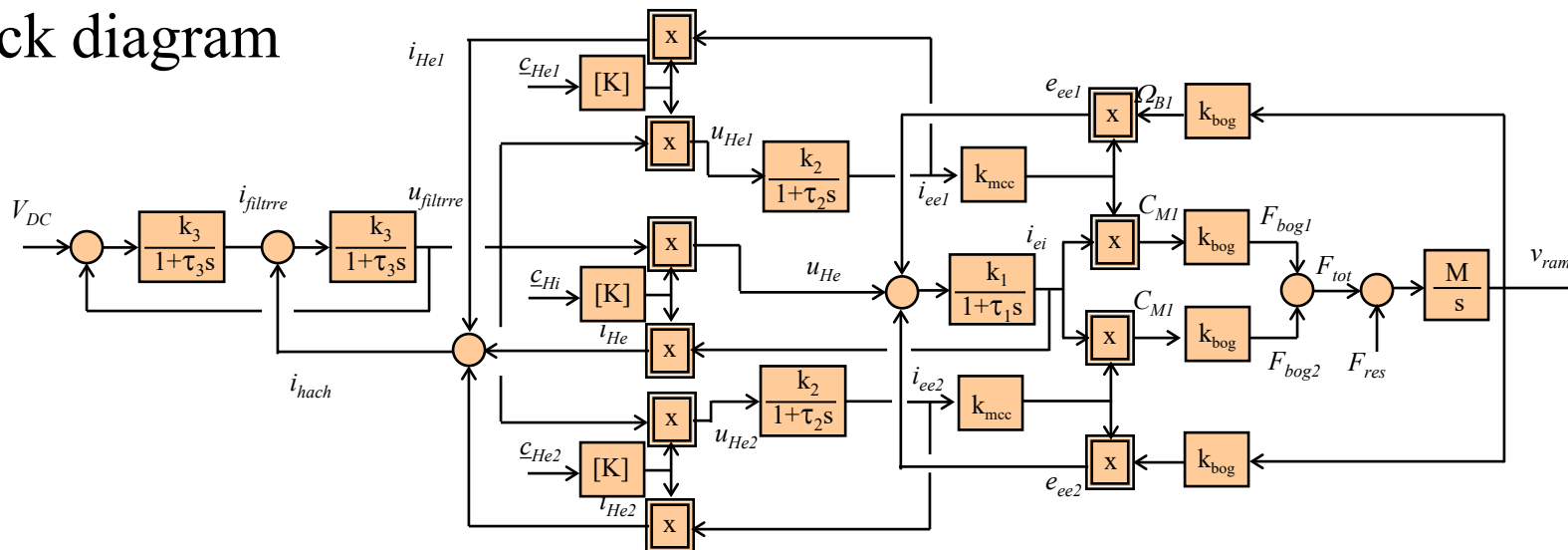
**Graphical descriptions**

Example  
 Subway traction system  
 of VAL 206  
 (subway of Lille)



