

« EMR-based Model of a hybrid braking for BEV »

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- 1** Importance of brakes modelling in traction model
- 2** Heat equation and application to brakes
- 3** Brakes temperature estimation in EMR-based model



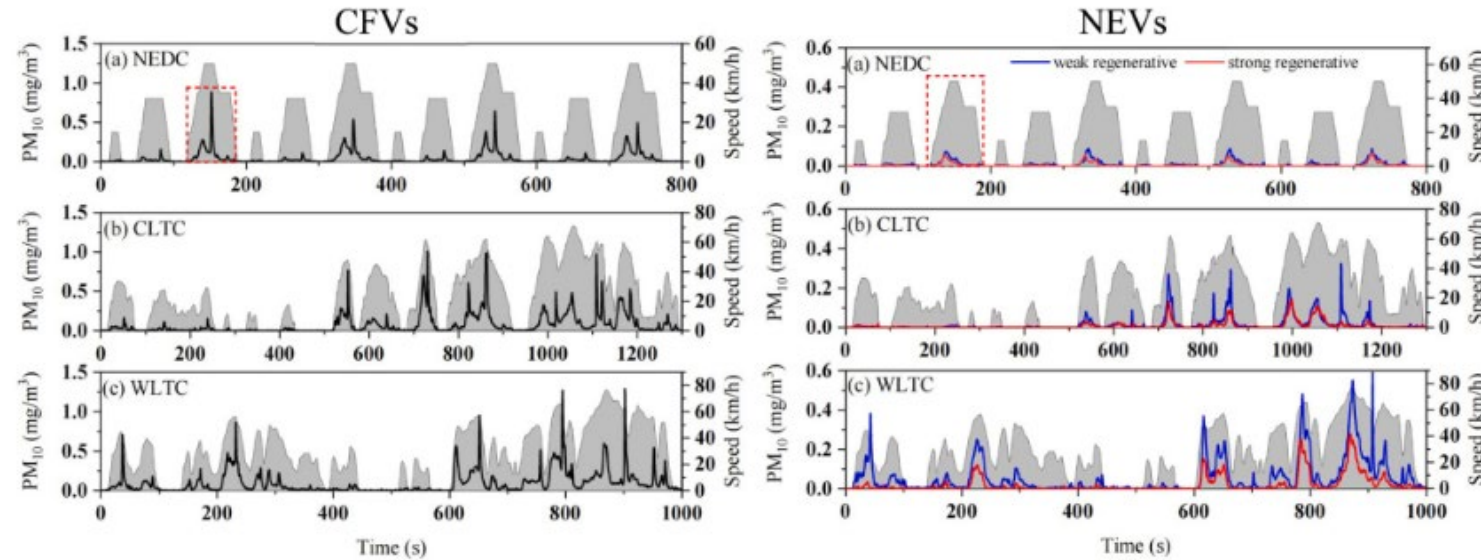
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«Importance of brakes modelling in traction model»

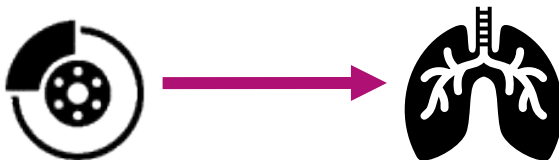
Non-exhaust emissions of a vehicle – brakes case

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Mass concentration emission characteristics of BWP from CFVs and NEVs under standard test cycle [Zhang 2024]

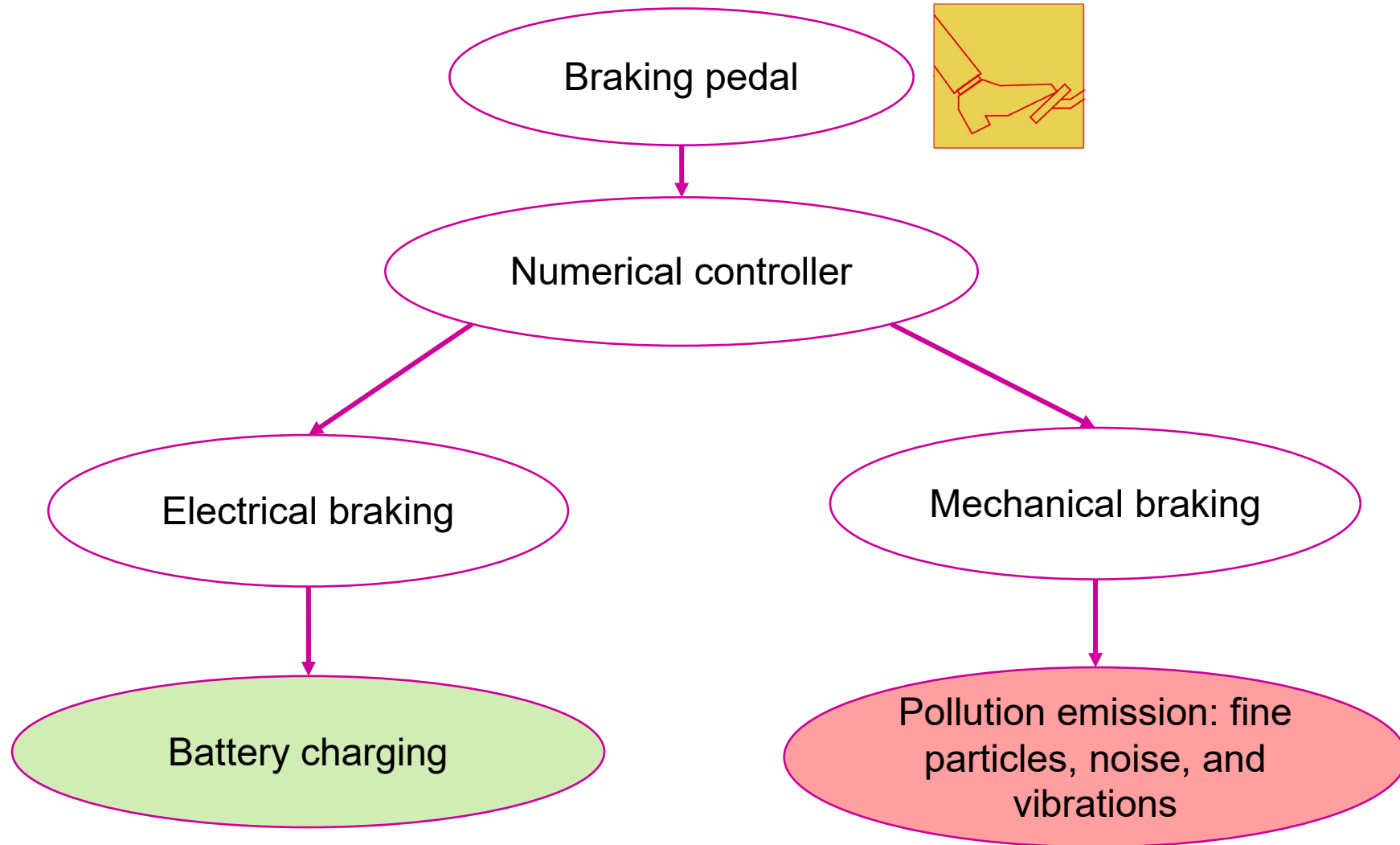


- Using mechanical braking leads to pollutants emissions such as noise and fine particles
- Security norms impose the usage of mechanical brakes
- Not using enough mechanical brakes may leads to instabilities

