

# INVERSION-BASED CONTROL DEDUCED FROM EMR

Alain BOUSCAYROL<sup>1</sup>, Pierre SICARD<sup>2</sup>

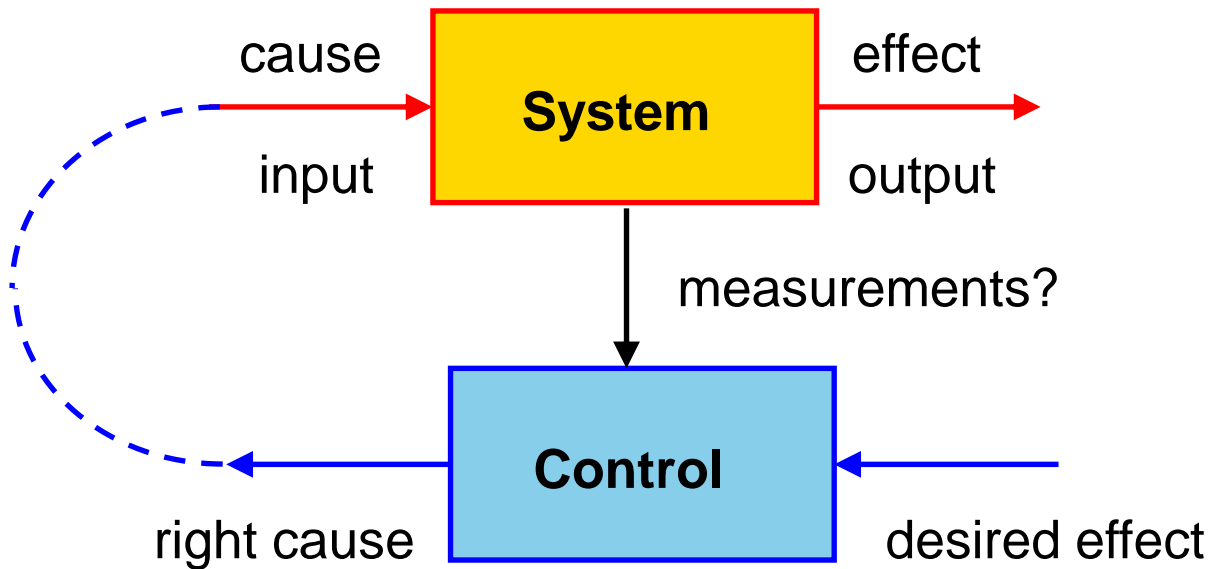
<sup>1</sup> L2EP, University of Lille, France

<sup>2</sup> Université du Québec à Trois Rivières, Canada

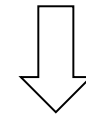
- 1. Principle of model-based control**
- 2. Inversion of EMR elements**
- 3. Inversion-based control schemes**

# **1. Principle of model-based control**

[Hautier 96]



Model  $out = f(in)$



Control  $in = g(out_{ref})$

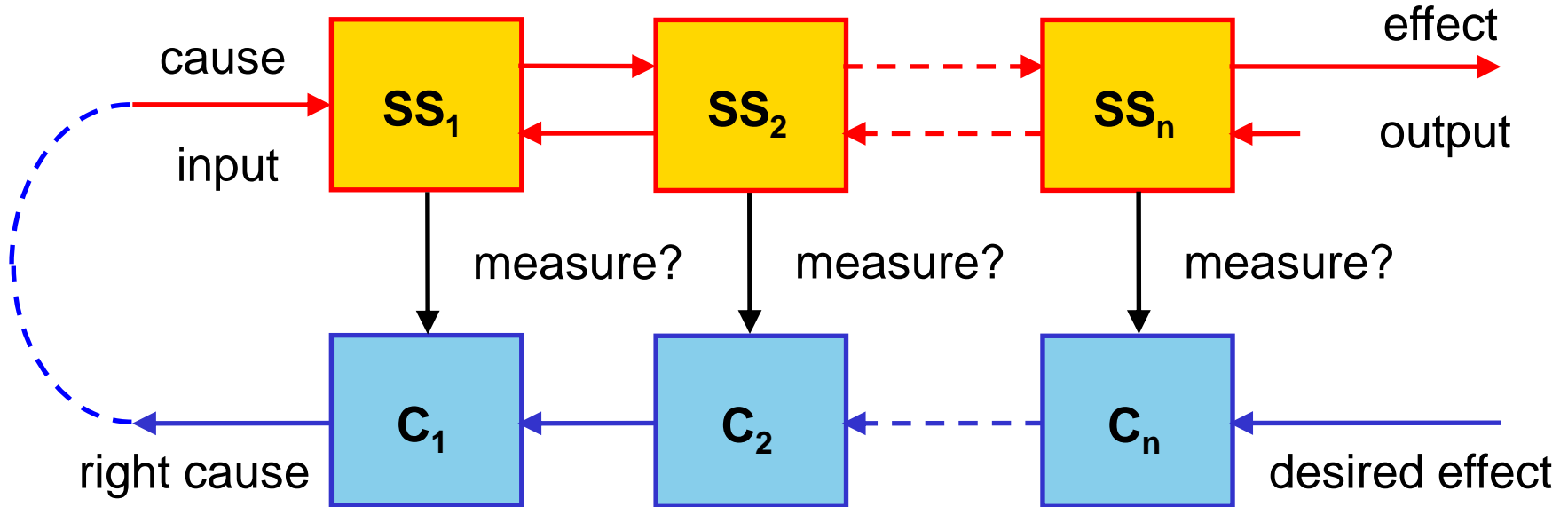
**control = inversion of the system functionality**