SIEMENS

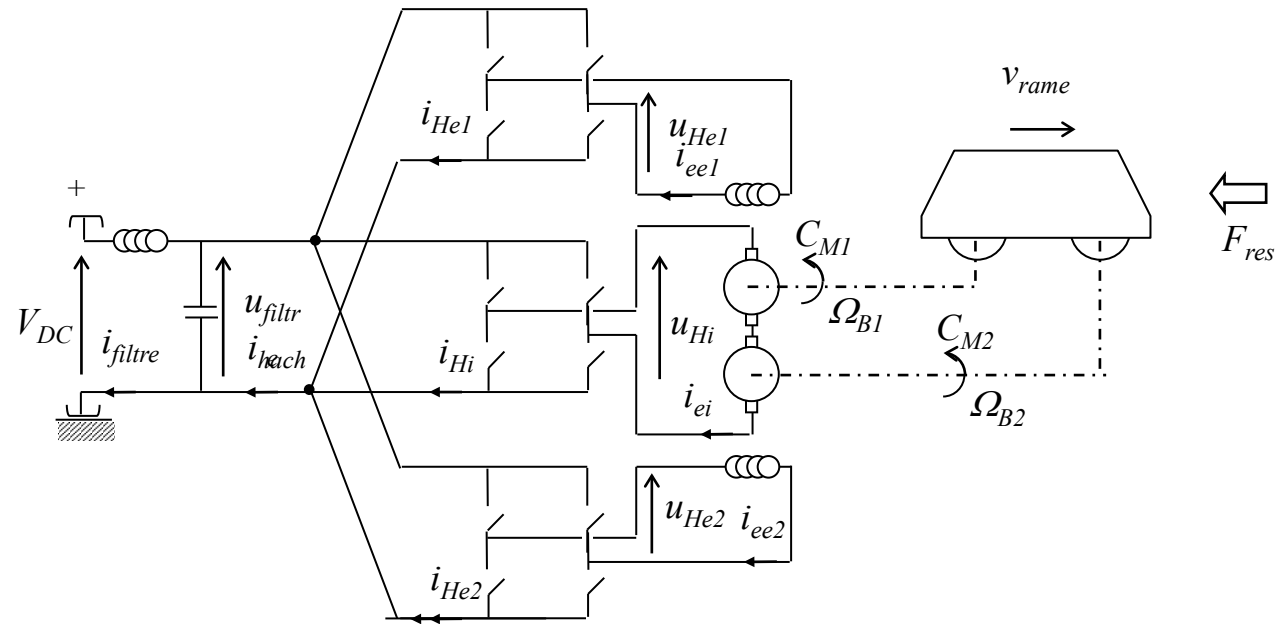
Simplified block diagram



causality?  
 action/reaction?