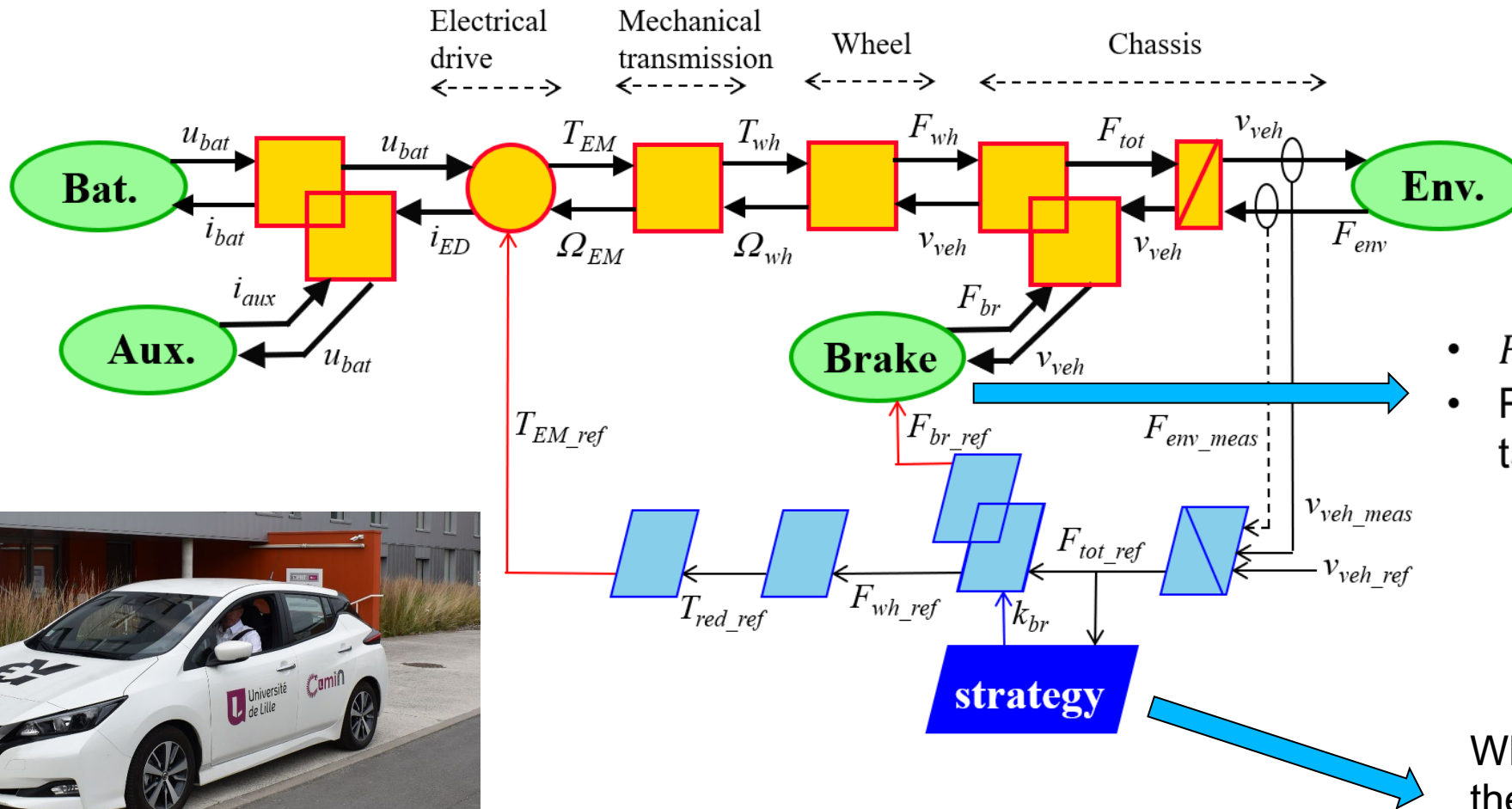
Brake-by-wire and electrical braking

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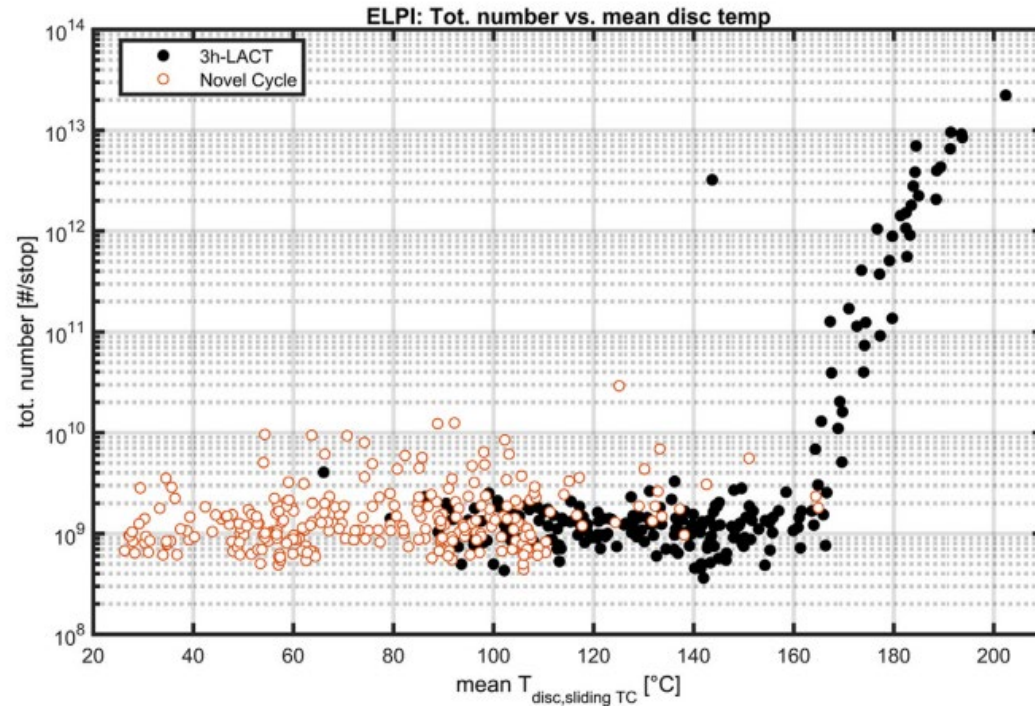
CURRENT MODEL AND CONTROL



- $F_{br} = F_{br_ref}$
- Particle emissions not taken into account

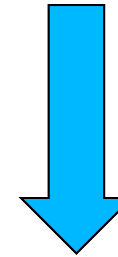
What braking strategy for the BEV?