# Inversion-Based Control from EMR

## - EMR and Inversion-based methodology -

EMR'22, Sion, June 2022

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**EMR** = system decomposition in basic energetic subsystems ( $SS_n$ )

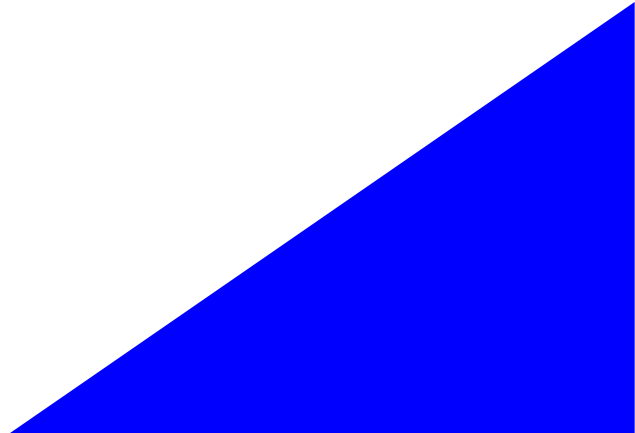
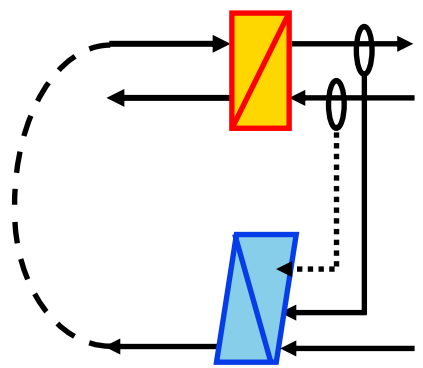


Remember,  
divide and conquer!

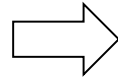
**Inversion-based control:** systematic inversion  
of each subsystem



## 2. Inversion of EMR elements

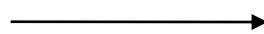


Model  $out = f(in)$



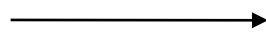
Control  $in = g(out_{ref})$

I/O relation without delay



direct inversion

I/O relation with delay



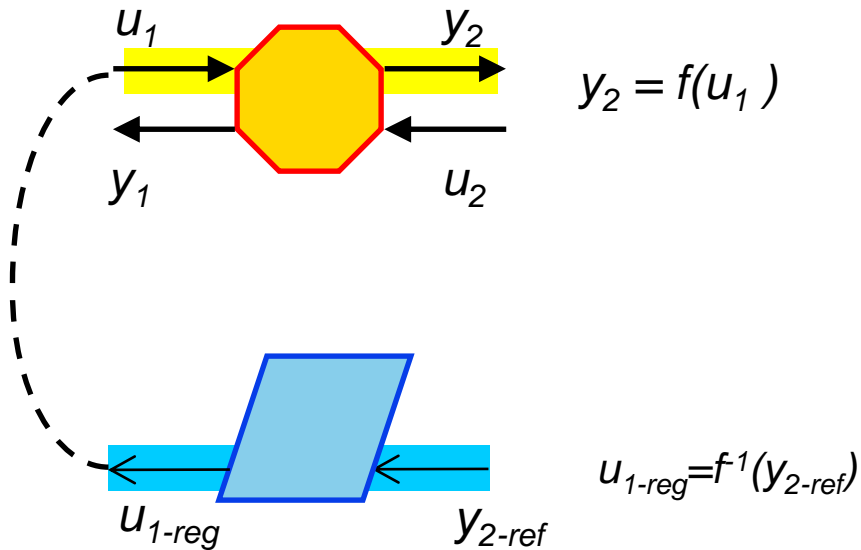
Indirect inversion  
(closed-loop control)