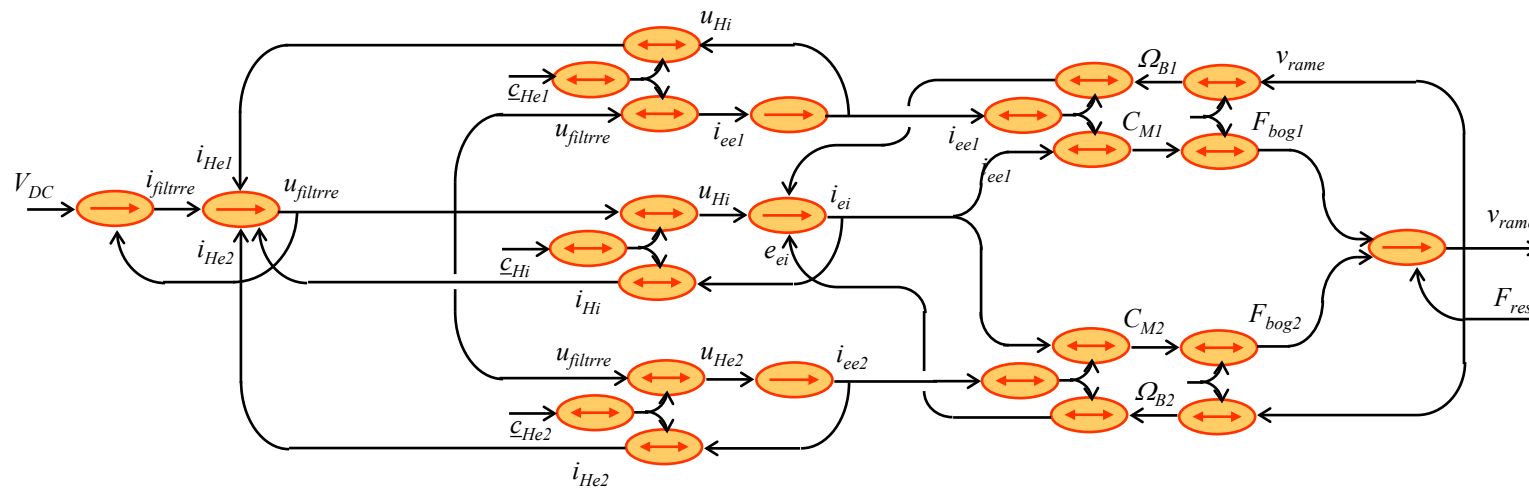
Example

Subway traction system of VAL 206



## Causal Ordering Graph (COG)

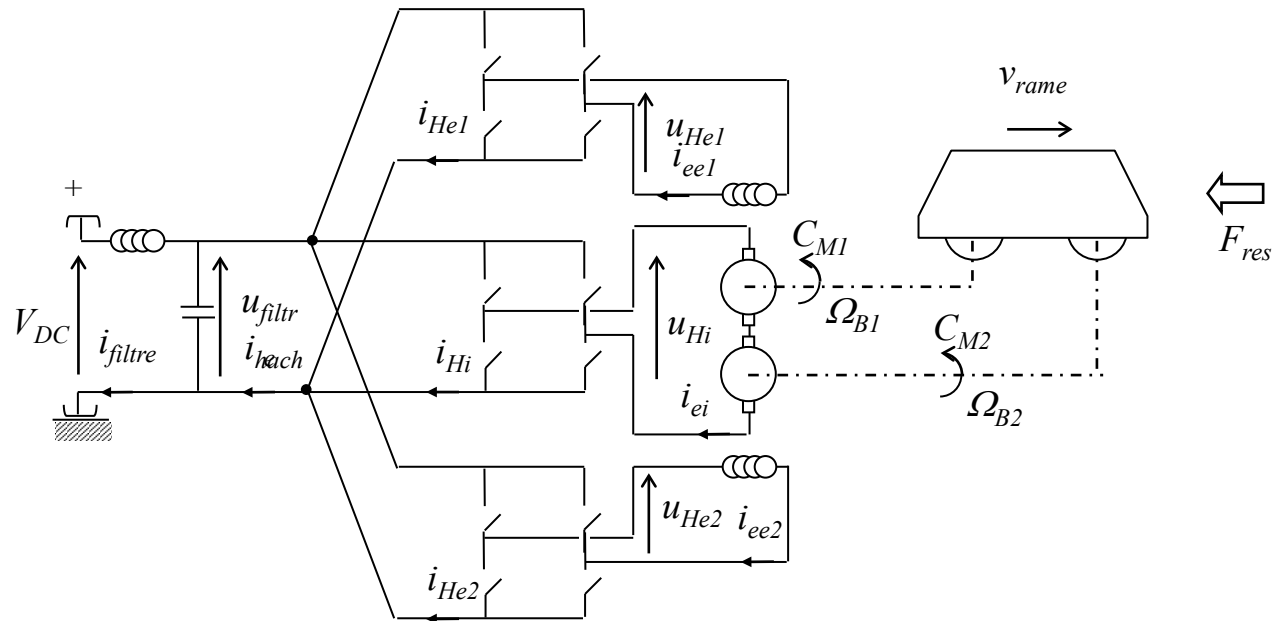
[Hautier 14]