Particle [6nm-10 μ m] number emissions and average disc temperature for several driving cycles [Mathissen 2018]

High temperature => high particles emissions
AND more ultrafine particles emissions



Need to estimate brakes temperature

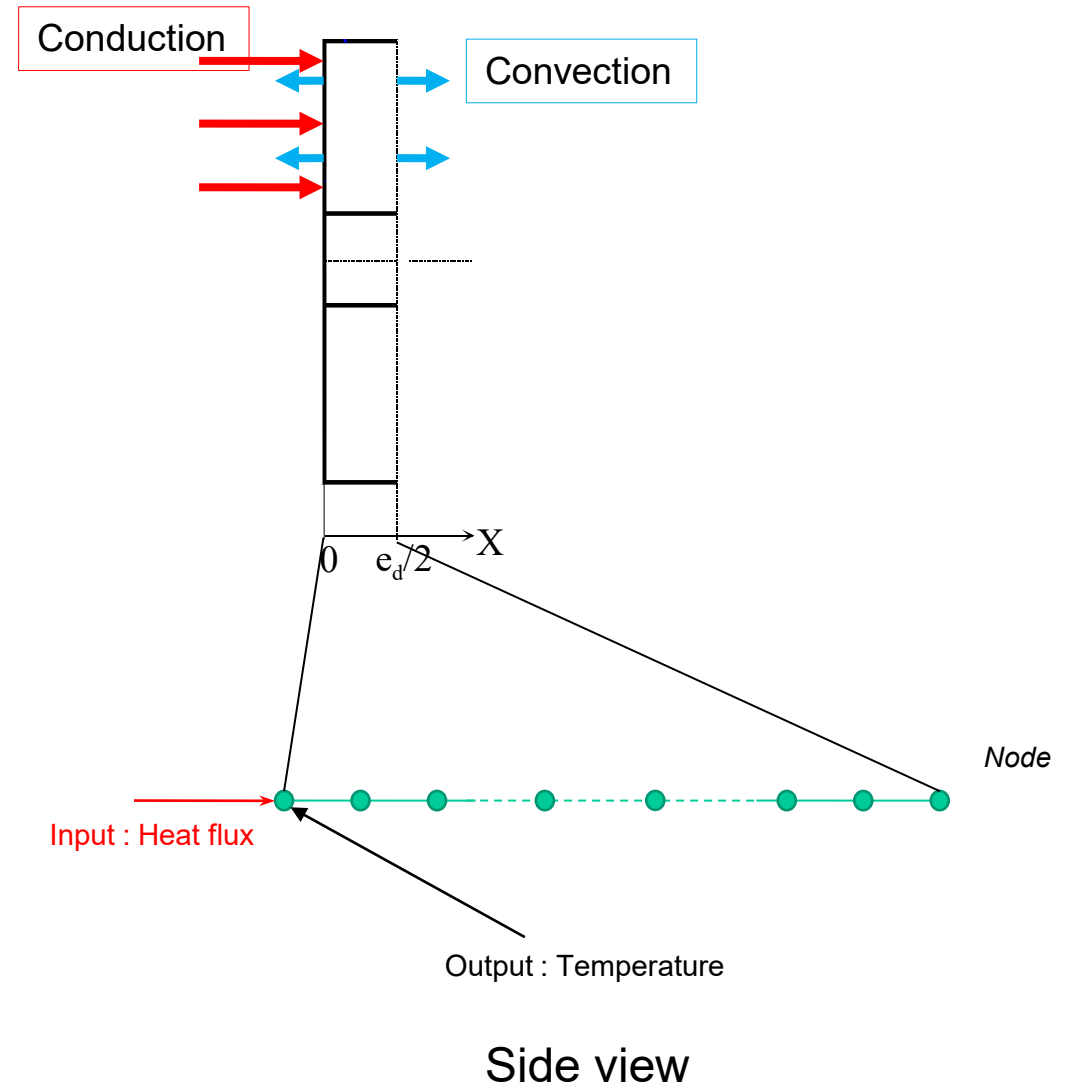
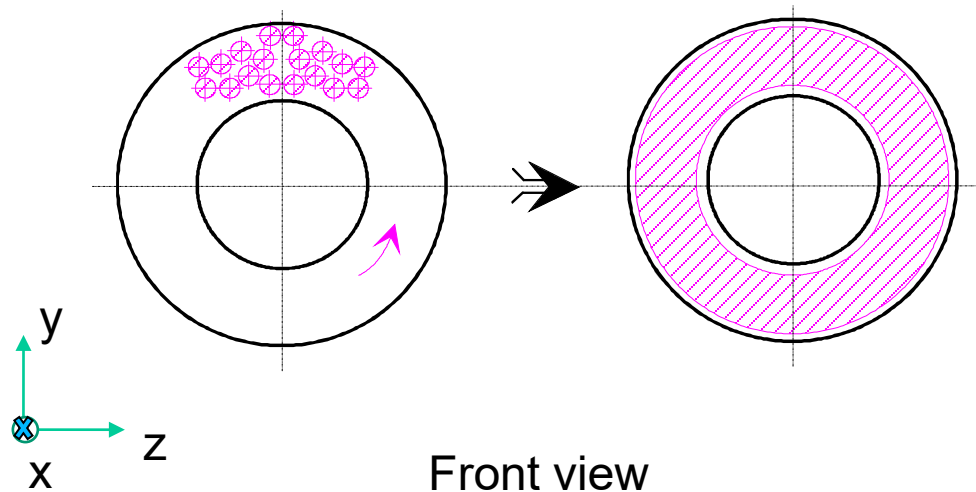


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«Heat equation and application to brakes»

Assumptions :

- Only thermal flux on the disk (not on the pad)
- Only half of the disk studied (symmetry)
- Heat is distributed over the entire surface of the disc during braking
- Thermal flux in only one direction



Heat equation

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$$\rho c \frac{dT}{dt} - \lambda \Delta T = \phi_{\text{cduct}} + \phi_{\text{cvect}}$$

Conduction during contact between pads and the disk => **heating**

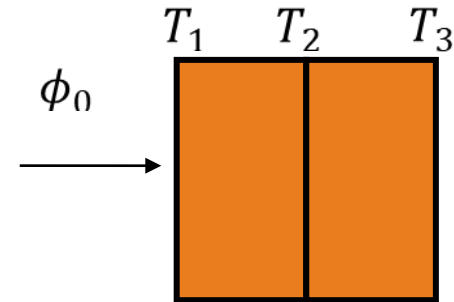
Convection with the air => **cooling**

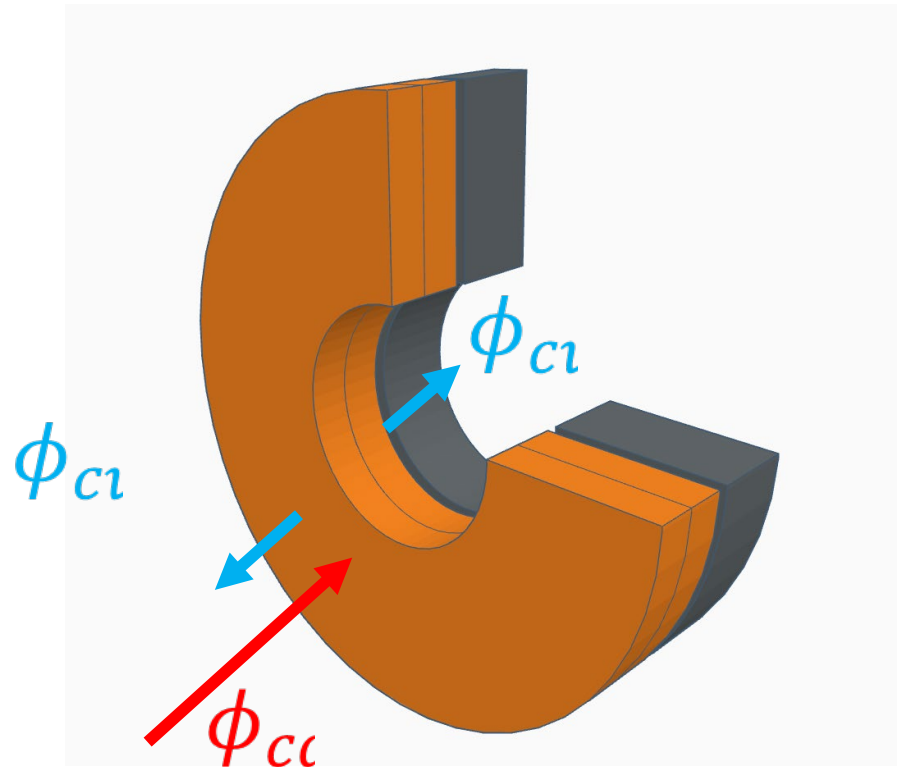
- Significant temperature rise at the surface, but slower heating of the overall disk
- Impossible to consider an average brake temperature