I/O relation with multiple Inputs



Multiple solutions

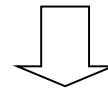
Objective: to control  $y_2$



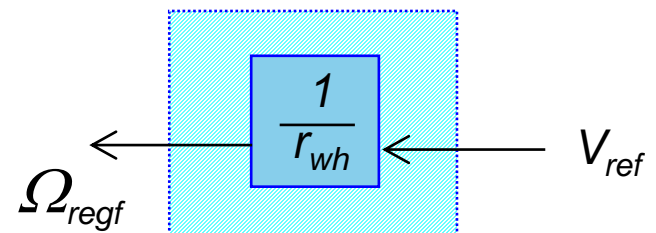
Direct Inversion

Ex : wheel

$$\begin{cases} V = r_{wh} \Omega \\ T = r_{wh} F \end{cases}$$

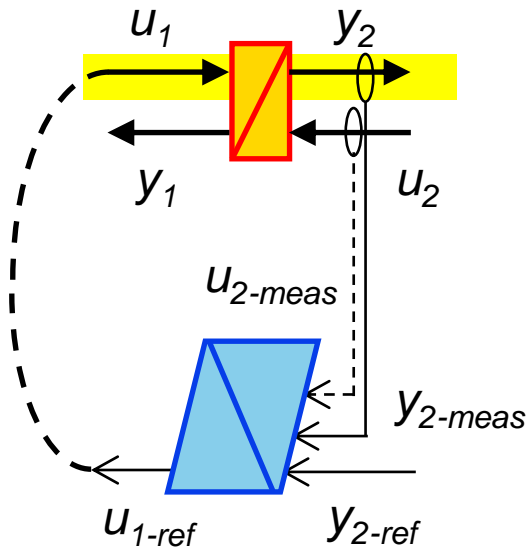


$$\Omega_{ref} = V_{ref} / r_{wh}$$





**Objective: to control  $y_2$**



$$y_2 = f(u_1, u_2)$$

$f$  is in integral form

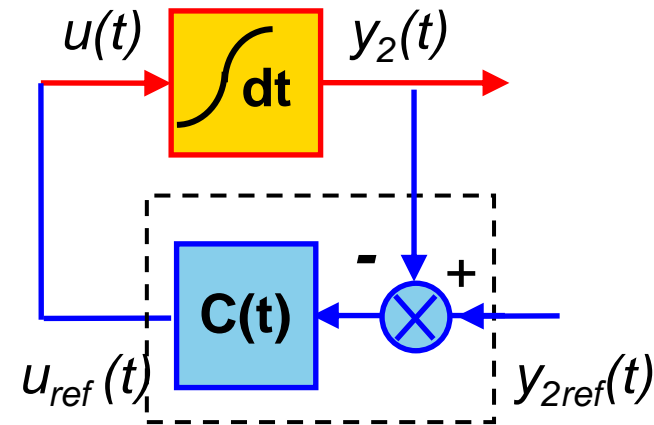
direct inversion

indirect inversion

**not possible in real-time**

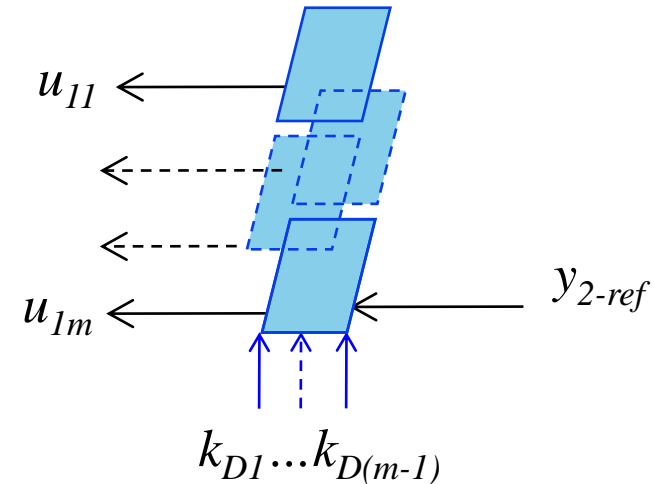
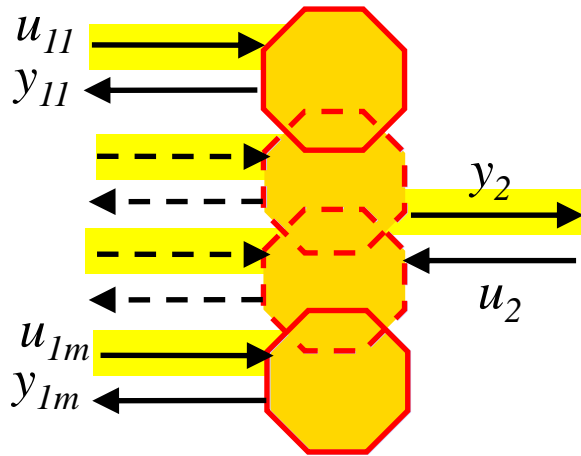
~~$$u_{\text{ref}}(t) = \frac{d}{dt} y_{\text{ref}}(t)$$~~

