

# INVERSION-BASED CONTROL DEDUCED FROM EMR

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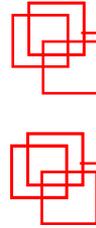
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- 1. Principle of model-based control**
- 2. Inversion of EMR elements**
- 3. Inversion-based control schemes**



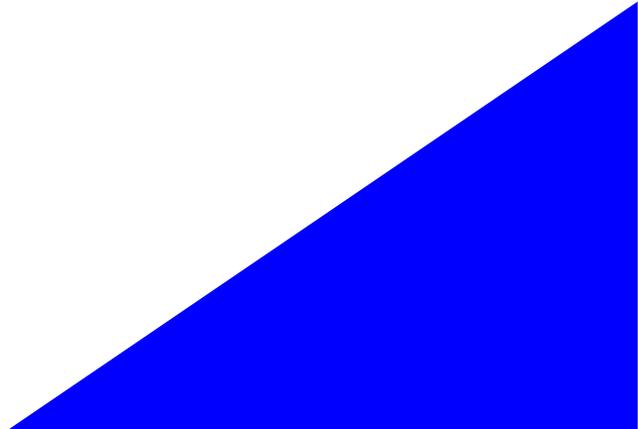
**EMR'22**  
**Sion**  
**June 2022**



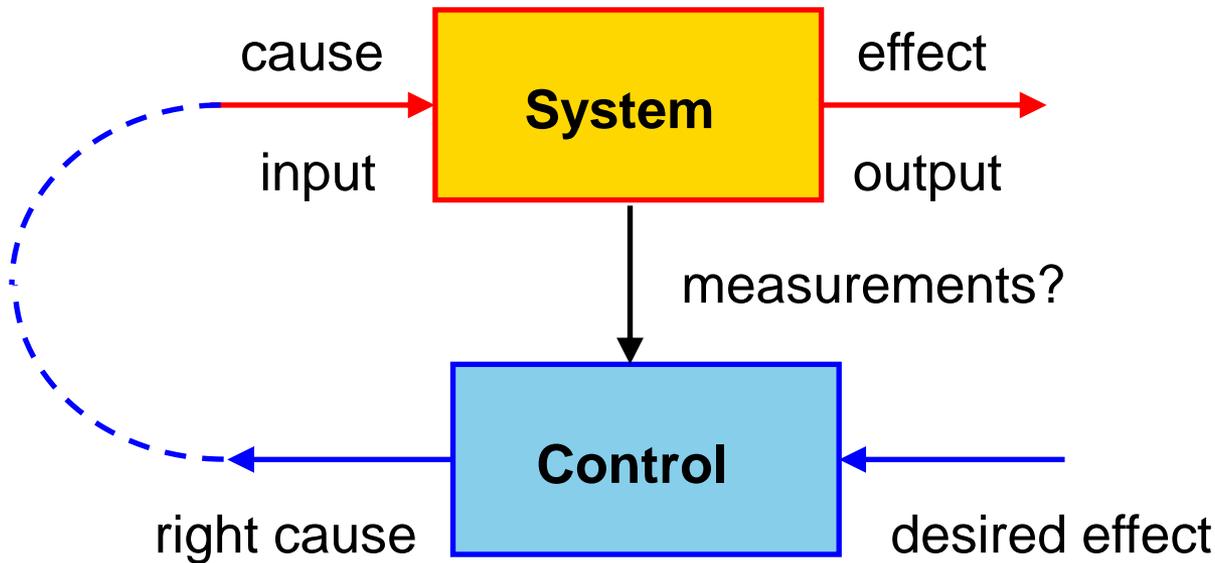
**EMR'22 Summer School**  
**“Energetic Macroscopic Representation”**



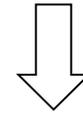
# **1. Principle of model-based control**



[Hautier 96]