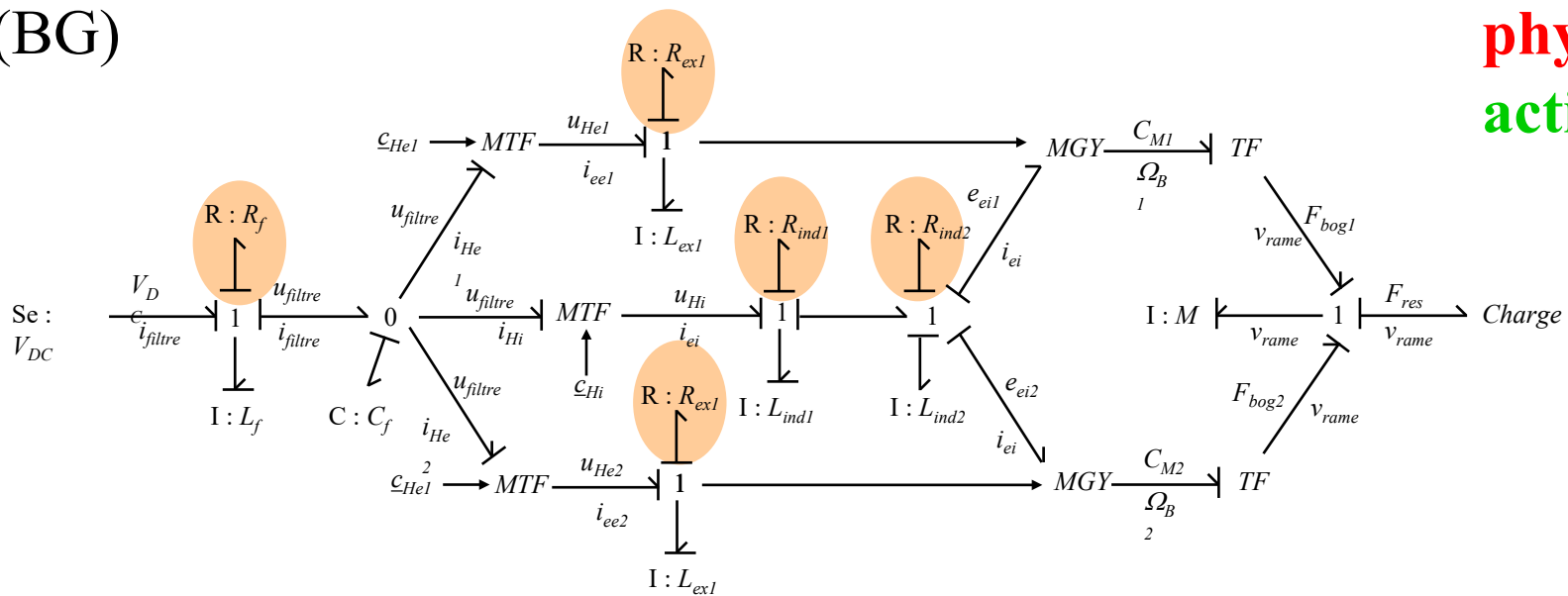
**causality OK**  
**action/reaction?**

Example

Subway traction system of VAL 206

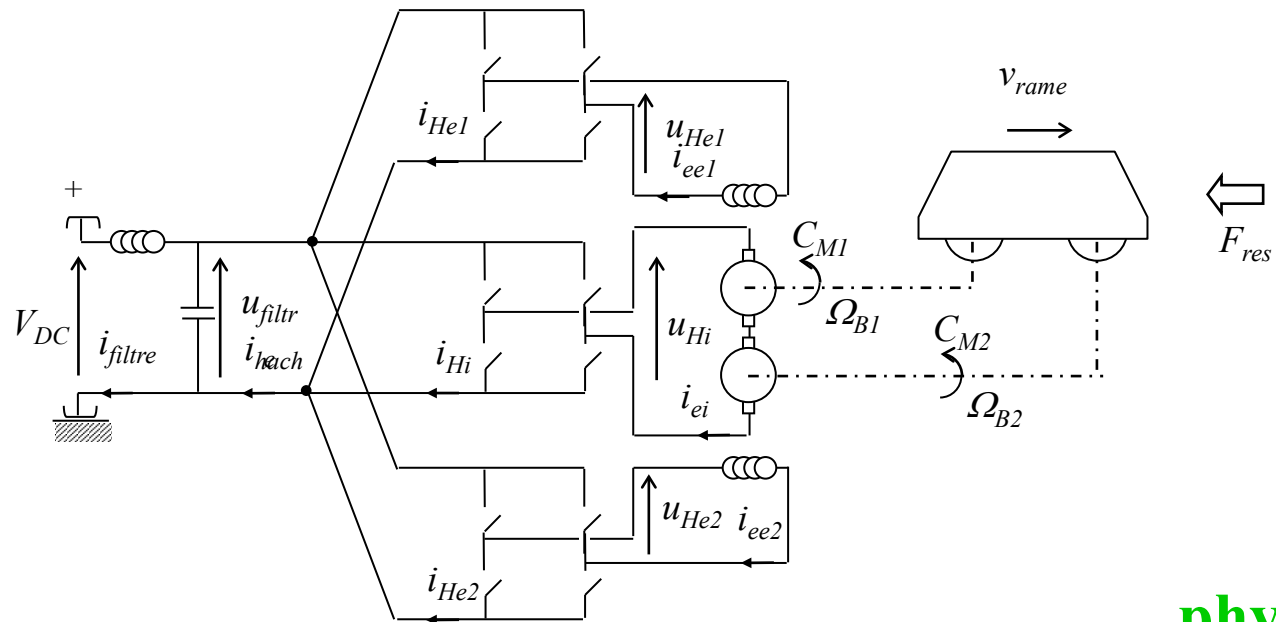


Bond Graph (BG)  
[Paynter 61]