Simple mesh for the study

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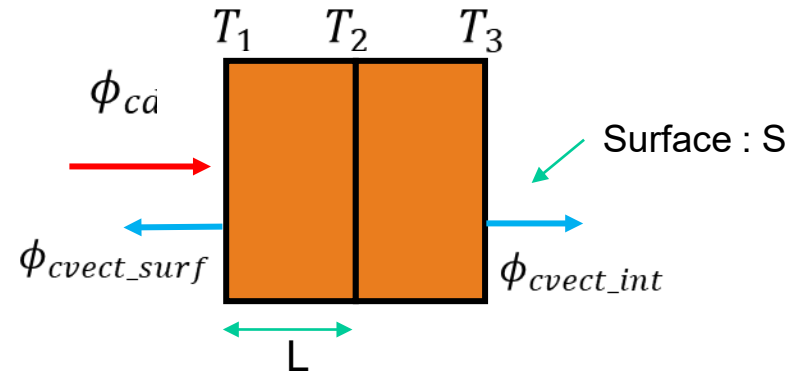
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Conduction effect

$$\phi_{cduct} = F_{T_gr} v_{veh}$$



Law of Fourier :

$$\begin{aligned} \phi_{1 \rightarrow 2} &= -\lambda \text{grad}(T) \\ &= -\lambda S \frac{T_2 - T_1}{L} = \frac{T_2 - T_1}{R_{th}} \end{aligned}$$

First law of thermodynamics : $dE = \underbrace{\rho c S L}_{C_{th}} dT = (\phi_{incoming} - \phi_{outgoing}) dt$

$$\begin{pmatrix} C_{th} & 0 & 0 & 0 \\ 0 & C_{th} & 0 & 0 \\ 0 & 0 & C_{th} & 0 \\ 0 & 0 & 0 & C_{th} \end{pmatrix} \begin{pmatrix} \frac{dT_1}{dt} \\ \frac{dT_2}{dt} \\ \frac{dT_3}{dt} \\ \frac{dT_3}{dt} \end{pmatrix} + \begin{pmatrix} \frac{1}{R_{th}} & -\frac{1}{R_{th}} & 0 \\ -\frac{1}{R_{th}} & \frac{1}{R_{th}} & -\frac{1}{R_{th}} \\ 0 & -\frac{1}{R_{th}} & \frac{1}{R_{th}} \\ 0 & -\frac{1}{R_{th}} & \frac{1}{R_{th}} \end{pmatrix} \begin{pmatrix} T_1 \\ T_2 \\ T_3 \\ T_3 \end{pmatrix} = \begin{pmatrix} \phi_{cduct} \\ \phi_{cduct} + hST_{ext} \\ 0 \\ hST_{ext} \end{pmatrix}$$

Convection effect

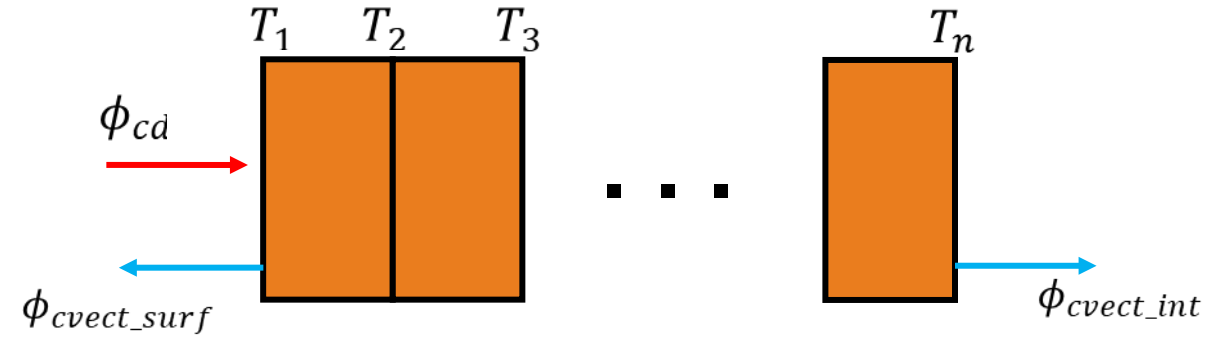
$$\phi_{cvect_surf} = hS(T_1 - T_{ext})$$

$$\phi_{cvect_int} = hS(T_3 - T_{ext})$$

Complexification of the mesh

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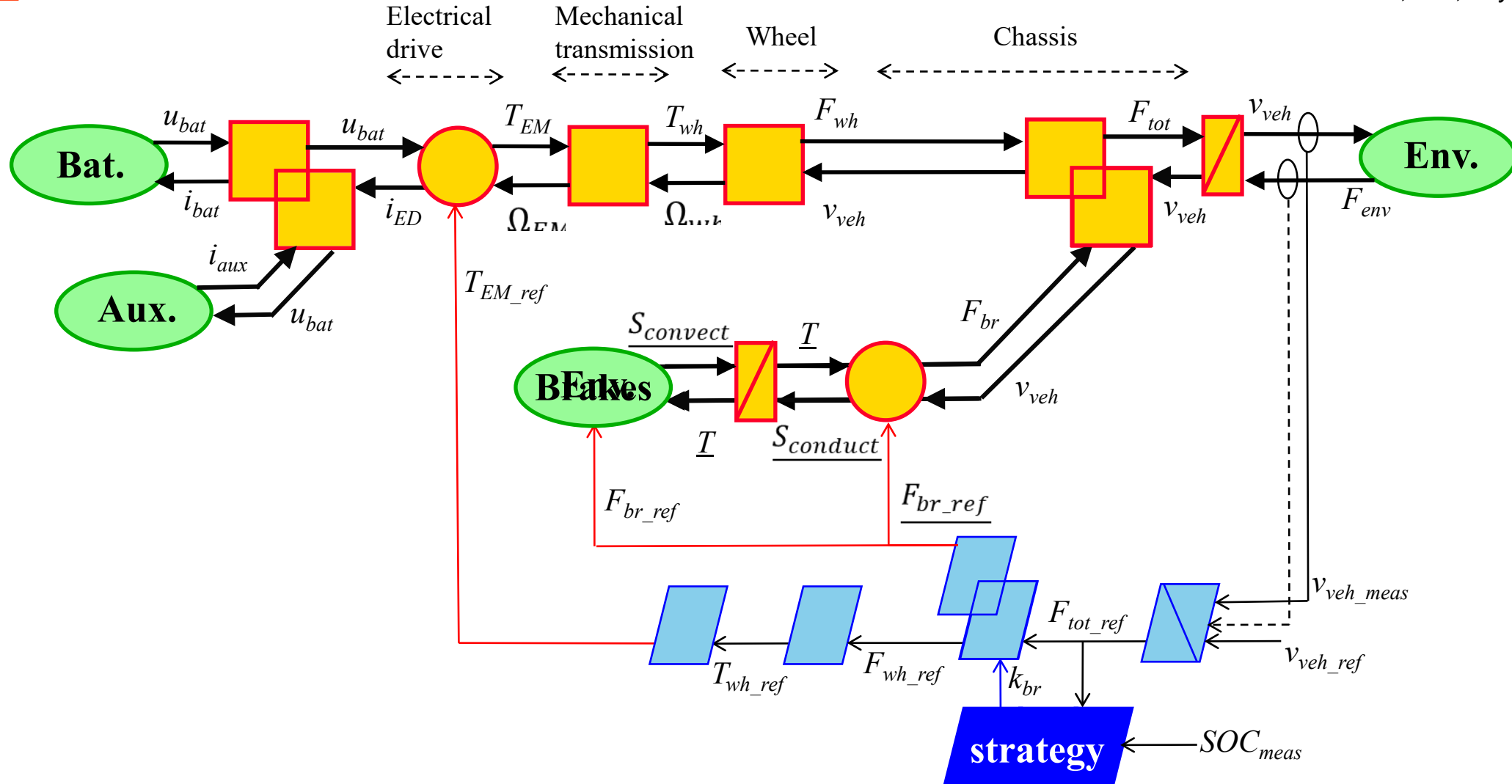