Model  $out = f(in)$



Control  $in = g(out_{ref})$

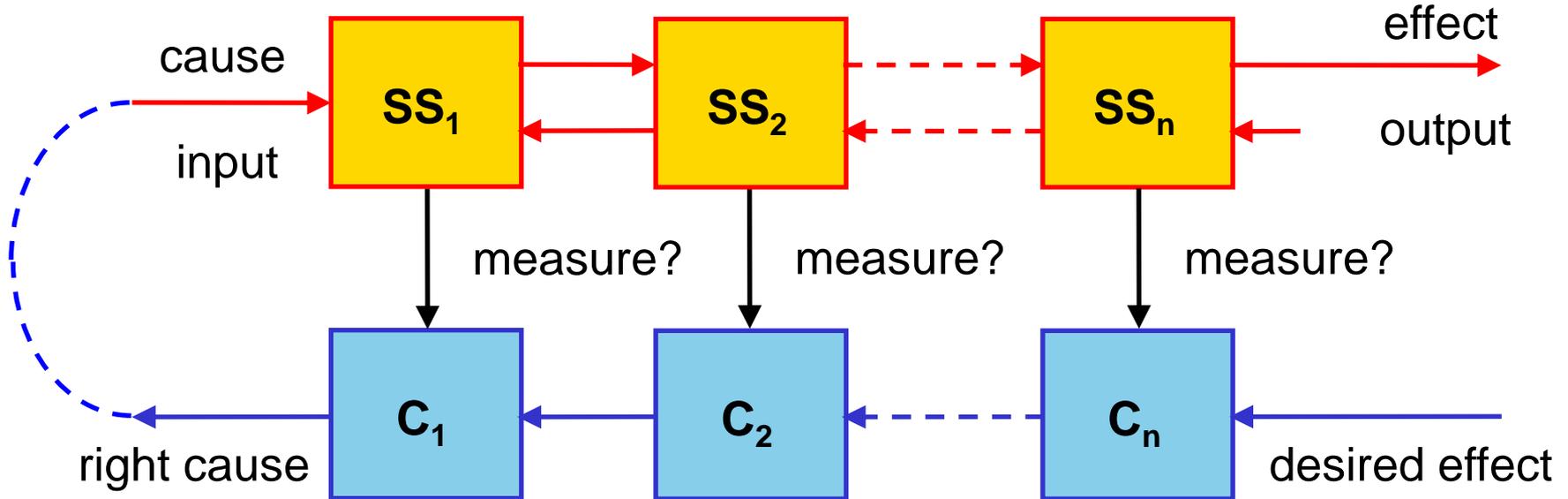
**control = inversion of the system functionality**

# Inversion-Based Control from EMR

## - EMR and Inversion-based methodology -

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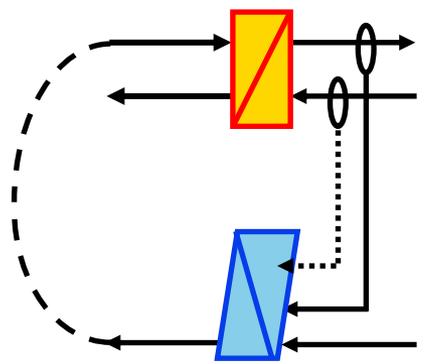
**EMR** = system decomposition in basic energetic subsystems ( $SS_n$ )



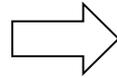
Remember,  
divide and conquer!

**Inversion-based control:** systematic inversion  
of each subsystem

## 2. Inversion of EMR elements

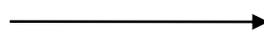


Model  $out = f(in)$



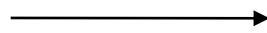
Control  $in = g(out_{ref})$

I/O relation without delay



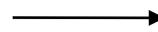
direct inversion

I/O relation with delay



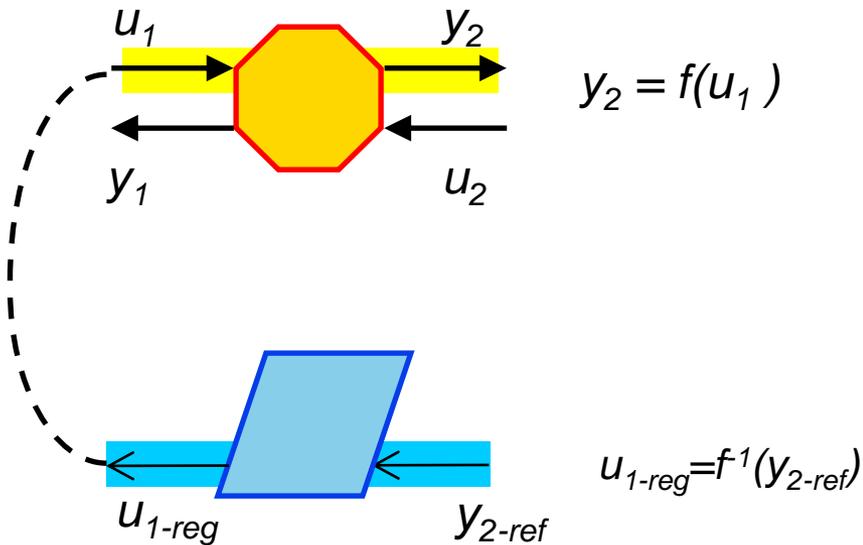
Indirect inversion  
(closed-loop control)