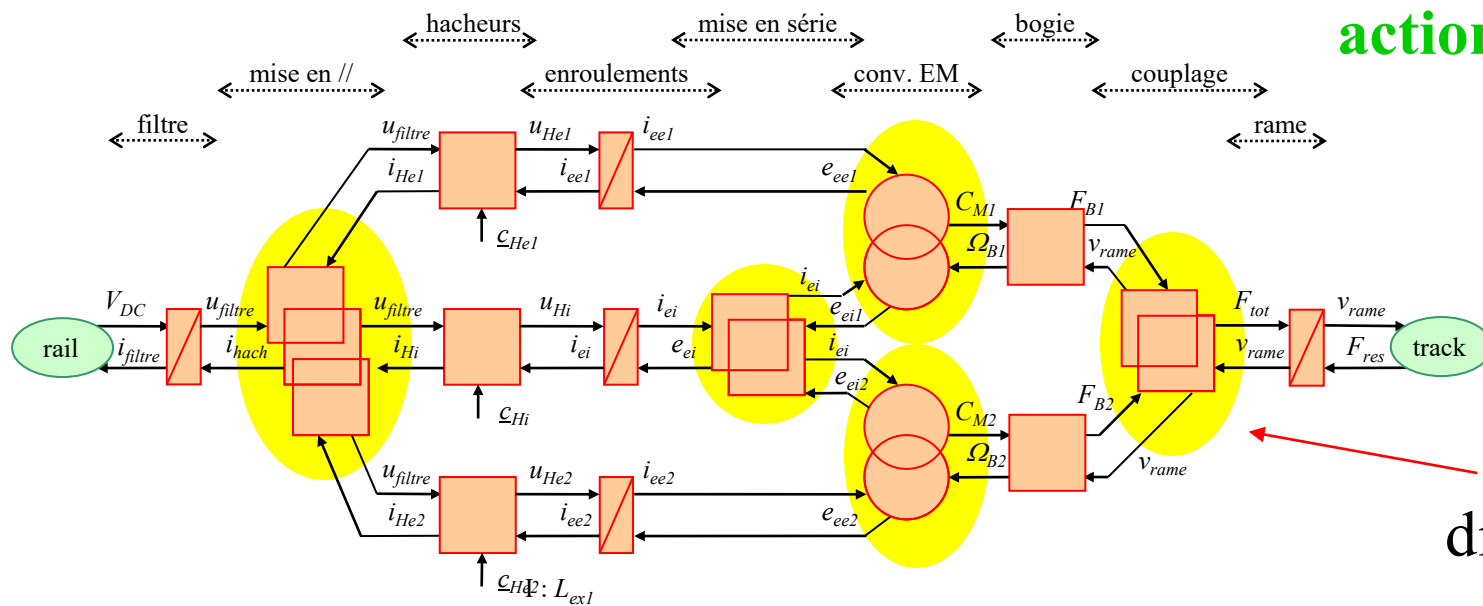


**physical causality?**  
**action/reaction OK**

Example  
Subway traction system  
of VAL 206



Energetic  
Macroscopic  
Representation  
(EMR)  
[Bouscayrol 12]



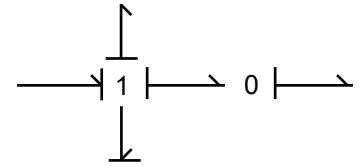
physical causality **OK**  
action/reaction **OK**

energy  
distribution

## Energy & System

- Energetic Puzzles (Laplace, France)
- Bond Graph** (USA, The Netherlands...)
- Power Oriented Graph (Italy)
- Signal Flow Diagram (Germany, Japan...)

*Structural description for analysis and design*



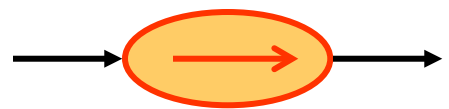
⇒ mathematical model



global controls

- Block diagrams**
- COG** (L2EP-LEEI, France)
- EMR** (L2EP, France)