$$u(t) = u_1(t) - u_2(t)$$



$$u_{\text{ref}}(t) = C(t)[y_{2\text{ref}}(t) - y_{2\text{meas}}(t)]$$

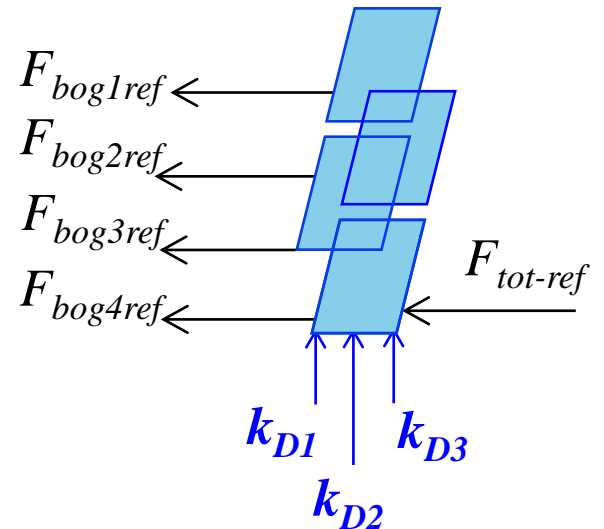
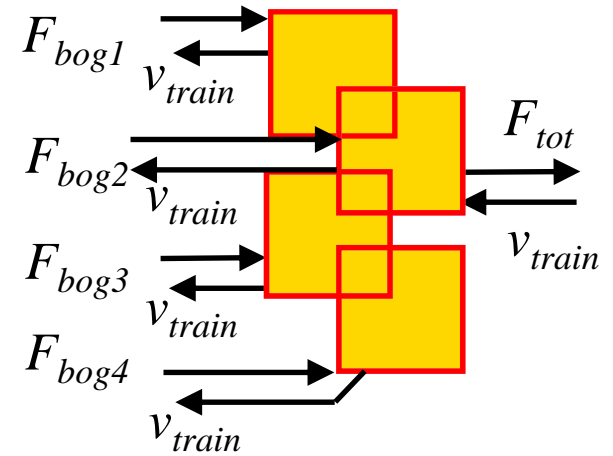
**closed loop controller**



no measurement  
no controller  
( $m - 1$ ) **distribution variables**

$$\left\{ \begin{array}{l} u_{11} = k_{D1} y_{2ref} \\ \dots \\ u_{1(m-1)} = k_{D(m-1)} y_{2ref} \\ u_{1m} = (1 - \sum k_{Di}) y_{2ref} \end{array} \right.$$

*Example: chassis of a train*



### Legend

Control = light blue  
 Parallelograms  
 with dark blue  
 contour

 direct inversion

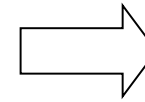
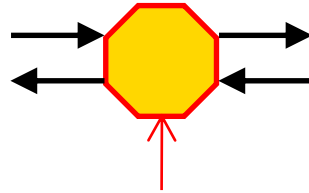
 indirect inversion

 sensor

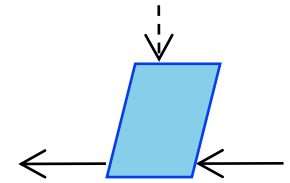
 mandatory link

 facultative link

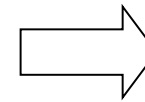
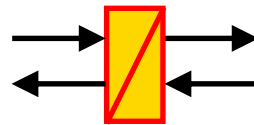
conversion element



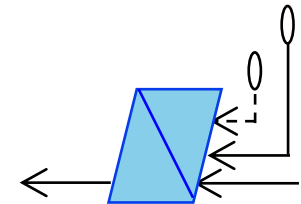
direct inversion +  
disturbance rejection



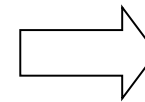
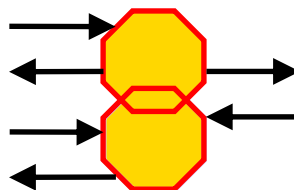
accumulation element