I/O relation with multiple Inputs



Multiple solutions

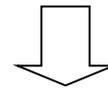
Objective: to control  $y_2$



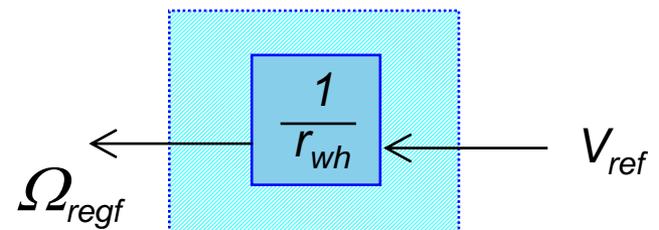
Direct Inversion

Ex : wheel

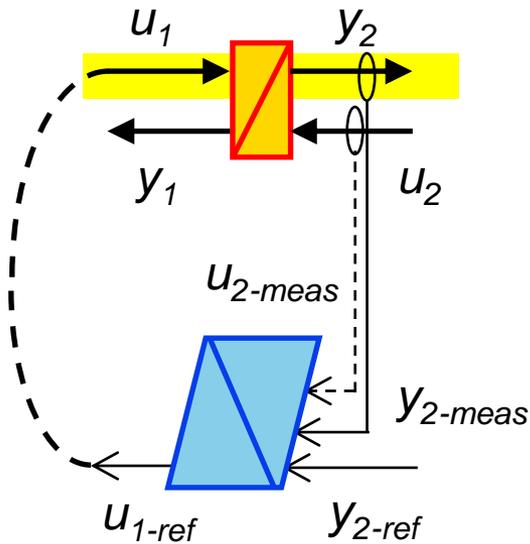
$$\begin{cases} V = r_{wh} \Omega \\ T = r_{wh} F \end{cases}$$



$$\Omega_{ref} = V_{ref} / r_{wh}$$



**Objective: to control  $y_2$**



$$y_2 = f(u_1, u_2)$$

$f$  is in integral form

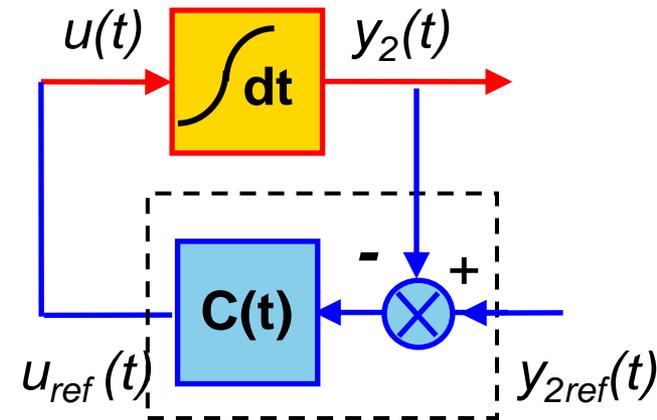
direct inversion

indirect inversion

**not possible  
in real-time**

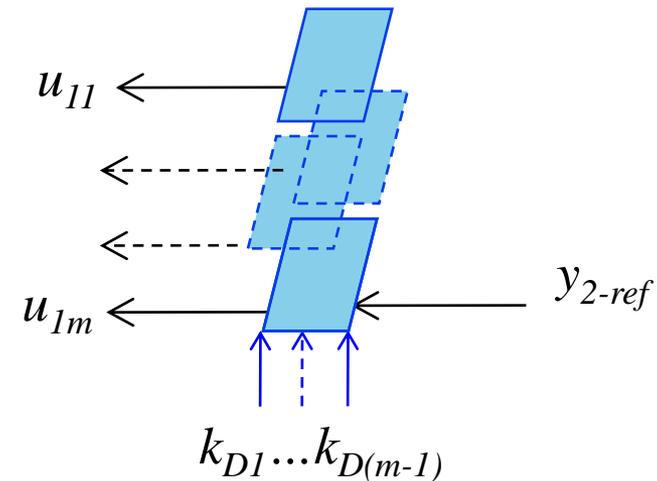
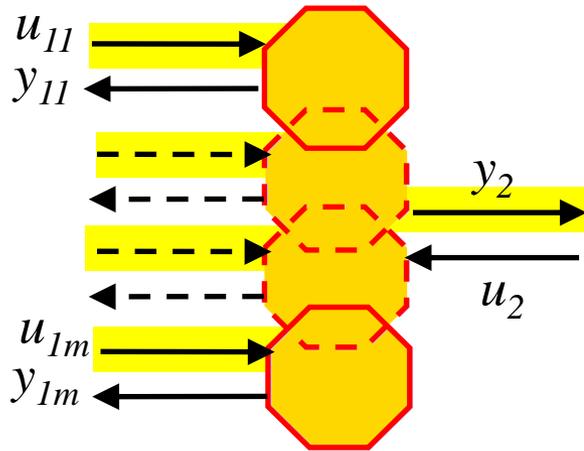
$$u_{ref}(t) = \frac{d}{dt} y_{ref}(t)$$