$$\underbrace{\begin{bmatrix} C_{th} & 0 & \dots & 0 \\ 0 & C_{th} & \dots & 0 \\ \vdots & \vdots & \ddots & \vdots \\ 0 & 0 & \dots & C_{th} \end{bmatrix}}_{[\mathcal{C}]} + \underbrace{\begin{bmatrix} \frac{dT_1}{dt} \\ \frac{dT_2}{dt} \\ \frac{dT_3}{dt} \\ \vdots \\ \frac{dT_n}{dt} \end{bmatrix}}_{\frac{d}{dt}} + \underbrace{\begin{bmatrix} \frac{1}{R_{th}} + hS & -\frac{1}{R_{th}} & 0 & \dots & 0 & 0 & 0 \\ -\frac{1}{R_{th}} & \frac{2}{R_{th}} & -\frac{1}{R_{th}} & \dots & 0 & 0 & 0 \\ 0 & -\frac{1}{R_{th}} & \frac{2}{R_{th}} & \dots & 0 & 0 & 0 \\ \vdots & \vdots & \vdots & \ddots & \vdots & \vdots & \vdots \\ 0 & 0 & 0 & \dots & \frac{2}{R_{th}} & -\frac{1}{R_{th}} & 0 \\ 0 & 0 & 0 & \dots & -\frac{1}{R_{th}} & \frac{2}{R_{th}} & -\frac{1}{R_{th}} \\ 0 & 0 & 0 & \dots & 0 & -\frac{1}{R_{th}} & \frac{1}{R_{th}} + hS \end{bmatrix}}_{[\mathcal{U}]} \underbrace{\begin{bmatrix} T_1 \\ T_2 \\ T_3 \\ \vdots \\ T_n \end{bmatrix}}_{\underline{T}} = \underbrace{\begin{bmatrix} \phi_{cd} + hST_{ext} \\ 0 \\ 0 \\ \vdots \\ hST_{ext} \end{bmatrix}}_{\underline{\Phi}}$$

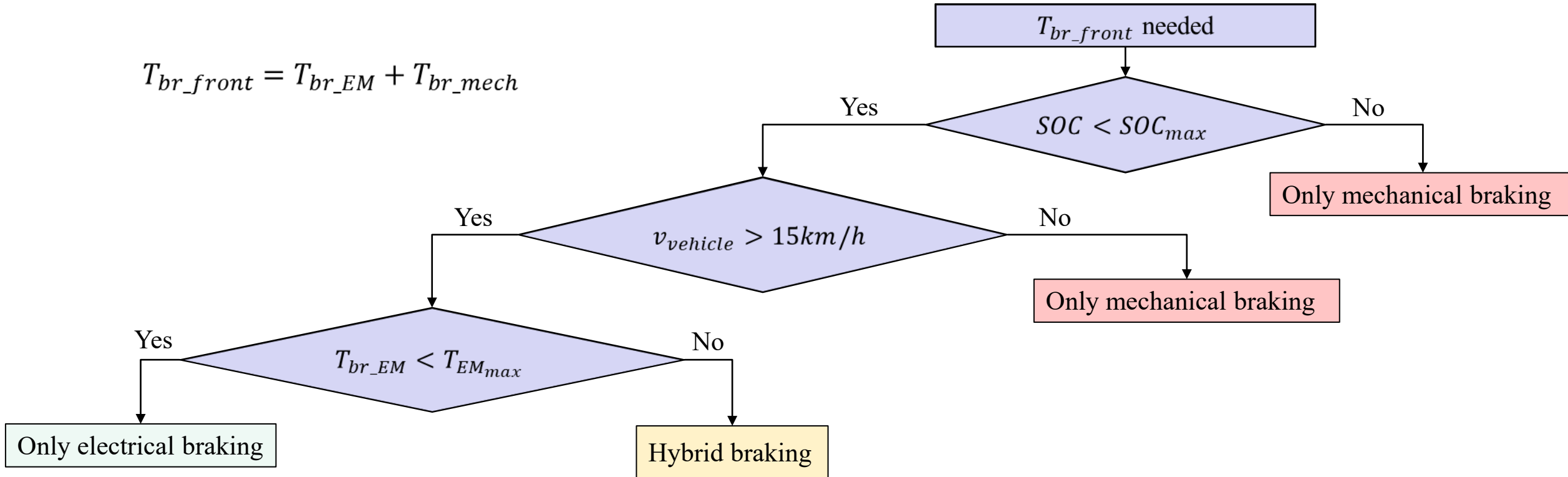


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«Brakes temperature estimation in EMR-based model»