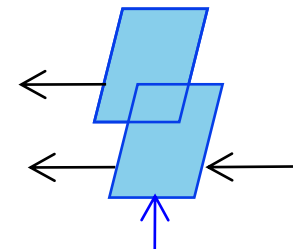
controller +  
disturbance rejection



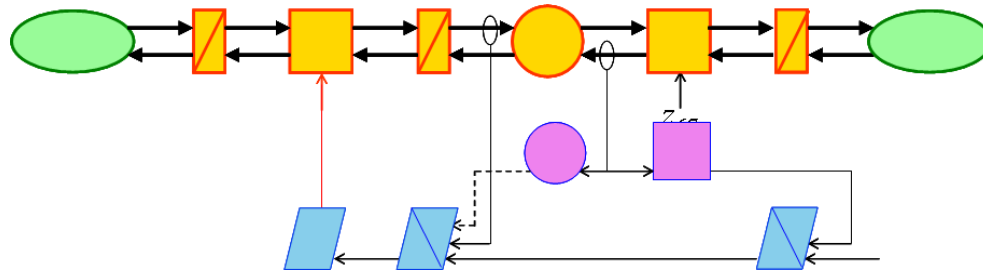
coupling element



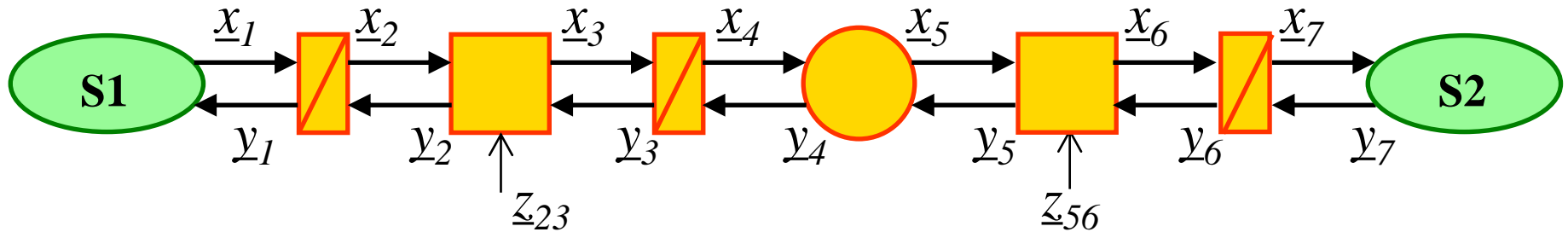
distribution criteria



### 3. Inversion-based control schemes



### 1. EMR of the system

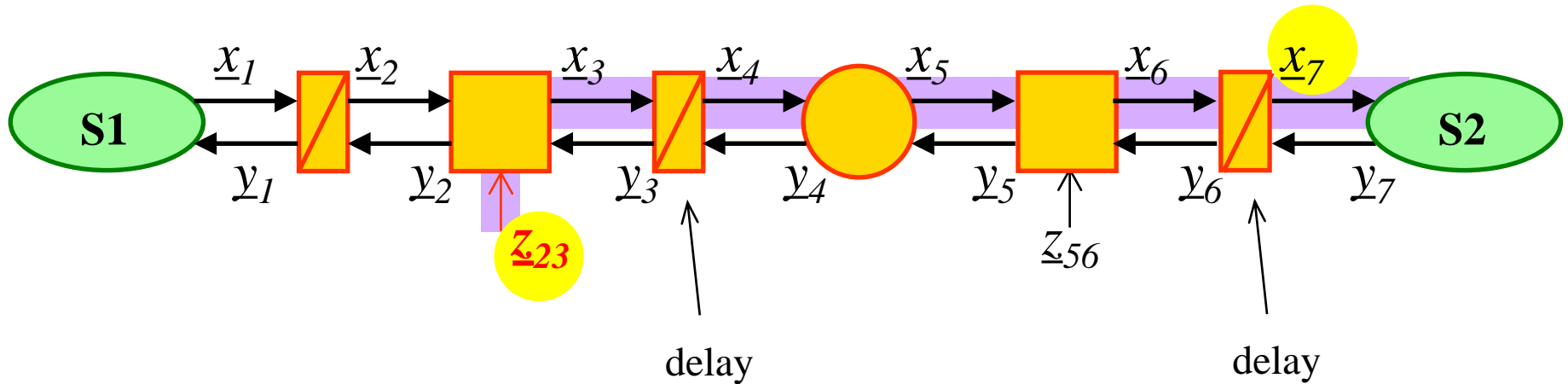


### EMR depends on:

- the study objective (limits between system and sources)
- the physical laws of subsystems (physical causality)
- the association of subsystems (systemic approach)

1. EMR of the system

2. Tuning path



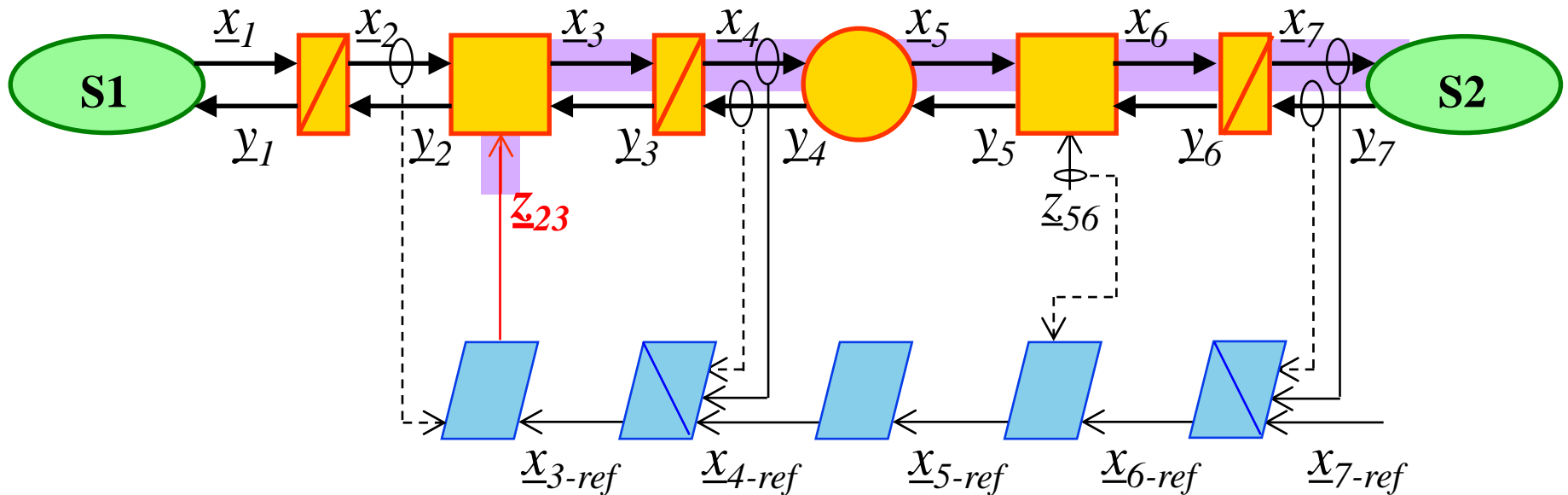
**The tuning path is:**

- dependant on the technical requirements (chosen tuning input / output to control)
- **independent of the power flow direction**