$$u(t) = u_1(t) - u_2(t)$$



$$u_{ref}(t) = C(t)[y_{2ref}(t) - y_{2meas}(t)]$$

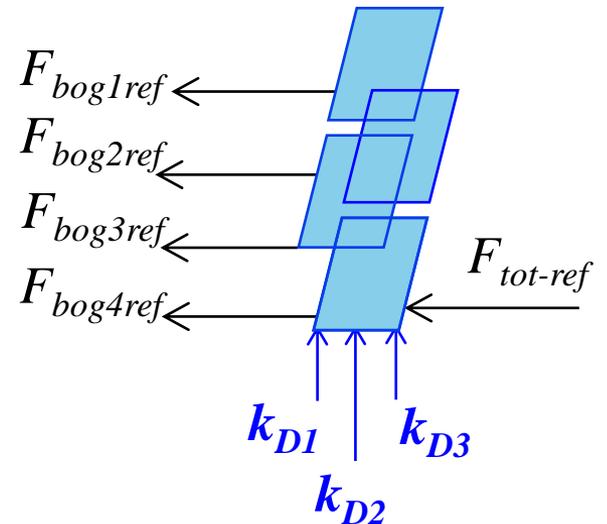
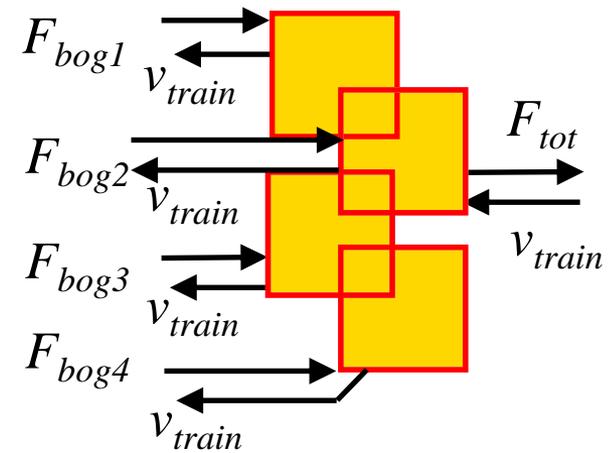
**closed loop controller**



no measurement  
no controller  
( $m - 1$ ) **distribution variables**

$$\left\{ \begin{array}{l} u_{11} = k_{D1} y_{2ref} \\ \dots \\ u_{1(m-1)} = k_{D(m-1)} y_{2ref} \\ u_{1m} = (1 - \sum k_{Di}) y_{2ref} \end{array} \right.$$

*Example: chassis of a train*



# Inversion-Based Control from EMR

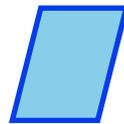
## - Inversion of EMR elements -

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### Legend

Control = light blue  
Parallelograms  
with dark blue  
contour

 direct  
inversion

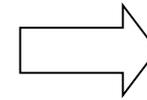
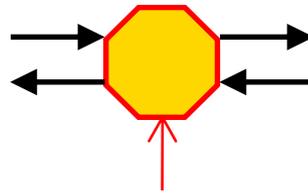
 indirect  
inversion

 sensor

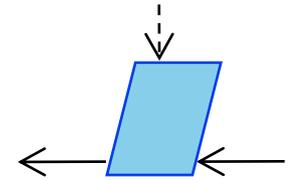
 mandatory link

 facultative link

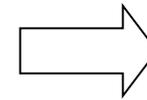
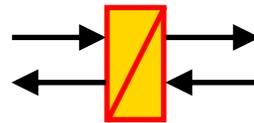
conversion element