$$T_{br_front} = T_{br_EM} + T_{br_mech}$$



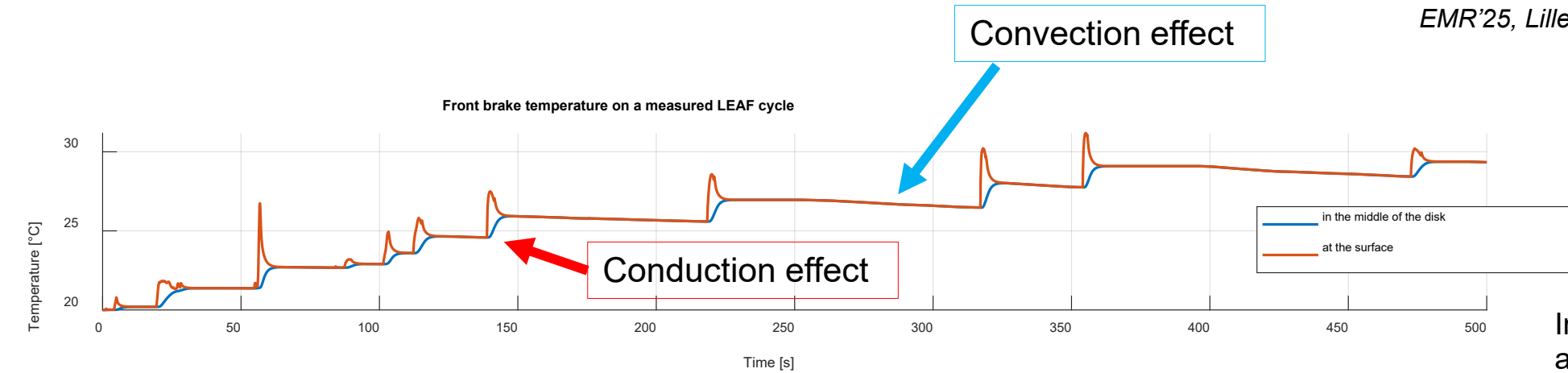
« As much electrical braking as possible »

EMR-based Model of a Hybrid Braking for BEV

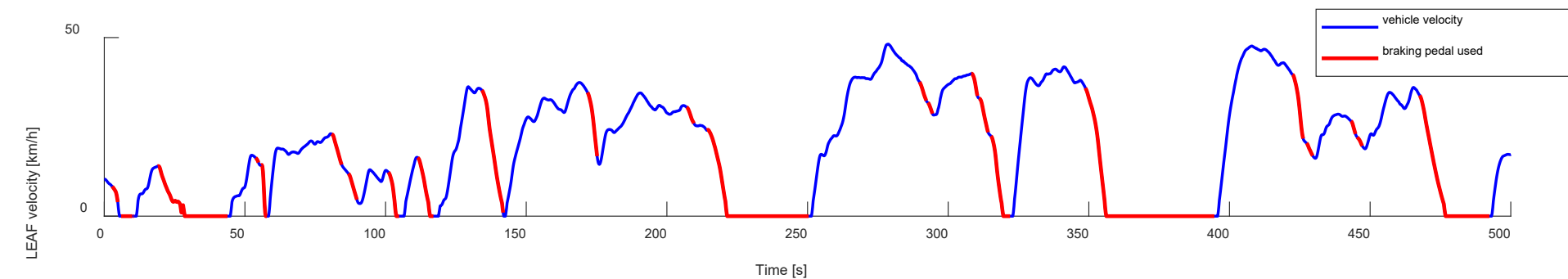
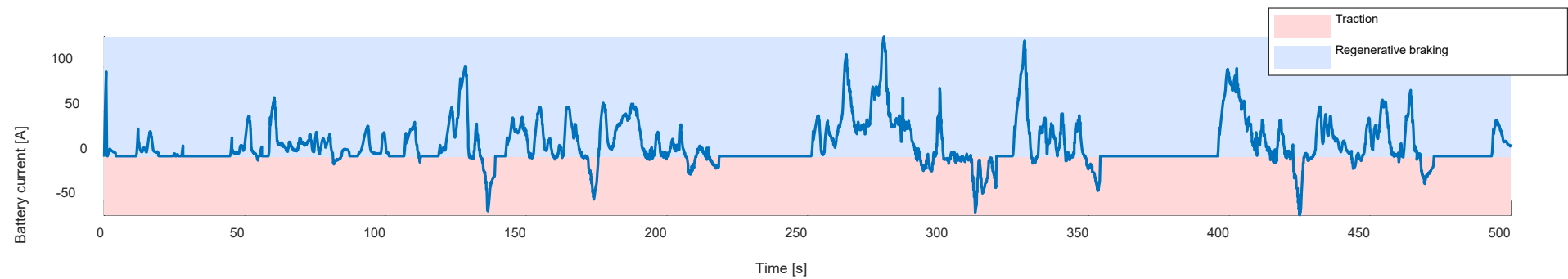
First results

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Importance of non-average model



Conclusion and perspectives

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Conclusion :

- Estimation of brakes temperature during a driving cycle
- Integration into a EMR-based model of a electric vehicle

Perspectives :

- Creation of a map linking particles emissions and brake temperature
- Adaptive strategy to limitate particles emissions from braking



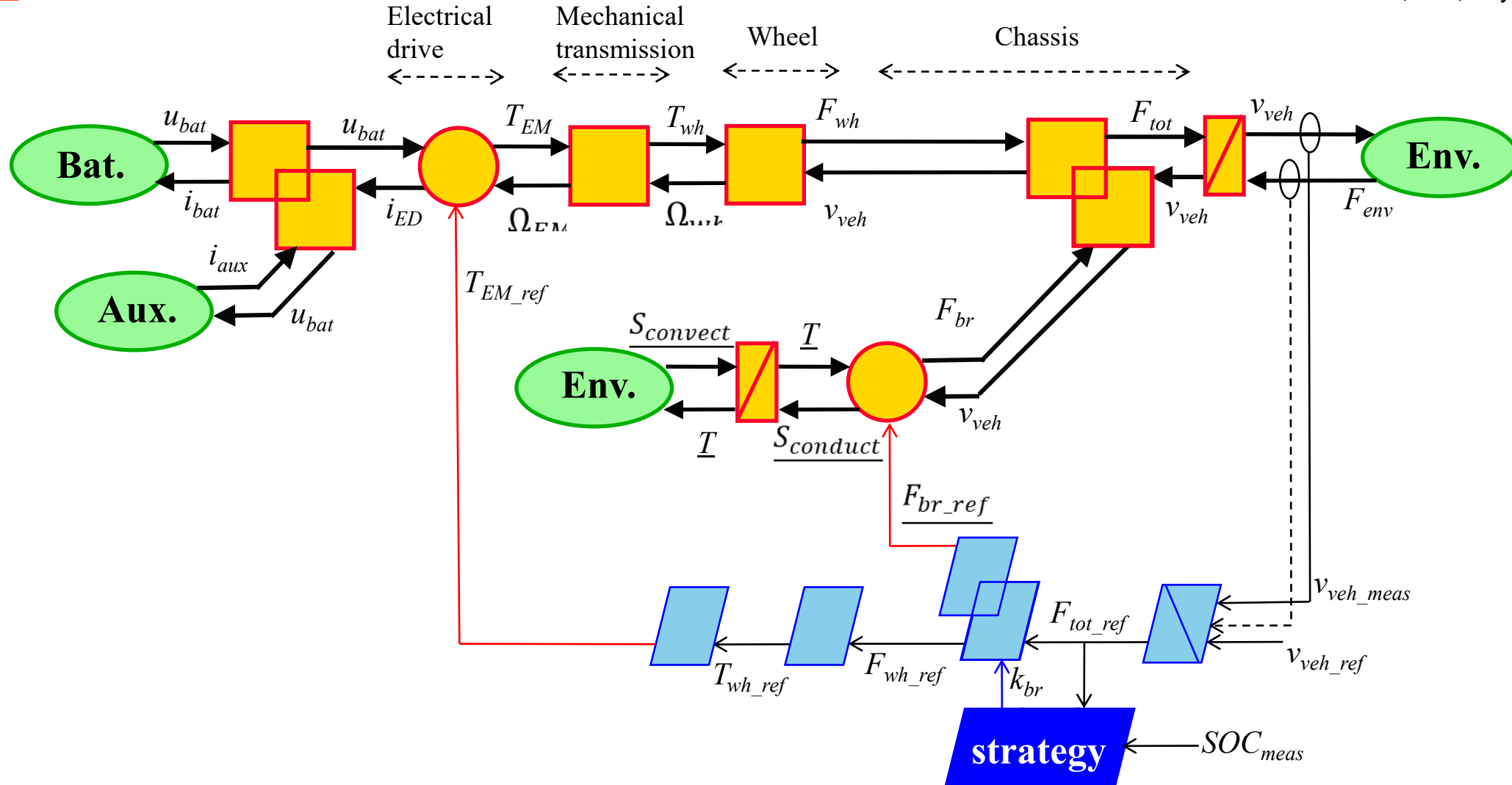
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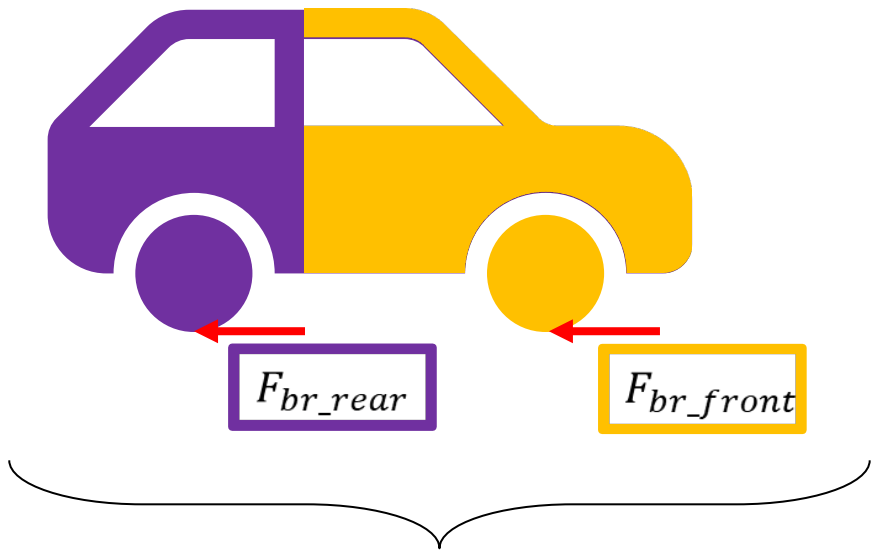
Thanks for your attention !