1. EMR of the system

2. Tuning path

3. Inversion step-by-step **Strong assumption: all variables can be measured!**



**Maximal Control Structure** (or scheme):

- maximum of sensors
- maximum of operations

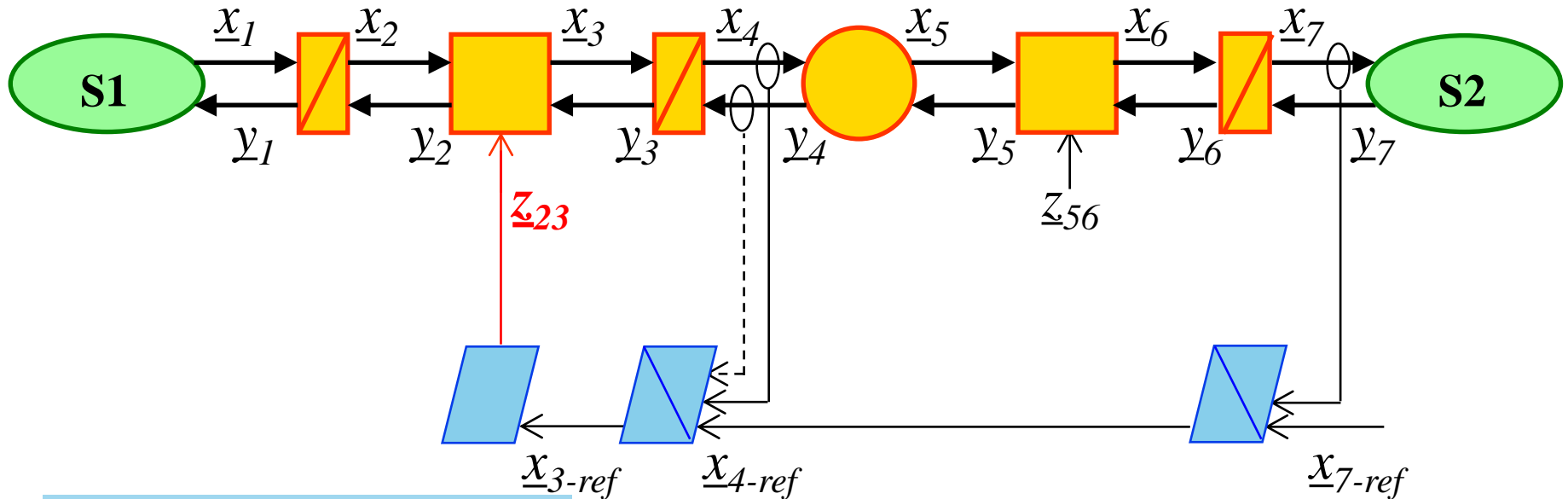
Example:

- 5 sensors
- 2 closed-loop controllers

1. EMR of the system

2. Tuning path

3. Inversion step-by-step **Strong assumption: all variables can be measured!**



4. Simplification of control

**Simplifications:**

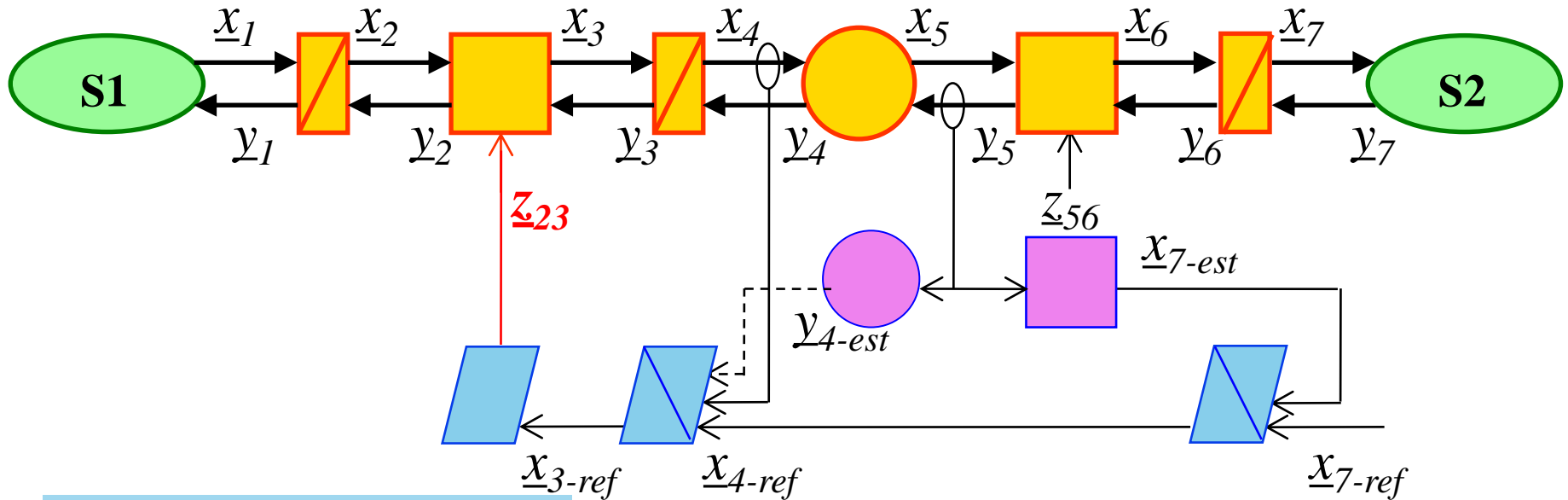
- non-consideration of disturbances  $\Rightarrow$  impact on the tuning and on the performances
- merging control blocks...