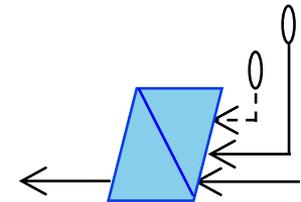
direct inversion +  
disturbance rejection



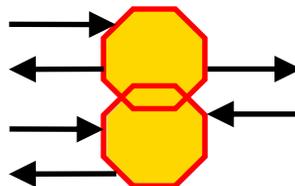
accumulation element



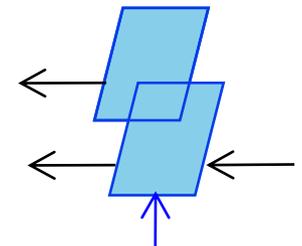
controller +  
disturbance rejection



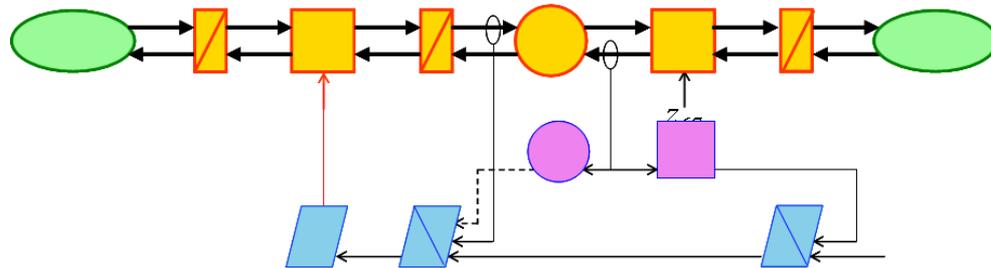
coupling element



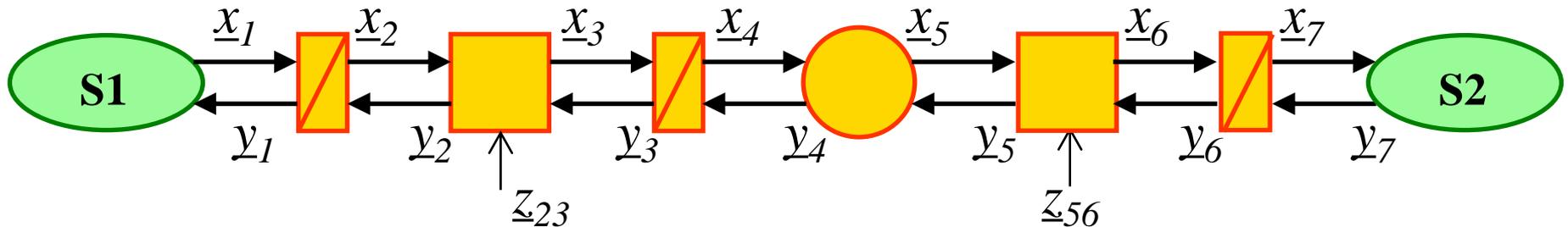
distribution criteria



### 3. Inversion-based control schemes



### 1. EMR of the system



### EMR depends on:

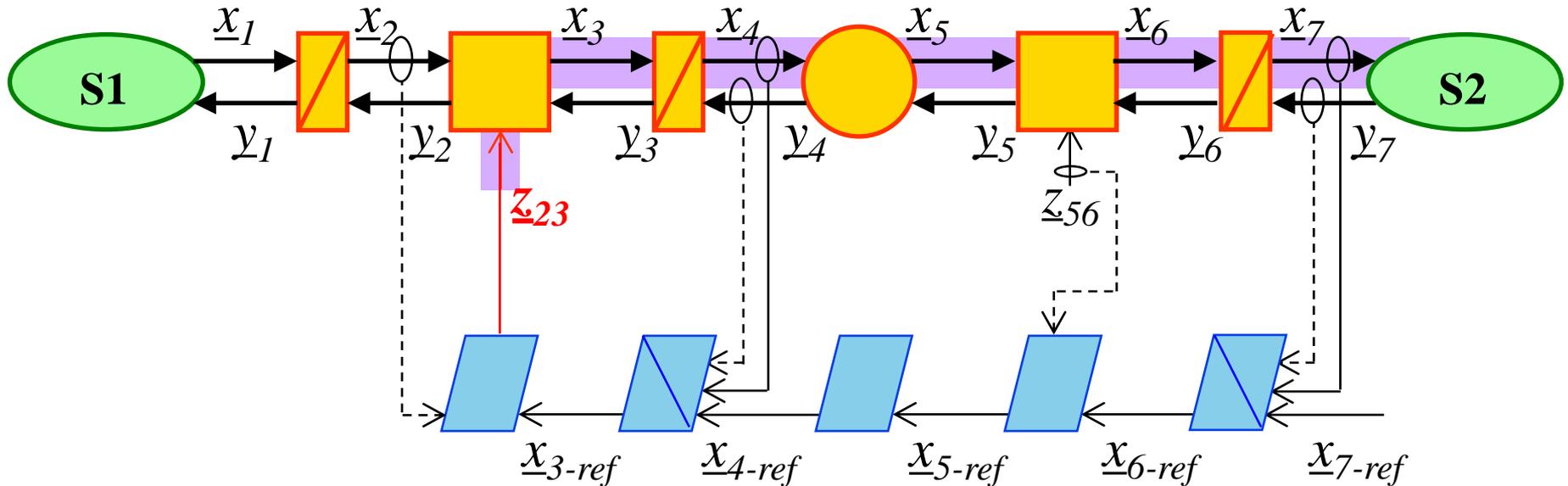
- the study objective (limits between system and sources)
- the physical laws of subsystems (physical causality)
- the association of subsystems (systemic approach)