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« Annex »

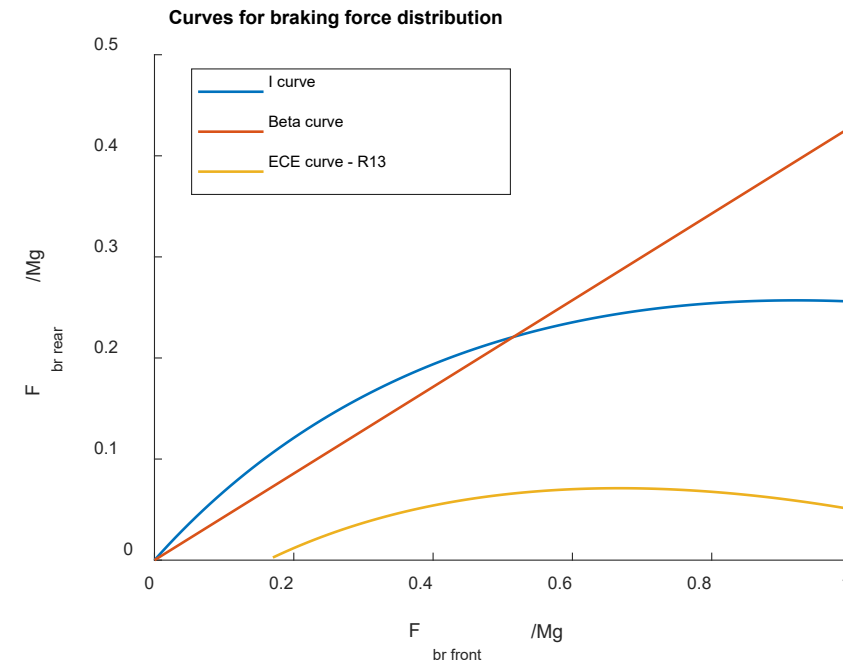


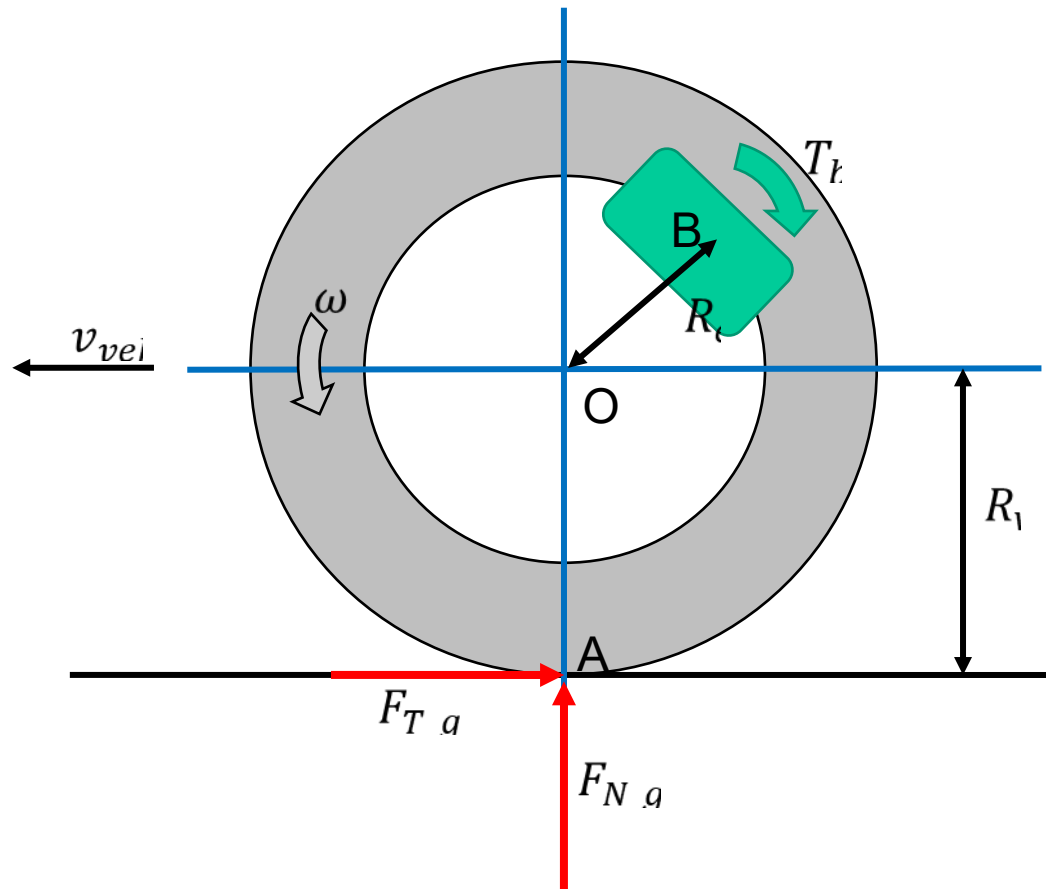


Industrial choice : fix distribution of braking between front and rear brakes : 70% at front and 30% at rear