1. EMR of the system

2. Tuning path

3. Inversion step-by-step **Strong assumption: all variables can be measured!**



4. Simplification of control

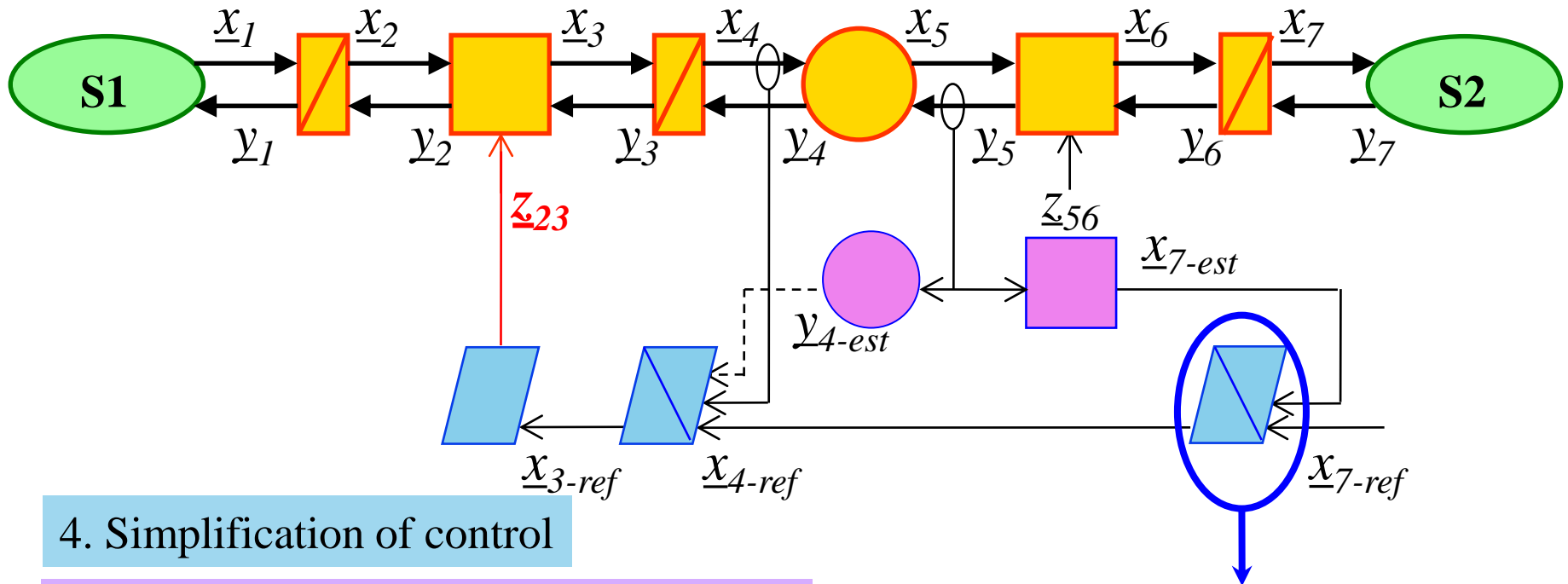
5. Estimation of non-measured variables

from measured variables

1. EMR of the system

2. Tuning path

3. Inversion step-by-step **Strong assumption: all variables can be measured!**



4. Simplification of control

5. Estimation of non-measured variables

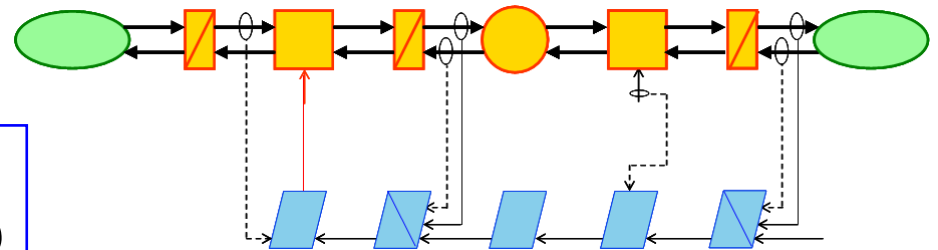
6. Tuning of controllers

PI / PID / fuzzy controller?  
Calculation of parameters?