1. EMR of the system

2. Tuning path

3. Inversion step-by-step **Strong assumption: all variables can be measured!**



**Maximal Control Structure** (or scheme):

- maximum of sensors
- maximum of operations

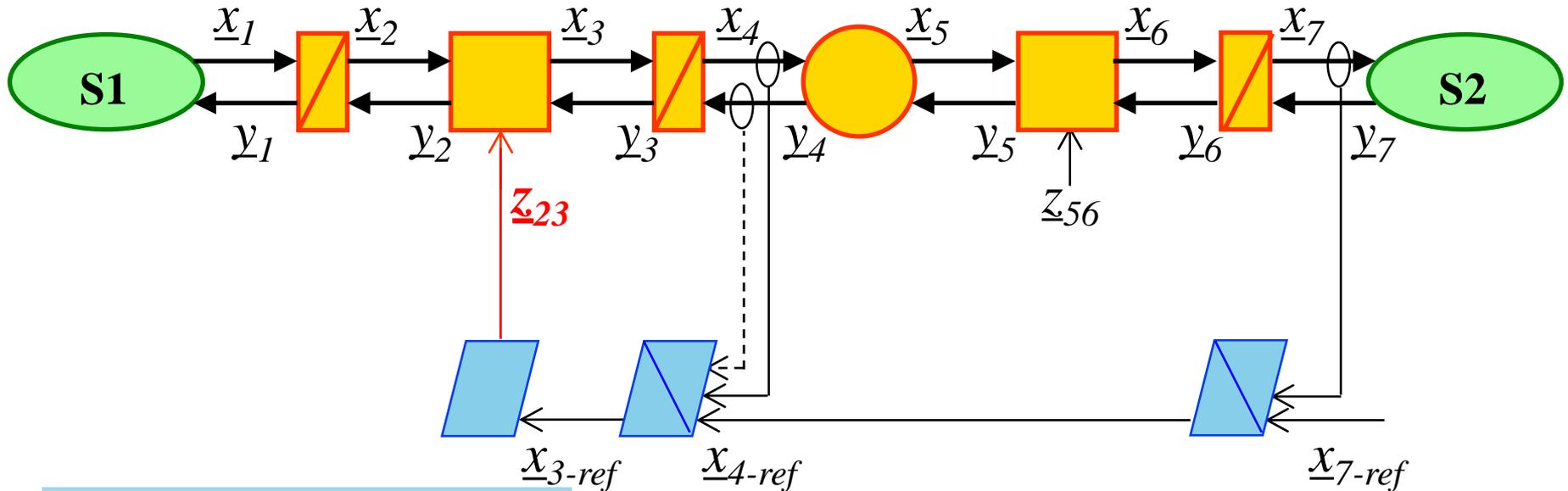
Example:

- 5 sensors
- 2 closed-loop controllers

1. EMR of the system

2. Tuning path

3. Inversion step-by-step **Strong assumption: all variables can be measured!**



4. Simplification of control

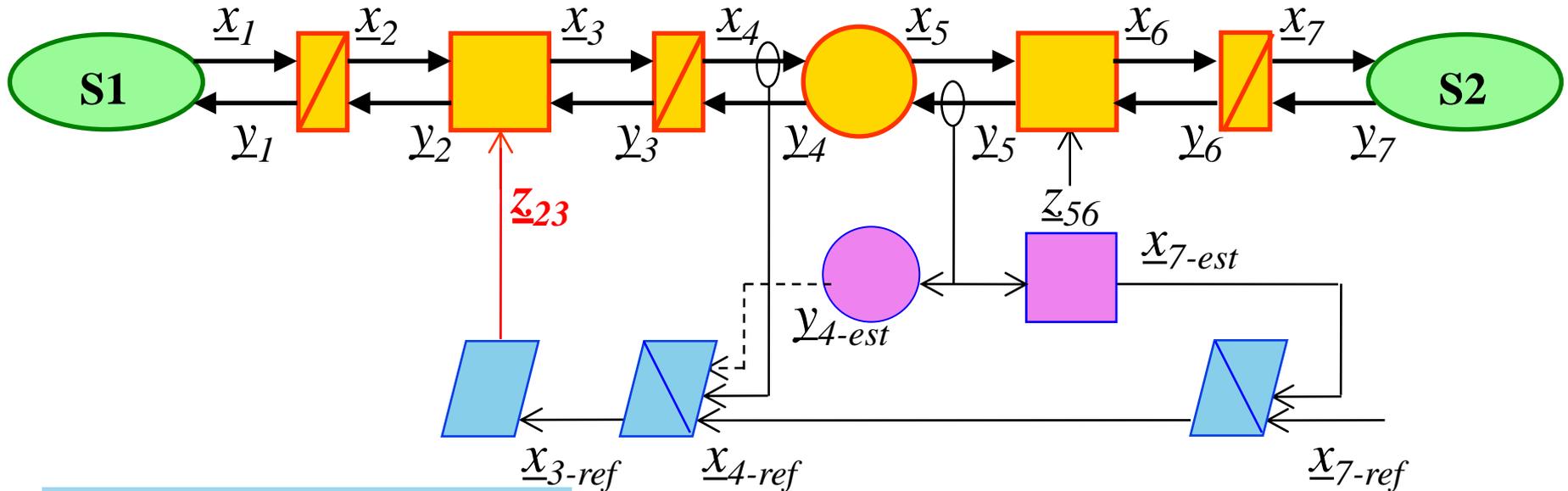
**Simplifications:**

- non-consideration of disturbances  $\Rightarrow$  impact on the tuning and on the performances
- merging control blocks...