Assumptions :

- Bicycle model : equidistribution of strength between left and right
- Only electrical braking available at front





$$T_{br} = F_{T_{gr}} R_{wh}$$

$$T_{br} = F_{T_{br}} R_{eff_{br}}$$

$$F_{T_{br}} = \mu_{br} F_{N_{br}}$$

$$\Phi_{th} = \mu_{br} F_{N_{br}} v_{veh} \frac{R_{eff_{br}}}{R_{wh}}$$

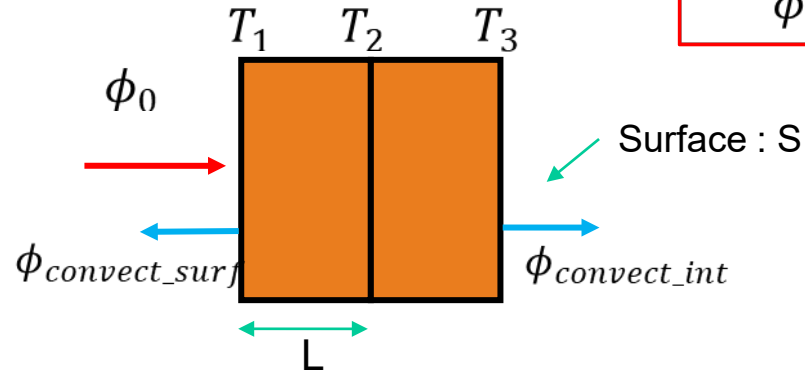
$$\Phi_{th} = \frac{R_{wh}}{R_{eff_{br}}} F_{T_{gr}} v_{veh} \frac{R_{eff_{br}}}{R_{wh}}$$

$$\Phi_{th} = F_{T_{gr}} v_{veh}$$

Thermal / electrical analogy for a simple example

Conduction effect

$$\phi_0 = F_{T_gr} v_{veh}$$

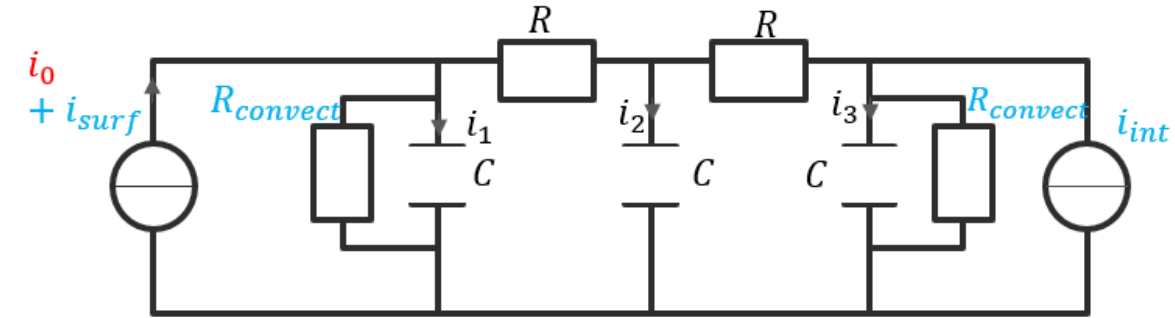


Convection effect

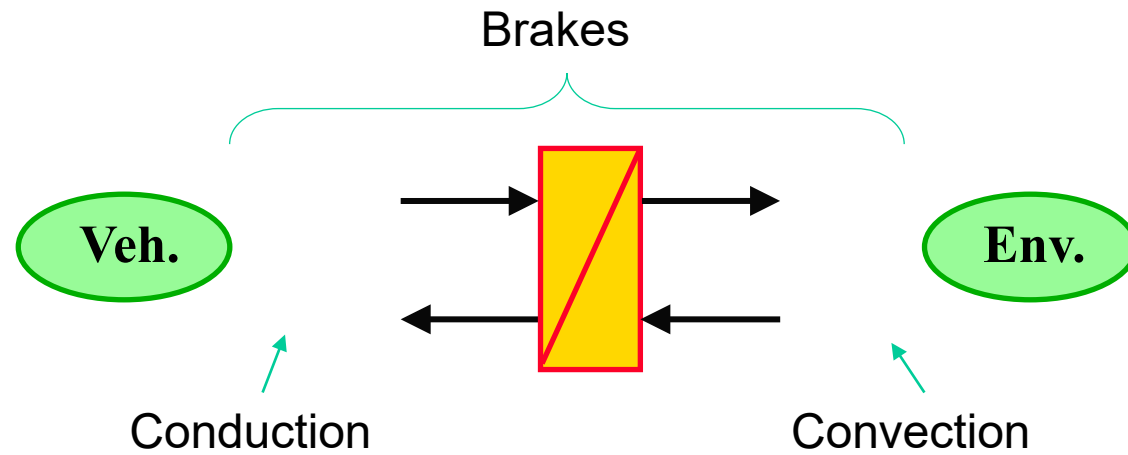
$$\phi_{convect_surf} = h(v_{veh})S(T_1 - T_{ext})$$

$$\phi_{convect_int} = h(v_{veh})S(T_3 - T_{ext})$$

$$\begin{pmatrix} C_{th} & 0 & 0 \\ 0 & C_{th} & 0 \\ 0 & 0 & C_{th} \end{pmatrix} \begin{pmatrix} \frac{dT_1}{dt} \\ \frac{dT_2}{dt} \\ \frac{dT_3}{dt} \end{pmatrix} + \begin{pmatrix} \frac{1}{R_{th}} + hS & -\frac{1}{R_{th}} & 0 \\ -\frac{1}{R_{th}} & \frac{2}{R_{th}} & -\frac{1}{R_{th}} \\ 0 & -\frac{1}{R_{th}} & \frac{1}{R_{th}} + hS \end{pmatrix} \begin{pmatrix} T_1 \\ T_2 \\ T_3 \end{pmatrix} = \begin{pmatrix} \phi_0 + hST_{ext} \\ 0 \\ hST_{ext} \end{pmatrix}$$

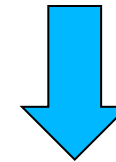


$$\begin{pmatrix} C & 0 & 0 \\ 0 & C & 0 \\ 0 & 0 & C \end{pmatrix} \begin{pmatrix} \dot{u}_1 \\ \dot{u}_2 \\ \dot{u}_3 \end{pmatrix} + \begin{pmatrix} \frac{1}{R} + \frac{1}{R_{conv}} & -\frac{1}{R} & 0 \\ -\frac{1}{R} & \frac{2}{R} & -\frac{1}{R} \\ 0 & -\frac{1}{R} & \frac{1}{R} + \frac{1}{R_{conv}} \end{pmatrix} \begin{pmatrix} u_1 \\ u_2 \\ u_3 \end{pmatrix} = \begin{pmatrix} i_0 + i_{surf} \\ 0 \\ i_{int} \end{pmatrix}$$



$\underline{q} \longrightarrow \text{in W}$

$\underline{T} \longrightarrow \text{in K}$



Use of 2 entropy flow [W/K] :

$\underline{S}_{conduct}$ and $\underline{S}_{convect}$



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« Biographies and references »

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