1. EMR of the system
2. Tuning path
3. Inversion step-by-step

### Maximal Control Scheme

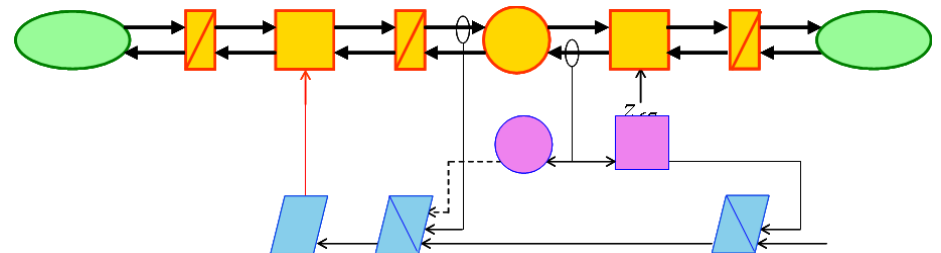
- mirror of the EMR (systematic)
- unique and theoretical solution



4. Simplification of control
5. Estimation of variables
6. Tuning of controllers

### Practical Control Schemes

- several solutions (expertise)
- reduced performances



## Conclusion

**Inversion based control = inversion of EMR**  
based on the cognitive systemic  
and the causality principle (energy)

### **Inversion rule for control scheme**

closed-loop control to invert accumulation, direct inversion for  
conversion element, degrees of freedom for coupling element



**EMR'22**

**Sion**

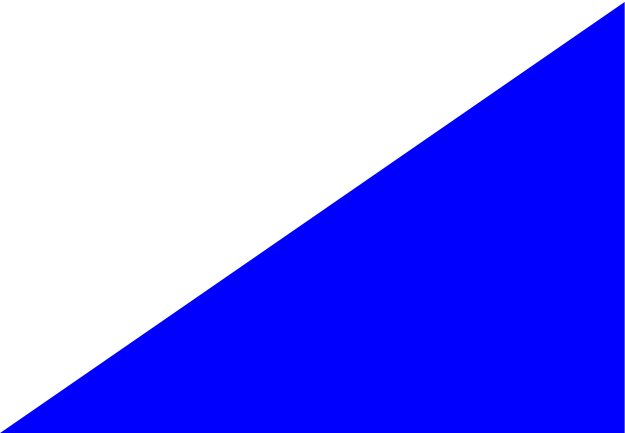
**June 2022**



**EMR'22 Summer School**  
**“Energetic Macroscopic Representation”**



# **BIOGRAPHIES AND REFERENCES**



[Barre 2006] P. J. Barre, A. Bouscayrol, P. Delarue, E. Dumetz, F. Giraud, J. P. Hautier, X. Kestelyn, B. Lemaire-Semail, E. Semail, "Inversion-based control of electromechanical systems using causal graphical descriptions", *IEEE-IECON'06*, Paris, November 2006.

[Bouscayrol 2000] A. Bouscayrol, B. Davat, B. de Fornel, B. François, J. P. Hautier, F. Meibody-Tabar, M. Pietrzak-David, "Multimachine multiconverter system: application for electromechanical drives", *European Physics Journal - Applied Physics*, vol. 10, no. 2, May 2000, p. 131-147 (common paper GREEN Nancy, L2EP Lille and LEEI Toulouse, according to the SMM project of the GDR-SDSE).

[Bouscayrol 2012] A. Bouscayrol, J. P. Hautier, B. Lemaire-Semail, "Graphic Formalisms for the Control of Multi-Physical Energetic Systems", *Systemic Design Methodologies for Electrical Energy*, tome 1, Analysis, Synthesis and Management, Chapter 3, ISTE Willey editions, October 2012, ISBN: 9781848213883

[Delarue 2003] P. Delarue, A. Bouscayrol, A. Tounzi, X. Guillaud, G. Lancigu, "Modelling, control and simulation of an overall wind energy conversion system", *Renewable Energy*, July 2003, 28(8), pp. 1159-1324 (common paper L2EP and Jeumont SA).

[Leclercq 2004] A. Leclercq, P. Sicard, A. Bouscayrol, B. Lemaire-Semail, "Control of a triple drive paper system based on the Energetic Macroscopic Representation", *IEEE-ISIE'04*, Ajaccio (France), May 2004, pp. 889-893.

[Djani 2006] Djani Wankam, Y., P. Sicard, A. Bouscayrol "Maximum control structure of a five-drive paper system using Energetic Macroscopic Representation," *IEEE IECON'2006*, Special Session Graphical Description for Modeling and Control Power Systems, Paris, France, November 2006, 5332-5337.

[Sicard 2009] P. Sicard, A. Bouscayrol, "Inversion-based control of electromechanical systems", EMR'09 summer school, Trois-Rivières, Canada, September 2009