1. EMR of the system

2. Tuning path

3. Inversion step-by-step **Strong assumption: all variables can be measured!**



4. Simplification of control

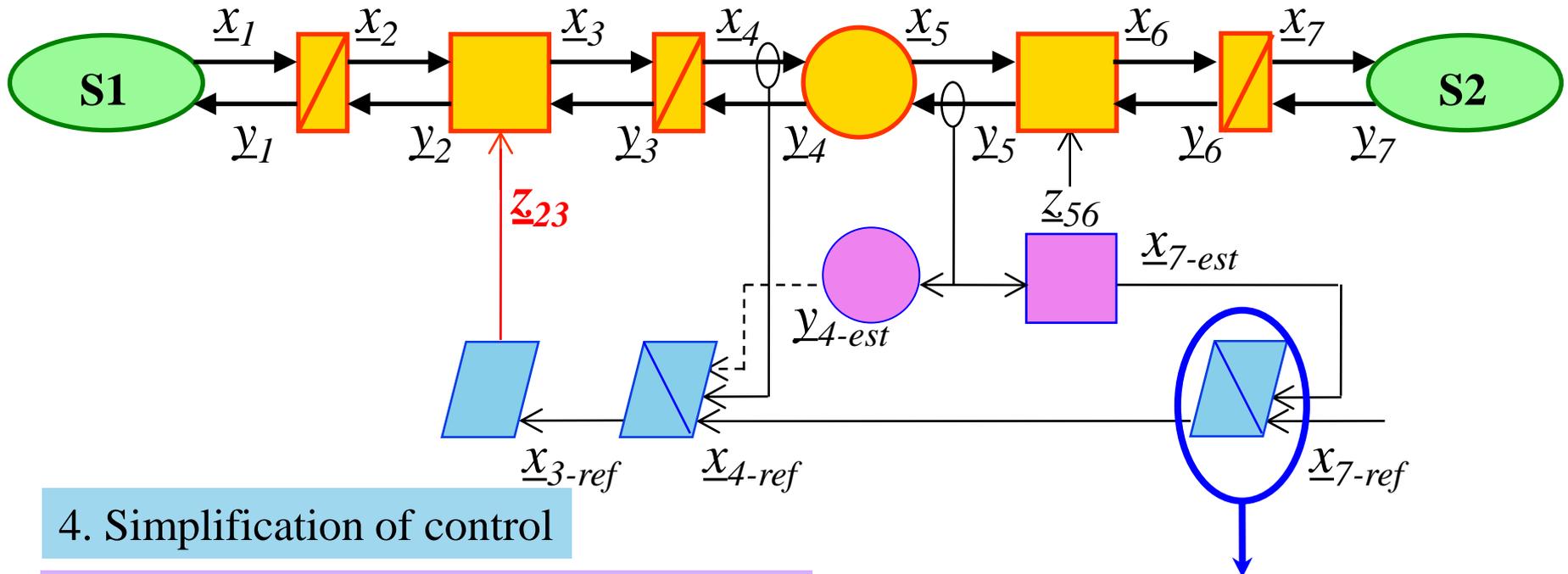
5. Estimation of non-measured variables

from measured variables

1. EMR of the system

2. Tuning path

3. Inversion step-by-step **Strong assumption: all variables can be measured!**



4. Simplification of control

5. Estimation of non-measured variables

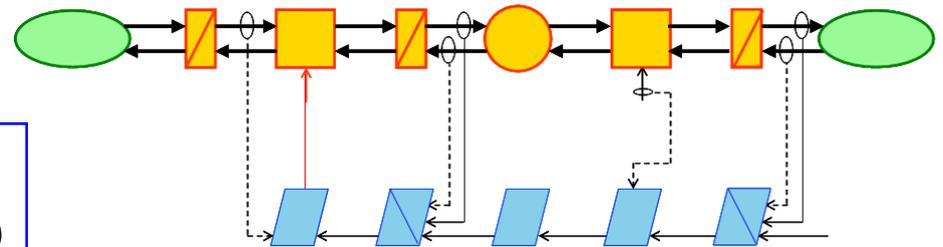
6. Tuning of controllers

PI / PID / fuzzy controller?  
Calculation of parameters?

1. EMR of the system
2. Tuning path
3. Inversion step-by-step

### Maximal Control Scheme

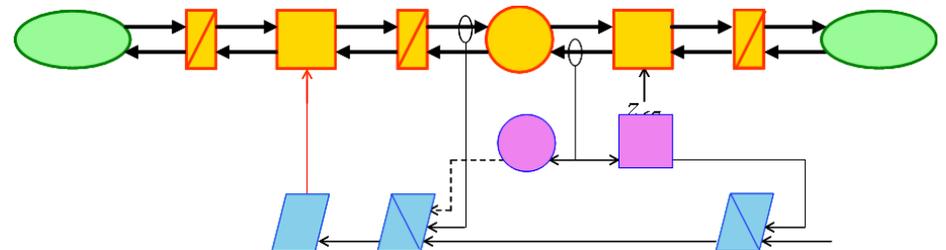
- mirror of the EMR (systematic)
- unique and theoretical solution



4. Simplification of control
5. Estimation of variables
6. Tuning of controllers

### Practical Control Schemes

- several solutions (expertise)
- reduced performances





## Conclusion

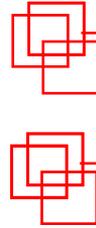
**Inversion based control = inversion of EMR**  
based on the cognitive systemic  
and the causality principle (energy)

### **Inversion rule for control scheme**

closed-loop control to invert accumulation, direct inversion for  
conversion element, degrees of freedom for coupling element



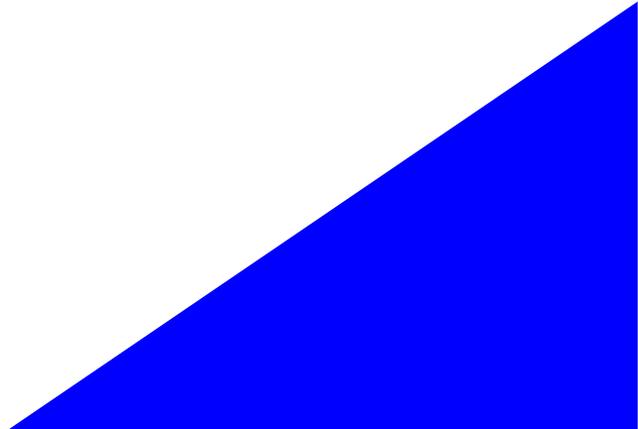
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# **BIOGRAPHIES AND REFERENCES**



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