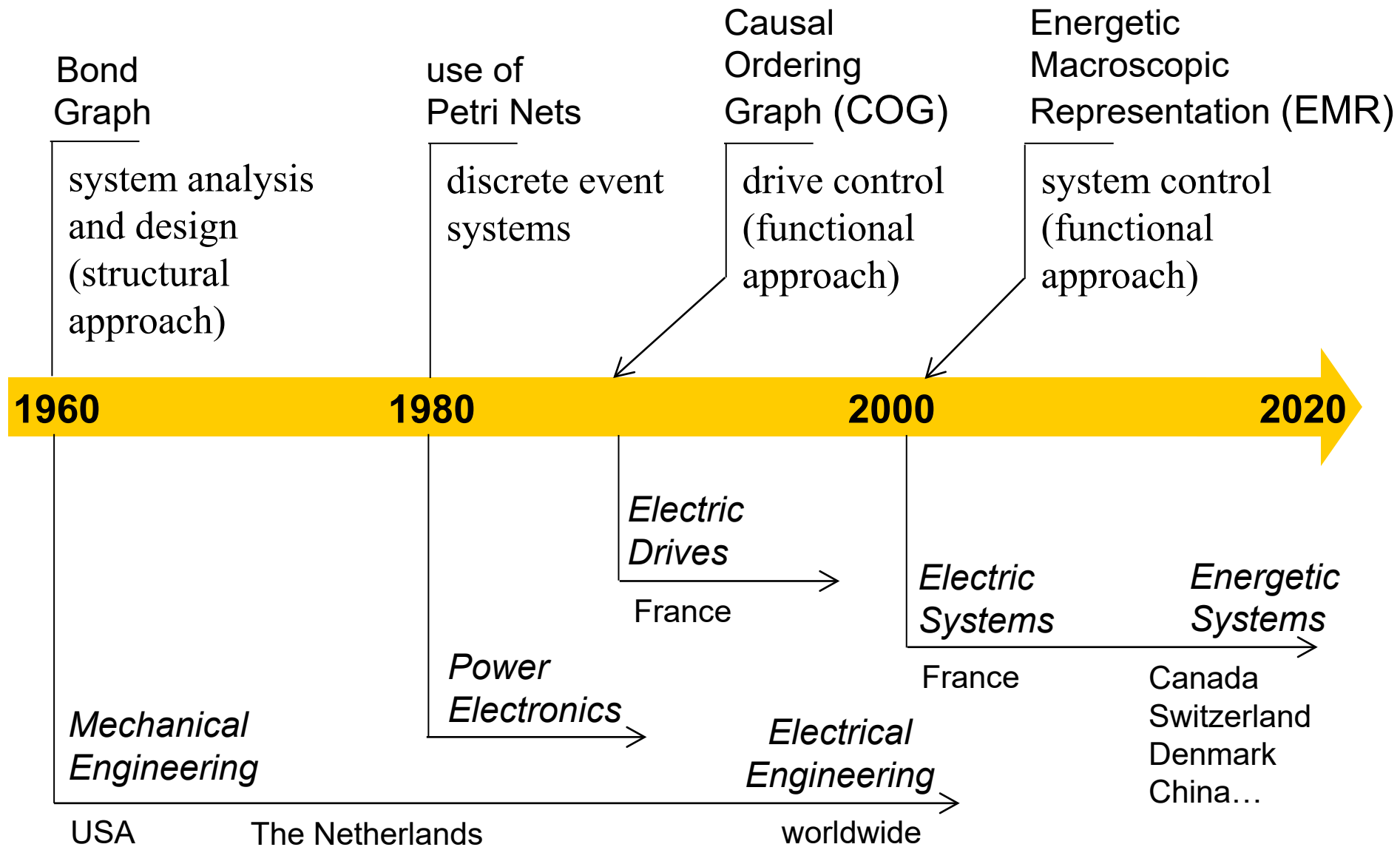
*functional descriptions for simulation and control*



⇒ Inversion graphs



cascaded control



Multi-physical system



Systemic approach

Energy management



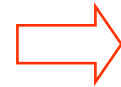
Energetic approach  
Causal representation

System control



Functional description

Real-time control



Dynamical modeling  
Causal representation

Moreover a graphical description could be a valuable intermediary step for such complex systems



**Conclusion**

**system = subsystems in interaction**

best performances require an systemic approach

**energy = respect of the physical causality**

energy management requires a causal approach

**control = inversion of a causal model of the system**

in order to respect its energy properties

**graphical description = model organization**

useful intermediary step

Remember, follow  
a disciplined procedure!



*Prof. C.C. Chan*

[Astier 2012] S. Astier, A. Bouscayrol, X. Roboam, "Introduction to Systemic Design", Systemic Design Methodologies for Electrical Energy, tome 1, Analysis, Synthesis and Management, Chapter 1, ISTE Willey editions, October 2012, ISBN: 9781848213883

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[Bouscayrol 2012] A. Bouscayrol, J. P. Hautier, B. Lemaire-Semail, "Graphic Formalisms for the Control of Multi-Physical Energetic Systems", Systemic Design Methodologies for Electrical Energy, tome 1, Analysis, Synthesis and Management, Chapter 3, ISTE Willey editions, October 2012, ISBN: 9781848213883.

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[Paynter 1961] H. Paynter, "Analysis and design of engineering systems", *MIT Press*, 1961.



Thanks for your attention!

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